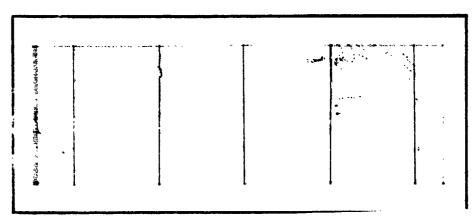
NASA UR- 1525-79



(NASA-CR-152579) TDRSS TELECOMMUNICATIONS SYSTEM, PN CODE ANALYSIS Final Report (Gold (Robert) Associates, Los Angeles, Calif.) 442 p HC A19/MF A01 CSCL 17B N77-29350

Unclas G3/32 44209

RGA



ROBERT GOLD ASSOCIATES

435 SOUTH LA CIENEGA BOULEVARD . LOS ANGELES, CALIFORNIA 90048

FINAL REPORT

TDRSS TELECOMMUNICATIONS SYSTEM PN CODE ANALYSIS

Contract NAS 5-22546

Prepared for

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION GODDARD SPACE FLIGHT CENTER Greenbelt, Maryland 20771

August 31, 1976

Robert Dixon Robert Gold Fred Kaiser

Robert Gold Associates 435 South La Cienega Boulevard Los Angeles, California 90048

TABLE OF CONTENTS

t T

1

				Page
LIST (OF TA	BLES .		v
LIST (OF FIG	GURES .		vii
1.0	INTF	ODUCTIO	ON	1-1
	1.1	General		1-1
		1.1.1	Contents of Report	1-1
	1.2	System 1	Design Considerations	1-5
	1.3	Link Ana	alysis	1-8
		1.3.1 1.3.2	Introduction	1-8 1-8
2.0	SUM	MARY OF	RESULTS	2-1
	2.1	Forward	Link Multiple Access	2-1
		2.1.1 2.1.2 2.1.3	Recommended Parameters	2-1 2-5 2-8
	2.2	Return I	· Link	2-22
		2. 2. 1 2. 2. 2 2. 2. 3	System Parameters	2-22 2-24 2-27
	Appe	ndix A.2	General Comparison of Biphase and Quadriphase (Double-Binary) Modulation	2-31
3.0	SUBS	SYSTEM I	DESIGN	3-1
	3.1	User Tr	ansponder	3-1
		3.1.1 3.1.2	Overall Design	3-2
			Transponders	3-9
	3. 2	Ground 1	Receiver	3-19
4.0	SYNO	CHRONIZ	ATION TECHNIQUES AND ANALYSIS	4 - 1
	4 4	T., 4.,	• •	

Table of Contents (continued)

		<u>-</u>	Page
4.2	Synchro	nization of Receive System	4-3
	4. 2. 1 4. 2. 2	Outline of Candidate Acquisition	4-3
	4.2.3		4- 3 4- 5
4.3	Analysi	s of Acquisition Techniques	4-12
	4.3.1 4.3.2 4.3.3	Sequential Detection Test	4-12 4-17
	4.3.4 4.3.5 4.3.6 4.3.7	Code Doppler Analysis	4-28 4-36 4-37 4-39 4-51
4.4	Applica Forwar	tion of Analysis to User Transponder - d Link	4-57
	4.4.1 4.4.2	Performance Summary	4-57
	4.4.3		4-67 4-80
4.5	Applica	tion of Analysis to Ground Receiver	4-92
	4.5.1	Performance Summary - Multiple Access Link	4-92
4.6	Impact Parame	of Multipath on Direct Sequence Acquisition eters	4-100
	4.6.1 4.6.2 4.6.3 4.6.4 4.6.5 4.6.6 4.6.7 4.6.8	Multipath Parameters	4-100 4-103 4-106 4-106 4-122 4-125 4-136
4.7	Referen	nces	4-142
COD	E GENEI	RATION TECHNIQUES FOR TDRS	5-1
5.1	Introdu	ction	5-1
5.2	Some R	Remarks on Code Tables	5-2

5.0

Table of Contents (continued)

			Page
5.3	Preferre	ed Pairs of Linear PN Codes	5-7
5.4	Generati	ion of TDRS Band Spreading Codes	5-10
	5. 4. 1 5. 4. 2	Introduction	5-10
	5.4.3	PN Sequence	5-11
		Codes	5-12
	5.4.4	Determination of Initial Conditions	5-13
5.5	The Effe	ect of Clock Error on Acquisition	5-16
	5.5.1	Introduction	5-16
	5.5.2	Notation	5-16
	5.5.3	Analysis	5-16
5.6	Code Lil	oraries for TDRS	5-21
	5. 6. 1 5. 6. 2	Forward Link Multiple Access Library Code Library for Mode 2 Return Link	5-21
		and Its Properties	5-24
	5.6.3	Dedicated Return Link Mode 1 Code	5-29
5.7	Listing of	of TDRSS User Code Libraries	5-31
5.8		Implementation of Shift Register Code	
	Generate	ors	5-36
5.9	Referen	ces	5-39
Appendix A. Appendix B.		elation Properties of Gold Codes	5-40
Appendix C.	Outpu	at Sequence and Output of kth Tap	5-64
	Phase	e Shifts of 18-Stage Maximal Codes	5-120
Appendix D.	-	outer Program Listing for Determination lelobe Distribution of Gold Codes	5-140
Appendix E.		e of Preferred Pairs of Maximal Poly-	3-140
rippendix 2.		als of Degree 11, 13, 15, 18, 19	5-175
Appendix F.		outer Program Listing for Generation of	
	_	erred Pairs of Maximal PN Sequences	5-190
Appendix G.		Library for Forward Link Range Channel -	
• •		mal PN Codes of Period 2 ¹⁸ -1 Having Six	
		ess Feedback Taps in the Generating Shift	
	Regis		5-196
Appendix H.	5 Alter	nate Code Library for Mode 1 Return Link -	
	Maxi	mal PN Codes of Period 2 ¹⁸ -1 Having Six or	
	Less	Feedback Taps in the Generating Shift Register	5-198

LIST OF TABLES

Table		Page
1.3-1	Link Analysis for MA Forward Link, S-Band	1-9
1.3-2	Link Analysis for SSA Forward Link, S-Band	1-10
1.3-3	Link Analysis for KSA Forward Link	1-11
1.3-4	Return Link Analysis	1-13
2.1-1	PN Code Lengths	2-5
2.1-2	User Transponder Design	2-10
2.1-3	Component Estimate	2-11
2.1-4	Total Power Estimate	2-12
2.1-5	Power Amplifier Estimate	2-12
2.1-6	Total Weight	2-12
2.1-7	Transponder Specifications	2-13
2.1-8	Comparative Summary of Average Acquisition Times for the MA Forward Link Short PN Code	2-19
2.1-9	Summary of Average Acquisition Times for the SA Forward Link Short PN Code	2-19
2.1-10	Comparative Summary of Mean Acquisition Times for Multiple Access Forward Link Long PN Code	2-20
2.2-1	Detection Performance of Desired and Interfering Signals	2-30
2.2-2	Average Acquisition Time vs. Code Length	2-30
3.1-1	Measured AM/PM Conversion for Various Traveling Wave Tube Amplifiers	3-18
4.2-1	Candidate Acquisition Techniques	4-5
4.2-2	Comparative Evaluation of Candiate Acquisition Techniques	4-8
4.3-1	Cross-Correlation Spectrum	4-43
4, 3-2	Baseline IF Signal-to-Noise Ratios	4-50
4.4-1	Threshold SNR Versus IF Bandwidth	4-58
4.4-2	Comparative Summary of Mean Acquisition Times for the Multiple Access Forward Link Short PN Code	4-62
4.4-3	Comparative Summary of Mean Acquisition Times for Multiple Access Forward Link Long PN Code	4-65

List of Tables (continued)

(

14.1.1 出て発音の名は一種の対象の対象の対象をあるがです。 まなが 後のでは、100mmのであるのであるのである。

Table		Page
4.4-4	Maximum Estimated Time for Sidelobe Rejection Test (Fixed Length) With Threshold 15 dB Above Acquisition Threshold	4-89
4.4-5	Maximum Estimated Time for Sidelobe Rejection Test (Fixed Length) With Threshold 20 dB Above Acquisition Threshold	4-91
4.5-1	Detection Performance of Desired and Interfering Signals	4-98
4.5-2	Average Acquisition Time vs. Code Length	4-98
4.6-1	Differential Delay and Doppler	4-109
4.6-2	Channel Parameter Spread Measures (RHC Polarization)	4-110
4.6-3	Channel Parameter Spread Measures (LHC Polarization)	4-111
4.6-4	$Q(\tau,\xi)$ Spreads and Tap Energy Capture (RHC)	4-112
4.6-5	$Q(\tau, \xi)$ Spreads and Tap Energy Capture (LHC)	4-116
4.6-6	Comparison Between Actual TDRSS and AEROSAT Extrapolated Spread Measures	4-124
4.6-7	Multipath Interference Parameters (IP) vs. Elevation Angle (EA)	4-129
4.6-8	Maximum Signal Level Above Threshold to Avoid Multipath Acquisition Versus Elevation Angle for Several Antenna Configurations	4-135
5.6-1	Preferred Pairs for Generation of Code Family of Long Codes	5-21
5.6-2	Preferred Pair for Generation of Code Family of Short Codes	5-23
5.6-3	Preferred Pair for Generating Code Library for Mode 2 Return Link	5-24
5.6-4	Probability Distribution of Sidelobes in Mode 2 Codes of Period 2 ¹¹ -1 · · · · · · · · · · · · · · · · · · ·	5-27
5. 7. 1	Summary of TDRSS Code Libraries	5-32

LIST OF FIGURES

Figure		Page
1.2-1	TDRSS Concept	1-6
2.1-1	Composite Signal Modulator	2-2
2.1-2	Composite Signal Structure	2-2
2.1-3	Transponder Block Diagram	2-6
2.1-4	Transponder Code Generator	2-9
2.2-1	TDRSS Frequency Plan	2-23
2.2-2	Signal Structure	2-25
2. 2-3	Frequencies Used in TDRS for Various Links	2-26
2.2-4	Simplified Block Diagram of Ground Receiver	2-28
3.1-1	Simplified Modulator and Demodulator Using Simultaneous Signal Approach	3-3
3.1-2	Basic Transponder Frequency Scheme and Signal Flow	3-4
3.1-3	Data Channel Block Diagram and Frequency Scheme	3-6
3.1-4	Range Channel Block Diagram	3 - 7
3.1-5	Tracking Channel Block Diagram	3-8
3.1-6	Signals Due to Phase Offset	3-10
3.1-7	Direct Sequence Signal with Data/Code Symmetry	3-11
3.1-8	Biphase PSK Modulator	3-14
3.1-9	Quadriphase PSK Modulator	3-14
3. 2-1	Block Diagram of Ground Receiver for TDRSS SMA, TT&C, and Test Signals	3-20
3.2-2	Block Diagram of Ground Receiver for SA Signals	3-22
3.2-3	Modified UHF Front End (One of 22)	3-23
3.2-4	Demod Matrix for Ground MA Subsystem	3-25
4.2-1	Pseudo Noise Synchronization Circuits	4-4
4.2-2	Models of Candidate Acquisition Techniques	4-6
4.2-3	Overall Synchronization Process	4-10
4.3-1	Functional Diagram of Acquisition Circuit for Fixed Length Test	4-13

List of Figures (continued)

Figure		Page
4.3-2	SNR at Envelope Detector Input vs. BT Product	4-16
4.3-3	Functional Diagram of Sequential Detection Circuit	4-18
4.3-4	Illustration of Sequential Search Strategy	4-23
4.3-5	Functional Diagram of Sequential Acquisition Detector	4-24
4.3-6	Operating Characteristic Function	4-26
4.3-7	Average Sample Number Versus Threshold Signal- to-Noise Ratio	4-29
4.3-8	State Diagram of the Dual Mode Synchronizer	4-33
4.3-9	Model of TDRSS Multiple Access Return Link	4-40
4.3-10	Model of Receiver Front End and Despreader	4-41
4.3-11	Parallel and Sequential Analysis Acquisition Circuitry for Frequency Resolution	4-52
4.3-12	Parallel Sequential Analysis Acquisition Circuitry for Frequency Resolution with Maximum Detector	4-53
4.4-1	Mean Acquisition Time vs. IF Bandwidth for MA Forward Link Short Code	4-63
4.4-2	Average Acquisition Time Versus Design Signal-to- Noise Ratio for Double Step Sequential Acquisition Analysis	4-64
4.4-3	Mean Acquisition Time vs. IF Bandwidth for Multiple Access Forward Link Long Code	4-66
4.4-4	Model of TDRSS Multiple Access Forward Link	4-68
4.4-5	Typical Auto- and Cross-Correlation Functions for the 1023 Gold Codes	4-70
4.4-6	Probability of Detection Versus SNR Relative to Design SNR for Sequential Test Strategy	4-73
4.4-7	Probability of Detection of Interfering Signal Versus Ratio of Desired Signal to Interfering Signal	4-75
4.4-8	Simplified Flow Graph of Forward Link Synchronization Algorithm	4-78
4.4-9	Estimated Mean Acquisition Time Versus Ratio of Desired Signal-to-Interfering Signal	4-79
4.4-10	Probability of Detection of Sidelobe as a Function of Signal Level Above Threshold	4-82

List of Figures (continued)

1.

Figure		Page
4.4-11	Sidelobe Rejection Algorithm	4-85
4.4-12	SNR at Envelope Detector Input vs. BT Product	4-58
4.6-1	Spread Parameter Definitions	4-104
4.6-2	Tapped Delay Line Representation of Receiver	4-108
4.6-3	Relative Mean Square Total Scatter Coefficients	4-121
4.6-4	Cumulative Multipath Energy Capture as a Function of Time	4-127
4.6-5	Cumulative Multipath Energy Capture as a Function of Time	4-128
4.6-6	Allowable Dynamic Range of Signal for Various Conditions Versus Elevation Angle	4-130
4.6-7	Estimated Fading Bandwidth as a Function of Elevation Angle	4-132
4.6-8	Required C/N ₀ in Direct Signal to Lock Onto Multipath Signal When User Gain is -9 dB to TDRS Satellite and +3 dB to Multipath	4-134
4.6-9	Sum a of Forward Link Acquisition Algorithm	4-141
5.2-1	Lineeedback Shift Register and Its Associated Polynomial	5-3
5.2-2	Description of Available Tables of Binary Polynomials	5-6
5.3-1	Performance of Preferred Pairs Compared with Worst Case Polynomial Pairs	5-8
5.4-1	Code Generator Configuration	5-13
5.4-2	Generation of Balanced Codes of Period 219-1	5-15
5.5-1	A Degradation of θ vs. % of Window to Complete Decorrelation	5-18
5.5-2	Acquisition Time vs. Clock Accuracy/Chip Rate	5-20
5.6-1	Long Code Generator Forward Link Multiple Access	5-22
5.6-2	Short Code Generator Forward Link Multiple Access	5-23
5.6-3	Generator for Mode 2 Return Link Codes	5-25
5.6-4	Probability of More Than s Sidelobes in Cross- Correlation Function of Mode 2 Return Link Codes of Periods (2 ¹¹ -1)	5-28

List of Figures (continued)

Figure		Page
5.6-5	Generation of Phase Shifts of a Maximal PN Sequence	5-29
5.6-6	Generation of Phase-Shifted Version of Maximal PN Code	5-30
5.8-1	Equivalent n-Stage Shift Registers	5-36
5.8-2	Equivalent 10-Stage Simple and Modular Shift Registers	5-37

1.0 INTRODUCTION

1.1 General

X.

×

This document is the final report on TDRSS Telecommunications System PN Code Analysis, performed by Robert Gold Associates for NASA Goddard Space Flight Center under Contract NAS 5-22546, and represents the work accomplished during the reporting period October 1975 through July 1976.

The purpose of this study was to perform parametric analysis of the pseudo noise (PN) codes required to support the TDRSS telecommunications services and to assess the impact of alternate coding techniques on the user transponder equipment, the TDRSS equipment, and all factors that contribute to the acquisition and performance of these telecommunication services. Specifically, possible alternatives to the currently proposed hybrid FH/direct sequence acquisition procedures have been considered and compared relative to acquisition time, implementation complexity, operational reliability, and cost. The hybrid FH/direct sequence technique was analyzed in detail and rejected in favor of the approach described in this report. The recommended approach minimizes acquisition time and user transponder complexity while maximizing probability of acquisition and overall link reliability.

1.1.1 Contents of Report

The remaining sections of this introduction provide a brief overall description of the TDRSS and a communication link analysis upon which the overall study conclusions were based. In Section 2, the recommended signal structure and associated codes are given. Code characteristics and taps selected to provide the desired characteristics are given. A description of the user transponder subsystem and specifications for system parameters are provided. Both the forward and

return link signals and their operation are described in this section. The emphasis of Section 2 is to provide an overview of the system, its characteristics, and operational capabilities as they are laid out in the selected design.

Subsystem design is described in Section 3. User transponder and ground receiver designs are described, and block diagrams and operational descriptions of these subsystems are given. User transponder design in postulated on the NASA Standard Transponder as a baseline. This permits a familiar transponder configuration to be considered for ready extension of expected complexity.

*

Phase-shift-keyed signals are employed throughout the system, in all modes, and in forward and return links. The signal format chosen has been based on system performance in acquisition, data trae mission, and ranging operations, and has also been oriented to minimizing overall system complexity—especially in the user transponder subsystem. Signal design and employment of dual PSK signal structures are discussed in detail in Appendix A. 2.

The recommended synchronization techniques of the user transponder for the forward link and the ground receiver of the return link are discussed and analyzed in Section 4. Emphasis is placed on the multiple access links which, for both the forward and return channels, have the lowest threshold. The code search algorithm requires the largest amount of the overall synchronization time. Hence, little emphasis was placed upon the code loops and carrier loops which are activated upon acquisition. It is estimated that the pull-in, settling and tracking times associated with these loops are less than 1 second and hence are almost insignificant contributors to the overall synchronization time.

Section 4 begins with an outline of candidate acquisition techniques.

A summary table is given of the candidate techniques which is the result of a first-level analysis documented in the Interim Report.* As a result

Interim Report, TDRSS Telecommunications System PN Code Analysis, Robert Gold Associates (under Contract NAS 5-22546), April 30, 1976.

of this preliminary study, two techniques were selected for more detailed analysis. In Section 4.3, the basic theory and associated analysis of the fixed length and sequential detection tests is presented. The functional models of the detectors, as well as the derivations of the mean acquisition times, is given. The results are extended to include a dual state detection algorithm. Several supplementary analyses are also given. These include a code doppler analysis, interfering signal analysis, and bandlimiting analysis. The subsection concludes with a discussion of multiple filter acquisition techniques for doppler resolution.

1

The application of the developed theory to the user transponder is given in Section 4.4 and to the ground receiver in Section 4.5. In each case, the discussion begins with a distribution of error and minimum threshold summary. Desired performance requirements are summarized and these parameters are used as inputs and applied to the theoretical development of Section 4.3. The overall performance is then summarized in tables and graphs.

The impact of multipath upon the synchronization parameters is summarized in Section 4.6. The basic multipath characteristics were established in a special study performed by the Boeing Company. A short summary of this study is presented herein with further details given in the Interim Report. The impact of these various parameters is discussed relative to the acquisition of the 3 Mcps PN signal on the forward link to the user receiver. The section concludes with the discussion of an algorithm developed to preclude false lock to a multipath signal.

Code generation techniques and recommended code libraries for the recommended TDRSS signal designs are presented in Section 5. Sections 5.1 through 5.4 discuss the general principles and techniques for the selection of the bandspread codes for TDRSS and Section 5.5 contains an analysis of the effect of clock error on acquisition. Specific code libraries for TDRSS are developed in Section 5.6. The Forward Link Multiple Access Library consists of 100 long codes of period 2¹⁸-1. These may be selected

from the family of Gold codes of the period which are generated as described in Section 5.6.1.1, or from the library of maximal PN codes of this period listed in Appendix G.5. The technique for the generation of the code library for the Mode 2 return link is described in Section 5.6.2 and the correlation properties of this family are analyzed and documented in Appendix A.5. The code library for the dedicated Mode 1 return link consists of maximal PN codes of period 2¹⁸-1. The codes selected are those such that phase-shifted versions in excess of 20,000 chips may be generated by adding the output of two stages of the 18-stage code generated. This code library, together with the taps which must be added and the resultant phase shift, are contained in Appendix C.5.

1.2 System Design Considerations

TDRSS is a satellite communication signal relay system intended to provide almost complete earth coverage to users wishing to transmit or receive messages to and from earth stations located within the United States. The system is illustrated in figure 1.2-1.

"The Tracking and Data Relay Satellite System (TDRSS) will consist of two geosynchronous relay satellites, 130 degrees apart in longitude, and a ground terminal located in the continental United States. Additionally, the system will include two spare satellites; one in orbit, and one in configuration for a rapid replacement launch. The purpose of the TDRSS is to provide telecommunications services which will relay communications signals between low earth-orbiting user spacecraft and the user control and/or data processing facilities. A real-time, bent-pipe concept is utilized in the operation of the TDRSS telecommunications services. The system will be capable of transmitting data to, receiving data from, or tracking user spacecraft over at least 85 percent of the user orbit."*

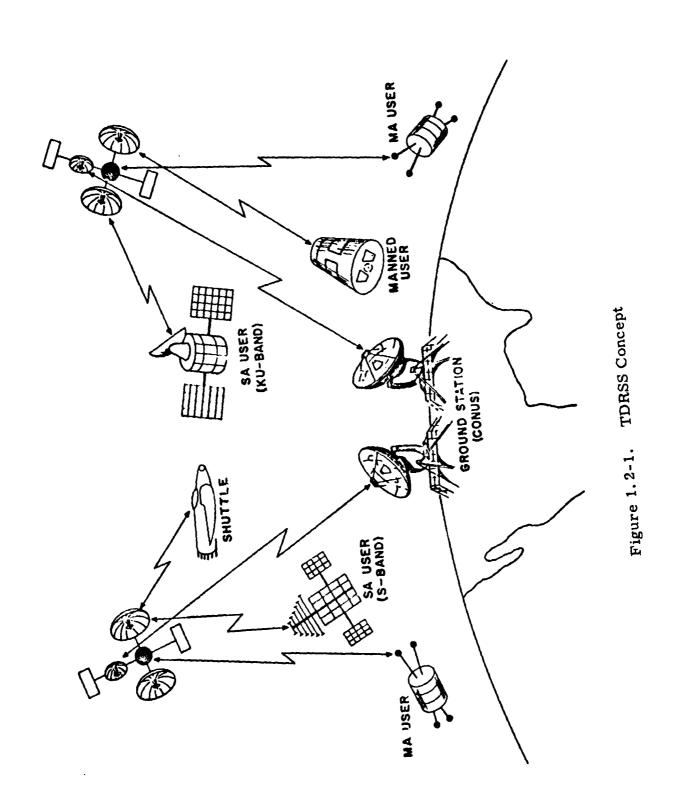
Services provided by TDRSS are:

Multiple Access - "The multiple access (MA) communication service system is designed to provide simultaneous real-time and dedicated return link service to low earth-orbiting user spacecraft with real-time data rates to ____ bps. Forward and return link service will be provided to all system users."*

Single Access - "The single access (SA) communication service system is designed to provide a high data rate return link to users with real-time, playback, or science data requirements. The system will be utilized on a priority scheduled basis, and will not normally be used for dedicated support to any mission (with the exception of Space Shuttle)."*

Cross-support - "Any mission which is compatible with the MA system can receive forward or return link support from either the MA or SSA systems."*

^{*}TDRSS User's Guide, May 1975.



ĺ.

].

Tracking - All service systems can provide range rate tracking data for the users supported. Tracking accuracy will be comparable to that currently available from the ground-based STDN (Spacecraft Tracking and Data Network).

Operating Frequencies

C.

ť.

 \mathbf{C}

TDRS to User

SMA 2106.4 MHz

SSA 2.2 to 2.3 GHz

KSA 15.0086 GHz

User to TDRS

SMA 2287.5 MHz

SSA 2025 to 2120 MHz

KSA 13.775 GHz

The various subsystems and their requirements are described in the sections of this report that follow. Each subsystem is considered, together with its signals, and its functions in handling and/or generating those signals.

1.3 Link Analysis

1.3.1 Introduction

One of the objectives of this investigation—as to determine, based on the link an lyses, the minimum received signal level by the user receiver for each of the TDRSS forward links and, similarly, for the ground receiver for each of the return links. One of the primary assumptions was the user antenna gain. Values assumed are those given in the performance specification for the simulation service.* For both the MA and SSA service, an antenna gain of -9 dB was used. For the KSA service, +17 dB gain was assumed.

1.3.2 Discussion of Results

Forward Links. A summary of the forward link analyses is given in tables 1.3-1 through 1.3-3. Considering first the MA forward link, we find the minimum received signal level is approximately -137 dBm. This is the required receiver sensitivity. Continuing on through the link analysis of table 1.3-1, we find that with no design margin the link is just on the edge of being able to support a data rate of 100 bps, the desired objective for the minimum data rate. By increasing the receiver antenna gain, the link is capable of supporting a higher data rate.

The SSA forward link does not require the receiver sensitivity of the MA forward link. It has a minimum received signal level as shown in table 1.3-2 of -127.8 dBm. This link is capable of supporting a data rate in excess of 400 bps with a 3 dB design margin. Compared with the multiple access system, the S-band single access system is characterized by higher S/N_0 values due to the gain of a dish antenna on the TDRS. Thus, synchronization acquisition on the forward link is less of a problem than with the multiple access system.

^{*}Performance Specification for Telecommunications Service Via the Tracking and Data Relay Satellite System, Goddard Space Flight Center, S-805-1, June 1975, p. 25.

Table 1.3-1. Link Analysis for MA Forward Link, S-Band

 $f_c = 2106.4 \text{ MHz}$

TDRS Antenna Gain (dB)	23.0	
TDRS Transmit Power (dBw)	13.0	
RF Transmit Loss (dB)	-1.0	
Transmitted EIRP (dBw)	35.0	
TDRS Transponder Loss (dB)	-1.0	
Antenna Pointing Loss (dB)	0	
Signal EIRP (dBw)	34.0	
Space Loss (dB)	-191.6	
User Antenna Gain (dB)	-9.0	
Polarization Loss (dB)	-0.5	
P _s - Signal Power Out of User Antenna (dBw)	-167.1	
Ps - Signal Power Out of User Antenna (dBm)	-137.1	
•		
T _s (Antenna Output) (824 ⁰ K) (dB)	29.2	
KT _s (dBw/Hz)	-199.4	
Ps/KTs (dB-Hz)	32.3	
- 5		
Required $E_b/N_0 = 9.9 \text{ dB} @ 10^{-5} \text{ BER}$	-9.9	
Demodulation Loss (dB)	-1.5	
PN Loss (dB)	-1.0	
Achievable Data Rate (dB), No Margin	19.9	implies 98 bps
Achievable Data Rate (dB), 3 dB Margin	16.9	implies 49 bps

Table 1.3-2. Link Analysis for SSA Forward Link, S-Band

f_c = 2106.4 MHz

TDRS Antenna Gain (dB)	35.4	
TDRS Transmit Power (dBw)	11.6	
RF Transmit Loss (dB)	-2.0	
Transmitted EIRP (dBw)	45.0	
TDRS Transponder Loss (dB)	-1.0	
Antenna Pointing Loss (dB)	-0.5	
Signal EIRP (dBw)	43.5	
Space Loss (dB)	-191.6	
User Antenna Gain (dB)	-9.0	
Polarization Loss (dB)	-0.5	
Ps - Signal Power Out of User Antenna (dBw)	-157.8	•
Ps - Signal Power Out of User Antenna (dBm)	-127.8	
T _s (Antenna Output) (824 ⁰ K) (dB)	29. 2	
KT _s (dBw/Hz)	-199.4	
P_s/KT_s (dB-Hz)	41.8	
Required $E_b/N_0 = 9.9 \text{ dB} @ 10^{-5} \text{ BER}$	-9.9	
Demodulation Loss (dB)	-1.5	
PN Loss (dB)	-1.0	
System Margin (dB)	-3.0	
Achievable Data Rate (dB)	26.4	implies 436 bps

Table 1.3-3. Link Analysis for KSA Forward Link

 $f_c = 13.775 \text{ GHz}$

TDRS Antenna Gain (dB)	52.0	
TDRS Transmit Power (dBw)	-3.0	
RF Transmit Loss (dB)	-2.0	
Transmitted EIRP (dBw)	47.0	
TDRS Transponder Loss (dB)	-1.0	
Antenna Pointing Loss (dB)	-0.5	
Signal EIRP (dBw)	45.5	
Space Loss (dB)	-208.6	
User Antenna Gain (dB)	17.0	
Polarization Loss (dB)	-0.5	
P _s - Signal Power Out of User Antenna (dBw)	-146.6	•
P _s - Signal Power Out of User Antenna (dBm)	-116.6	
T _s (Antenna Output) (893 ^C K) (dB)	29.5	
KT _s (dBw/Hz)	-199.1	
P_s/KT_s (dB-Hz)	52.5	
Required $E_b/N_0 = 9.9 \text{ dB } @ 10^{-5} \text{ BER}$	-9.9	
Demodulation Loss (dB)	-1.5	
PN Loss (dB)	-1.0	
System Margin (dB)	-3.0	
Achievable Data Rate (dB)	37.1	implies 5128 bps

The link analysis for the KSA forward link is given in table 1.3-3. The received signal power is the greatest of the three links, -116.6 dBm. With a 3 dB design margin, the link is capable of sustaining a data rate in excess of 5 kbps.

One area of investigation which was not considered in the link analyses given in the above reports is that of ionospheric scintillation. Recent investigations have found that it does have an effect on the signal in the 2-4 GHz region. This effect occurs only if the signal penetrates the ionosphere. If the signal does penetrate the ionosphere, peak-to-peak amplitude fluctuations of 2 to 5 dB, as well as phase perturbations, can occur at certain times during a 24-hour time period. The fluctuations will be the greatest if the propagated signal comes within the influence of the earth's magnetic equator or the aurora zones. The intensity of the scintillation effects is also correlated with the sunspot activity. To obtain a point of reference, an analysis was made to determine the range from the TDRS satellite to a user in a 2000 km orbit at which the signal would penetrate the edge of the ionosphere. Referring to Figure C-7 on page C-16 of the User's Guide,* we see the geometry depicting the range selected for the link calculations. At this range, the closest distance to the earth's surface is 1829 km. For the satellite to be within 500 km of the earth's surface, which would be the outer edge of the ionosphere, the range to the user satellite is 46,550 km. It is at this range and beyond for the spatial relationships given in Figure C-7 that the scintillation effects can be observed.

Return Links. A summary of the multiple access, single access and Ku-band single access return link analyses is given in table 1.3-4. These results are taken from the User's Guide and are included here for completeness.

1

^{*}Tracking and Data Relay Satellite System (TDRSS) User's Guide, Goddard Space Flight Center, STDN No. 101.2, Rev. 2, May 1975, pp. C5-C16.

Table 1.3-4. Return Link Analysis

Î.

S-Band: $f_c = 2287.5 \text{ MHz}$

Ku-Band: $f_c = 15 \text{ GHz}$

()

	S-Band		Ku-Band
	Multiple		
Link Parameters	Access	Single Access	Single Access
BER	10 ⁻⁵	10 ⁻⁵	10 ⁻⁵
User EIRP (dBw)	EIRP	EIRP	EIRP
Space Loss (dB)	-192.2	-192.2	-209. 2
Polarization Loss (dB)	-1.0	-0.5	-0.5
Pointing Loss (dB)		-0.5	-0.5
TDRS Antenna Gain (dB)	28.0	36.0	52. 6
P _s at Output of Antenna (dBw)	~165.2 + EIRP	-157.2 + EIRP	-157.6 + EIRP
T _s (Antenna Output Terminals) (^O K)	824	586	893
T. (Due to Other User Interference)(OK)	255		
$K (T_s + T_i) (dBw/Hz)$	-198.3	-200.9	-199.1
$P_s/K(T_s+T_i)$ (dB-Hz)	33.1 + EIRP	43.7 + EIRP	41.5 + EIRP
Transponder Loss (dB)	-2.0	-2.0	-2.0
Demodulation Loss (dB)	-1.5	-1.5	-1.5
PN Loss (dB)	-1.0		
Antenna Beam Forming Loss (dB)	-0.5		
System Margin (dB)	-3.0	-3.0	-3.0
Required ${ m E_b/N_0}$ (dB)	-9.9	-9.9	-9.9
Achievable Data Rate (dB)	15.2 + EIRP	27.3 + EIRP	25.1 + EIRP
FEC Gain (dB) R = 1/2, K = 7	5. 2	5. 2	5. 2
Achievable Data Rate (dB)	20.4 + EIRP	32.5 + EIRP	30.3 + EIRP

Data rates on the return link multiple access spread spectrum signal from a user can range up to 50 kbps and rate 1/2 error correction establishes the maximum symbol rate at 100 kbps. Return link performance for a given multiple access user is affected by interference from other users within the receive beam. An analysis of this degradation is given in Section 4.3.5.

The S-band single access return link may have telemetry data rates in the range from 100 bps up to 6.3 Mbps. As with the multiple access return link, the rates are a function of the operational mode, the EIRP, whether the data is biphase formatted or convolutionally coded, and whether spectrum spreading is utilized.

8

X

The Ku-band single access return link is intended to handle telemetry data rates from 1 kbps to 300 Mbps. The data rates are functions of the same factors as given above for the single access return link.

2.0 SUMMARY OF RESULTS

7. .

This report section describes the results of studies carried out by Robert Gold Associates. Signal design descriptions are given for both forward and return links, together with recommended system and subsystem parameters.

2.1 Forward Link Multiple Access

2.1.1 Recommended Parameters

Signal Design

7

S

ľ.

The recommended signal design is a dual format, wherein a pair of PSK (phase-shift-keyed) signals are sent on quadrature-related versions of the same carrier signal. This is illustrated by the modulator of Figure 2.1-1. (It is noted that the modulator shown is different from a standard quadriphase PSK modulator only in that one of the two biphase PSK signals generated internally to the modulator is held to a level 10 dB below the other.) The signal employed can be considered to be a composite of two signals, one of which has 10 dB less power than the other, whose carriers happen to be at the same frequency and whose carrier phases are in quadrature. The quadrature phase relationship is assured by actually employing only one carrier signal source and routing properly phase-shifted versions of this carrier to the right place. Frequency coherence is assured by this employment of phase-separated versions of the same carrier reference for the two signals.

The forward link multiple access signal is an unbalanced quadriphase pair of signals, as shown in Figure 2.1-2. This signal is made up of a pair of bi-phase signals related in such a way that their combined structure has a constant envelope. That is, in the steady state, the signal always takes one of the four phases as shown in Figure 2.1-2, and the radius vector has the same value in all four phases as long as the two bi-phase signals are maintained in phase quadrature. Constant envelope

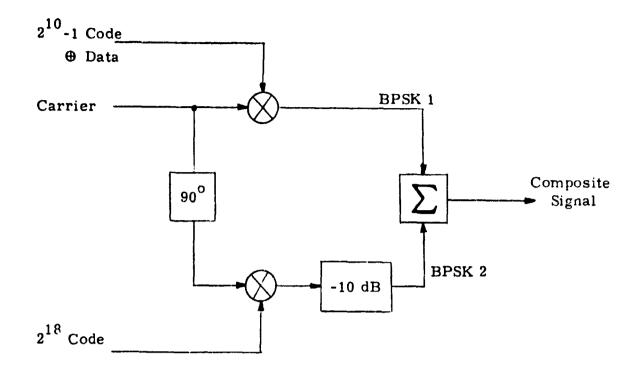


Figure 2.1-1. Composite Signal Modulator

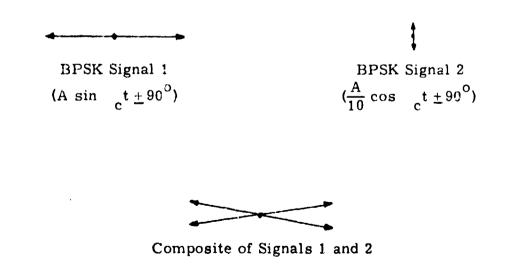


Figure 2.1-2. Composite Signal Structure

• 1

1;

ţ.

ŗ.

•

•

n sami

| ----

Chinesia - Carlos santi - (

power is important in systems employing either traveling wave tube or solid-state power amplifiers, as these exhibit AM-to-PM conversion in the range of 6 to 10 degrees for each 1 dB signal amplitude change. Thus, incidental phase modulation may be caused by unintended amplitude modulation, and this phase modulation can approach the level of the desired signal, causing serious loss or degradation of the intended signal.

A dual bi-phase signal format has been chosen in preference to dual quadriphase because of the relative simplicity of the bi-phase structure from the hardware point of view. In addition, it is necessary to limit the allowable plase states assumed by the smaller signal in a dual-QPSK modulator, to avoid incidental AM modulation.

Direct sequence spread spectrum modulation is employed in the forward link for several reasons:

- The spread spectrum modulated signal has relatively low power density, which is necessary to meet system requirements for signal flux density at the earth's surface* due to TDRSS transmissions.
- 2. The coded modulation provides for code division multiple access operation.
- 3. The system has reduced sensitivity to interference, as well as furnishing low interference to other link users.
 - 4. Good range resolution is facilitated by the coded modulation.

Demodulation of the dual signals must be accomplished by synchronizing the receiver to both transmitted code sequences. For all practical

Ku-band

S-band

⁻¹⁵⁴ dBw/m² in 4 kHz for 0° to 5° arrival angle. -154 + (0-5)/2 dB BW/m² in 4 kHz for 5° to 25°

 $^{-144 \}text{ dBw/m}^2$ in 4 kHz for 25° to 90°

 $^{-152 \}text{ dBw/m}^2 \text{ in 4 kHz, 0}^{\circ} \text{ to 5}^{\circ}$

^{-152 + (0-5)/2} dBw/m² in 4 kHz, 5° to 25°

 $^{-142 \}text{ dBw/m}^2 \text{ in 4 kHz. } 25^{\circ} \text{ to } 90^{\circ}.$

purposes, the signal received is treated as if it were two unrelated signals. Therefore, the optimum receiver is actually a pair of bi-phase PSK receivers rather than a single quadriphase receiver for two unequal signals; even though the two signals are in phase quadrature just as are other quadriphase PSK signals.

Ĺį

As the coded modulation is a key to range resolution, multiple access, interference rejection, and low spectrum density, the codes employed must be plentiful, readily generated, and have good correlation properties. The larger of the dual signal pair is modulated by a 3.077799 Mbps, 1023-bit code sequence of the "Gold" type. This signal is employed for initial acquisition and for data transmission. The second, smaller signal is modulated by a longer code (2¹⁸-25' bits) at the same bit rate, and is employed for range measurement.

The code sequences employed in the forward link (Codes 1 and 2 of figure 2.1-1) are of lengths 1023 bits and (1023·256) bits, at a bit rate of 3.077799 Mbps. Gold sequences will be employed for the 1023-bit codes to insure that a large family of usable codes is available. The long code is specifically chosen to have a length which is an integral multiple of the shorter code length, which aids in the long code synchronization process.

In the return link, the f_1 signal used as a reference for carrier frequency generation may be coherent or noncoherent with the f_1 signal used in the forward link. This depends on the mode in which the system is operating (see table 2.1-1). In all cases, code rates are related to carrier frequency in the following ratios:

Operation	Ratio	Bit Rate
SMA, SSA	$\frac{31 \text{ fc (fwd)}}{221 \times 96}$	3.077799479 Mbps
KSA	31 fc (fwd) 1469 x 96	3. 02803069 Mbps

The section that follows lists the specific codes that have been selected for use in this program.

Table 2.1-1. PN Code Lengths

Mode	Q Channel Code	I Channel Code	$\frac{f_1/f_2}{}$
1	1023 bits	$(1023 \cdot 256)$ bits	Coherent
2	2047 bits	2047 bits	Nonconerent
3	None	$(1023 \cdot 256)$ bits	Coherent

Codes recommended are listed in the following paragraph.

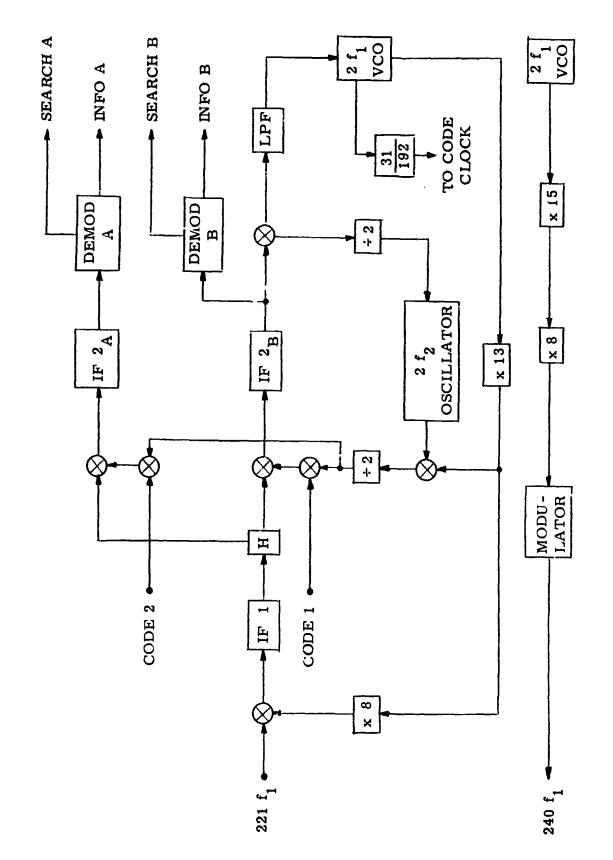
2.1.2 User Transponder Description

C

This section describes a user transponder design used to implement tradeoffs in signal structure and signal selection. Further information and details may be found in Robert Gold Associates Interim Report for Contract NAS 5-22546, TDRSS PN Code Analysis, April 30, 1976.

2.1.2.1 Figure 2.1.3 shows the simplified block diagram of a transponder design based on the NASA Standard Transponder configuration. The necessary spread spectrum blocks have been added to the standard transponder to provide the desired signal characteristics (i.e., wideband, low-powerdensity signals in the modulated signal band).

A signal at 2106. 40625 MHz (221 f_1) is received and mixed with a local oscillator at 1982. 5 MHz (208 f_1) to produce a 193. 90625 MHz IF signal. At this IF frequency, the signal is split and applied to two second mixers along with two local code-modulated reference signals. One of these local reference codes (No. 1) is the 2^{10} -1 bit synchronization and data sequence, and the other (No. 2) is the 2^{18} -256 bit ranging sequence. Both local reference signals are centered at 136.15625 MHz, so that when local codes are synchronous with either received signal, the corresponding IF2 output signal is 12.25 MHz, output to either IF2 $_{\rm A}$ or IF2 $_{\rm B}$ depending on which code is synchronous (either one or both may be synchronized at any given time).



8

t (

Figure 2.1-3. Transponder Block Diagram

į,

A synchronized signal output in IF2_B is from the 1023 bit code channel, which includes forward link data in its modulation. The synchronized signal output then is a carrier (at 12.25 MHz) that is PSK modulated by the desired data. This signal is then demodulated and the data employed as required.

The IF2_A signal is an unmodulated carrier employed in ranging. Since this signal is unmodulated, the design of Demod A is greatly simplified by a carrier detector. Further, since the IF2_B signal will be acquired prior to the IF2_A signal, coherent carrier detection is facilitated, as a carrier reference is available from Demod B. If desired, low rate data such as commands might be sent as baseband modulation on the signal in IF2_A. Of course, this would impact the demodulator design since it would then be required to accept data, and this would in turn bring about the need for a somewhat wider bandwidth (at least as great as the data rate).

Either coherent or noncoherent signal transmission at $240\,\mathrm{f}_1$ is facilitated to allow for turnaround ranging or any other operation that might require a return link signal that is coherent with the forward link signal.

Two separate oscillators are provided as $2f_1$ sources. One, a VCO, is phase locked to the forward link signal, which provides a coherent $2f_1$ source for generating (after multiplication by 120) the return link carrier. In the noncoherent mode, a separate $2f_1$ oscillator is used to generate the return link carrier. In some instances, the noncoherent mode is necessary to prevent retransmission of a return link signal that is perturbed by forward link carrier phase noise.

Code clock is also derived by operation on the $2f_1$ VCO or $2f_1$ oscillator. Again, the decision as to which is used depends on whether coherent or noncoherent turnaround must be employed. The clock rate is $31/96 \ f_1$, or 3.077799479 Mbps when the return link carrier frequency is 2287.5 MHz. Code rate does vary as carrier frequency is changed, but within the range of carrier frequencies expected, the code rate will be close to 3.0 Mbps.

Basic code generator design is illustrated in figure 2.1-4. A number of codes must be generated simultaneously for full forward and return link operational capability. The use of a number of codes and availability of a large library of well-defined and carefully selected codes is a feature of the system design and a specific goal of this study program.

The most prominent features of the user transponder design selected are given in table 2.1-2.

l

2.1.2.2 Estimates of the number of components required to implement the portions of the user transponder that are beyond the subsystem included in present standard transponder design (i. e., code generators, code modulators, and other circuitry associated specifically with spread spectrum modulation and demodulation) are given in table 2.1-3. Also included in this table is an estimate of the additional power required to operate these additional components. Overall power estimated for a transponder is given in tables 2.1-4 and 2.1-5.

Table 2.1-6 shows overall weight estimated for a spread spectrum user transponder.

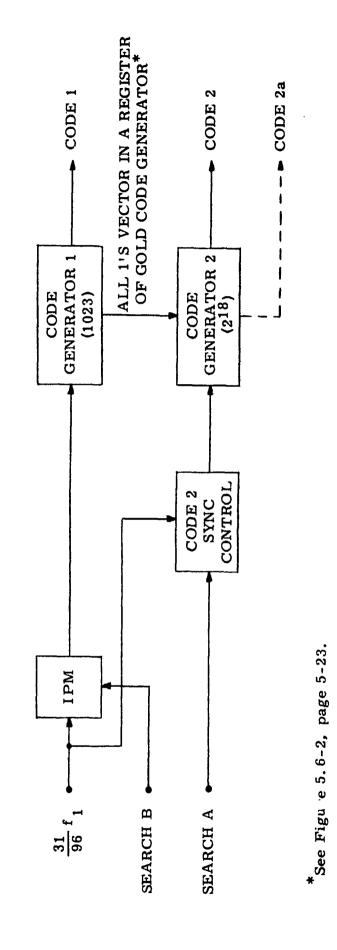
It is apparent from considerations of available alternatives that the selected direct sequence approach meets TDRSS requirements and is the best available method for doing so.

Further descriptions of the user transponder and the signal structure employed in TDRSS may be found in section 3.1 of this report.

Table 2.1-7 lists the overall characteristics of the recommended subsystem.

2.1.3 System Performance

The results obtained for the S-band multiple access and single access forward link synchronization study are summarized below. We begin by summarizing the performance objectives and the system constraints.



1.

1

a []

Figure 2.1-4. Transponder Code Generator

Table 2.1-2. User Transponder Design

Synchronization Technique

1-23 bit sequence

Sequential acquisition with doppler

resolution filters

Data Transmission

By sequence inversion modulation

of the 1023 bit sequence

Ranging Code

2¹⁸-256 bit sequence ranging code acquisition by derivation from short

code timing. Used for ranging only

Signal Format

Unbalanced QPSK, synchronization/ data transmission code on (90,270) degree carrier, range co e on

(0,180) degree carrier. Range carrier 10 dB below data carrier

Code Rate

3.07799 Mbps

Average Synchronization Time

Sequential Search

14.2 seconds

Short code Long code

1.5 seconds

User can synchronize any time, no specific synchronization mode

Additional Hardware Required (transponder)

75 components

Power Estimated (transponder)

7.4 watts MIC constuction

(not including P.A.)

12.0 watts

Hybrid construction

(not including P.A.)

Development Risks

No new transponder circuitry needed.
Code generators, frequency synthesizers, modulators, and demodulators use proven circuits and

techniques

Table 2.1-3. Component Estimate

	Circuits		Power
Transmitter			
Coders	8	33 f-f	0.33 w
	2	8 mod 2	0.08
	3	3 nor	0.03
Modulator	12	2 B.M.	0
	1	1 90 ⁰ hybrid	0
	1	1 Σ	0
	1	1 10-dB atten.	0
	28 components		0.44 w
Receiver			
	36	6 B.M.	0
	2	2 Σ	0
	6	6 IF I.C.	0.6 w
	30	30 resistors	0
	25	25 capacitors	0
	2	2 BPF	0
	12	45 f-f	0.45
	1	1 comparator	0.1
	1	1 diff. amp.	0.1
	1	1 4 Q mult.	0.1
	2	7 gates	0.07
	2	8 mod 2	0.08
	2	2 VCO I.C.	0.1
	122 components		1.6 w

Assumes: 10 mw/digital I.C.; 100 mw/analog I.C.

28 + 122 = 150 total parts

0.44 + 1.6 = 2.04 w total

Table 2.1-4. Total Power Estimate

04	w	
. 0	w	
. 5	w	
04	w	total
54	w	total
o PA	A)	
(o P	o PA)

Table 2.1-5. Power Amplifier Estimate

Power Amplifier (20 watts)

TWT	6.5 lb	80-133 w prime power
Trapatt	<4 lb	50-80 w prime power
Transistor	< 4 lb	50-67 w prime power

Table 2.1-6. Total Weight

33	1.5 10
Hybrid IF/RF	2.25 lb
MIC IF/RF	1.6 lb
Hybrid	3. 85 lb total
MIC	3.2 lb total

Table 2.1-7. Transponder Specifications

RECEIVER CHANNEL

Center Frequency

2106, 40625 MHz

Noise Figure

2.5 dB max

Bandwidth (3 dB)

5 MHz min (at 2nd IF)

VSWR

1. 1:1 to \pm 2. 25 MHz

Phase Response

Linear to within ±5°

Flat to within 1/2 dB

+ 1.50 MHz

+ 1.50 MHz

Amplitude Response

Dynamic Signal Range

40 dB

Maximum Signal and Noise

-130 dBW

Minimum Signal

-180 dBW

SYNCHRONIZATION PREAMBLE

Code:

Type

Pseudorandom, Gold-type

Code Generation

Linear

Code Length

1023 bits

Code Loop:

Dither

 $\tau_{\rm d}$ = 0.5 chip (if τ dither used), delay lock preferred

Order

1st

Bandwidth (B,)

0.1 Hz

Dynamics Aiding

From carrier loop

Acquisition:

Search Steps

1/2 chip

Average Search Rate

75 chips/second

Signal Detector

Sequential detector

Detector Bandwidth

+ 3 kHz

Frequency Uncertainty

700 Hz nominal, 3000 Hz maximum

Time Uncertainty

1023 PN chips maximum

Table 2.1-7. (continued)

PN Losses:

Bandwidth

Negligible

Channel Distortion

0.5 dB

Imperfect Tracking

0.3 dB

CARRIER ACQUISITION AND TRACKING

Type of Loop

Costas/PLL or Squaring

Loop Orde"

2nd

Loop Bandwidth (B,)

32 Hz

Damping Factor

0.707

Frequency Offset (Max)

Acquisition

+ 3 kHz

Tracking

+ 60 kHz

Incidental FM

6° RMS in 10 Hz with good S/N,

maximum

Carrier Tracking Losses:

Incidental FM

0.2 dB

Nonlinearities

0.5 dB at threshold

AGC Noise

0.3 dB at threshold

COMMAND DATA DEMODULATION

Demodulator

Costas Loop

Fixed Data Rate

125, 1000 bps

Data Processing

Integrate and dump

Telemetry Data:

Rate

1 kbs - 50 kbs

Clock

Asynchronous, user supplied

External Interface

TTL compatible

EDAC Encoding

Type

Convolutional

Constraint Length

7

Rate

1/2

Transmission Encoding

Type

Differential

Table 2.1-7. (continued)

User Oscillator Phase Noise ≤ 3° RMS; BW - 6 Hz - 100 kHz

Modulator/Demodulator Phase ≤ 4⁰

Imbalance

Modulator/Demodulator Amplitude ≤ 0.5 dB

Imbalance

Data Asymmetry ≤ 1 percent

Data Skew ≤ 0.1 bit time

Data Decoding Differential

Data Clock Derived from PN code

Data Interface TTL

Implementation Losses:

Carrier Reference at 1 dB at 100 bps

Threshold

Nonlinearity 0.3 dB

Bandlimiting 0.2 dB

TRANSMIT CHANNEL

Transmitter:

Type Solid State or TWT

Center Frequency 2287.5 MHz

Bandwidth (3 dB) 6 MHz minimum

Amplitude Response Flat to within 1/2 dB bandwidth

Phase Response Linear to within + 5°

Modulator:

Modulation Unbalanced QPSK

Code Families Gold code pairs

PN Chip Rate 3.077799 MHz

Code Lengths

Forward Link 218-256, 1023

Return Link 218-256, 1023

Bandwidth 3 MHz

Filter Type Butterworth, 4-pole

Table 2.1-7. (continued)

Carrier Suppression

30 dB or greater

Spurious Responses

20 dB down outside of + 3 MHz

AM/PM Conversion

 $< 10^{\circ}/dB$

Cross-Modulation

≥ 10 dB below signal

Code Epoch

82 msec, 322 µsec

Local Reference:

Bandwidth (3 dB)

3 MHz

Phase Response

Linear to within + 5° over + 1.5 MHz

Amplitude Response

Flat to within 1/2 dB over + 1.5 MHz

Spurious Responses

20 dB down outside + 3 MHz

Acquisition:

Signal Bandwidth

3.077 MHz x 2 (nuli-null)

Signal Detector

Sequential detector

Detection Bandwidth

+ 1500 Hz

Average Search Rate

136 chips/second

Frequency Uncertainty

700 Hz nominal, 3000 Hz maximum

PN DEMODULATION

PN Code:

Type

SQPN (Staggered Quadriphase Pseudonoise)

Code Family

Maximal code pairs truncated by

255 bits

Code Period

2¹⁸ - 256, 1023

PN Chip Rate

3.077 MHz

Repetition Interval

82.432 ms, 322 µsec

Local Reference:

Bandwidth (3 dB)

3 MHz

Phase Response

Linear to within +5° over +1.5 MHz

Amplitude Response

Flat to within 1/2 dB over + 1.5 MHz

Carrier Suppression

45 dB or greater

);

\$

Performance Objectives

Short Code - 1023 chips

Mean Acquisition Time

20 seconds (including long code)

Probability of Detection

0.9

Probability of False Alarm

10⁻⁶

Long Code - 2¹⁸-256 chips

Mean Acquisition Time

Included in 20 seconds

Probability of Detection

0.9

Probability of False Alarm

10⁻⁶

Multipath rejection algorithm required

System Constraints

Multiple Access Mode:

 $C/N_0 = 32.3 dB-Hz$

Data Rate = 125 bps

Single Access Mode:

 $C/N_0 = 41.8 dB-Hz$

Data Rate = 125 bps

Total Doppler and

Frequency Uncertainty:

3000 Hz

The recommended synchronization approach for the short code is to use a noncoherent sequential search strategy. The theory and functional description of this search strategy is given in section 4.3.2. The analysis of the technique as applied to the forward link is given in section 4.4.

Both the noncoherent fixed length strategies and sequential test strategies were considered in the study. In order to meet the performance objectives, multiple IF contiguous doppler resolving filters are required. The technique analyzed was a completely parallel processing approach. Techniques for simplifying the hardware, such as the implementation of a maximum detector, are possible. However, with the use of the sequential search strategy, only two doppler cells are required. The same performance could be obtained by using two despreaders with

each local reference stepping through a different set of cells simultaneously. In this case, only one IF filter covering the total uncertainty band would be associated with each despreader.

The performance of the S-band multiple access and single access forward links is summarized in tables 2.1-8 and 2.1-9, respectively. The fixed length test analysis was not performed for the single access link. However, rough estimates indicate that the average acquisition time exceeds the sequential test acquisition time by an order of magnitude.

Either the coherent or noncoherent sequential test strategy can be used for the long code acquisition of the multiple access forward link. Code tracking and carrier lock are obtained at the conclusion of the short code acquisition. Therefore, two possibilities exist. The first is that the long code can be coherently acquired. The second is that the local reference can be doppler corrected permitting the use of a narrowband IF filter which precedes a noncoherent detector. Clearly, the performance is a function of how narrow an IF filter can be utilized. The average acquisition times for a range of IF bandwidth filter cases for the two approaches suggested above are summarized in Table 2.1-10.

The third aspect of the performance analysis was to assess the nature of the multipath between a low orbiting user satellite and the synchronous TDRS satellite (cf. Section 4.6.7). The primary problem is one of false locking to a multipath component. The differential doppler is small enough that most of the multipath energy will fall within the receiver bandwidth. The basic nature of the multipath signal is diffuse rather than specular. The multipath energy tends to be smeared over several tap positions. The degree of smearing is a function of the elevation angle and the antenna polarizations relative to the multipath signal.

3

\$

Several techniques for avoiding false lock to a multipath signal are suggested. These techniques take advantage of the basic properties of the multipath signal at the output of the despreader. The one approach takes advantage of the diffuse nature of the multipath energy in frequency, thus making it very difficult to falsely code lock and carrier lock to the multipath

Comparative Summary of Average Acquisition Times for the MA Forward Link Short PN Code Table 2. 1-8.

をおからいませんというできないというからないできない。 それらいからしていているから

•

3 1..

Mimbon	j.		Noncoherent Test S	Noncoherent Fixed Length Test Strategy	Noncohere Test	Noncoherent Sequential Test Strategy
of Doppler Cells	Bandwidth per Cell (Hz)	SNR in Frequency Cell (dB)	Tacq (sec)	Average Search Rate (chips/sec)	Tacq (sec)	Average Search Rate (chips/sec)
н	0009	-9.3	42.9	23.8	28.6	35.8
7	3000	-6.3	27.5	37.2	14.2	72
ß	1200	-2.3	16.5	62.0	5.7	179
10	009	0.7	13.7	74.7	2.9	353

l

Table 2.1-9. Summary of Average Acquisition Times for the SA Forward Link Short PN Code

Nimp	Ē		Noncoherer Test S	Noncoherent Sequential Test Strategy
of Doppler Cells	Bandwidth per Cell (Hz)	SNR in Frequency Cel! (dB)	$\overline{\Gamma}_{ m acq}$ (sec)	Average Search Rate (chips/sec)
1 2	3000	0.2 3.2	0.8 0.8	1279 1279

1

Comparative Summary of Mean Acquisition Times for Multiple Access Forward Link Long PN Code Table 2.1-10.

The table of the state of the s

;

		Sequential Col	Sequential Test Strategy* Coherent	Sequential Test S Noncoherent	Sequential Test Strategy Noncoherent
IF Bandwidth (Hz)	SNR in IF Bandwidth (dB)	Tacq (sec)	Mean Search Rate (chips/sec)	T acq (sec)	Mean Search Rate (chips/sec)
0009	-17.2	1.4	182.9	276	0.93
3000	-14.2	1.35	189.6	138	1.9
1200	-10.2	1.3	196.9	55	4.7
009	-7.2	1.3	196.9	27	9.5

* Assumes local reference stepped in 1/2 chip increments.

THE PERSON OF TH

signal. The other approach makes use of the time spread of the multipath signal. The energy is almost flat across several adjacent time cells. This is in contrast to the direct signal whose cross-correlation function peaks at its in-phase position, and is almost negligible at adjacent cell positions. The sequence of steps in the acquisition process for both the short and long codes is given below:

Step 1	Short Code Acquisition
Step 2	Short Code Verification
Step 3	PN Code Tracking with Multiple Test
Step 4	Carrier Lock Search with Coherent Amplitude Detection Multipath Test
Step 5	Long Code Acquisition
Step 6	Long Code Verification
Step 7	Direct Signal Verification

2.2 Return Link

The return link consists of a path from the user transponder, through TDRS as a relay, and to the ground receiver. Signals employed in the return link are similar to those employed in the forward link, but differ somewhat in their particulars. The paragraphs that follow delineate these differences.

Figure 2.2-1 shows both forward and return links and the frequencies employed in those links. (Figure 2.2-1 is from TDRSS User's Guide, dated May 1975.)

2.2.1 System Parameters

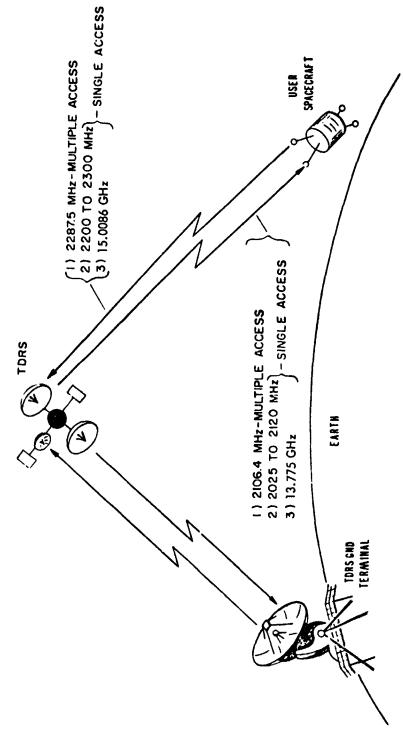
Ü

E)

The user transponder portion of the return link consists of the 2f₁ source, multipliers to develop the 2287.5 MHz transmitted signal center frequency, and a modulator for impressing the data transmitted on the signal carrier. It is of some interest to note that the PSK modulation employed in TDRSS cannot be followed by multiplication as in the NASA Standard Transponder, since multiplication of such PSK signals removes the modulation and produces an unmodulated carrier signal at the desired output frequency. For this reason, the return link blocks shown in figure 2.1-3 are reversed in order from those usually seen in the Standard Transponder.

Three signalling modes are provided in the return link. Mode 1, which employs coherent turn-around of the forward link carrier signal, uses a 1023 bit synchronization and data transmission coded signal, together with a reduced-power 2¹⁸-256 bit range code modulated signal (actually the turn-around ranging signal). This signal is, of course, identical to the structure of the forward link signal, with the exception of the use of different code sequences where required for multiple access operations.

Figure 2.2-1. TDRSS Frequency Plan



 \mathbf{J} :

ſ

L _.

L l

ŧ

Noncoherent turnaround is employed in Mode 2. That is, the independent $2f_1$ oscillator shown in figure 2.1-3 is used to generate the carrier signal. Also in Mode 2, the code length employed is 2^{11} -1 (2047 bits).

Ĭ ...

Mode 3 employs a coherent carrier, with a 2¹⁸-256 bit coded ranging signal being present, but the primary signal (transmitted instead of the Mode 1, 1023 bit data and synchronization code) is a clear PSK data signal transmitted at data rates higher than those that could be supported by the Mode 1 PN signal transmission. It is expected that such data will be at rates sufficient to reduce signal power density below critical levels with respect to meeting flux density criteria.

The various signal structures corresponding to Modes 1, 2, and 3 are shown in figure 2.2-2.

2.2.2 Ground Receiver

E

a (

1

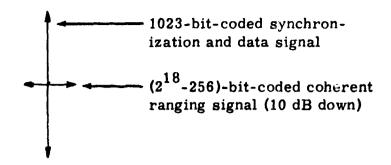
The TDRS ground receiver system performs three basic receiving functions:

- 1. Receives multiple access and single access sent to the TDRS relay satellite on both S-band and K-band, at K-band (i.e., both are translated to K-band).
- 2. Receives test signals returned from the TDRS satellite, when the system is in the test mode.
- 3. Receives TTNC signals when they are being sent during launch operations.

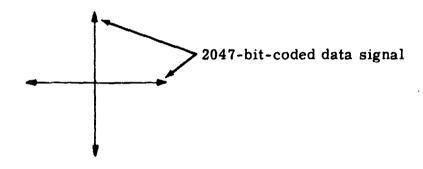
Figure 2.2-3 illustrates the frequencies used by the TDRS system in links to and from the ground to the satellite, and to and from the TDRS relay satellite to the user satellite (or other user, such as Space Shuttle). TDRS-to-ground signals are:

13.937 GHz K-band signal access. 225 MHz bandwidth provided. May be split into two 88 MHz-BW channels.

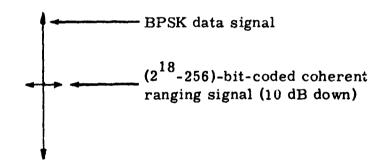
13.7 to 13.725 GHz S-band single access signals. Two 10 MHz bands provided, with 5 MHz guard band (25 MHz total)



a. Mode 1 Signal Structure (Coherent Turnaround)



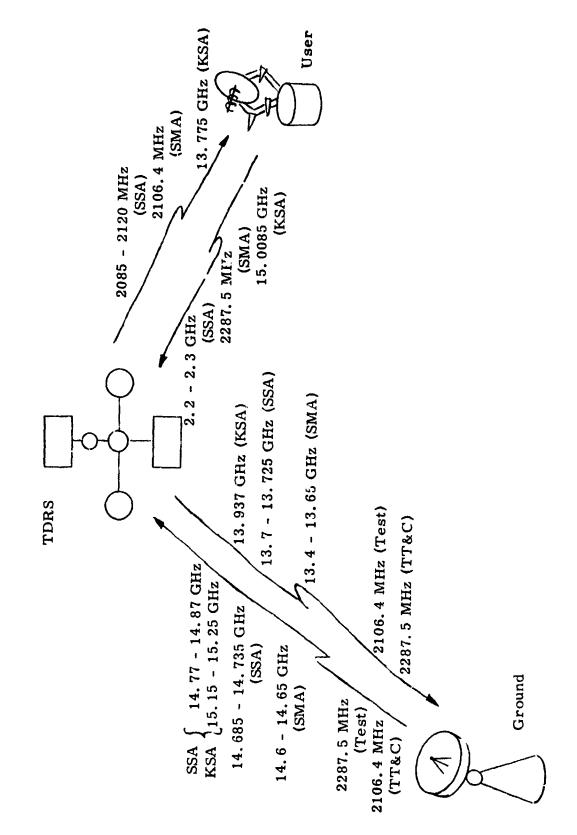
b. Mode 2 Signal Structure (Noncoherent Turnaround)



c. Mode 3 Signal Structure (Coherent Turnaround)

Figure 2.2-2. Signal Structure

•



Ü

4.0 4.0

Figure 2.2-3. Frequencies Used in TDRS for Various Links

13.4 to 13.65 GHz	S-band multiple access users. 42 channels provided. 41 at 6 MHz spacing and one at 4 MHz spacing. 40 slots with 4.5 MHz BW for downlink user signals, 2 slots for turnaround ranging.
2106.4 MHz	Test receive frequency for TDRS satellite transmitter (same frequency as TDRS-to-user)
2287.5 MHz	Receive frequency for TT&C signals used during satellite launch period. Same frequency as user-to-TDRS.

Figure 2. 2-4 illustrates a receiver design that could serve to meet the requirements of the TDRS-to-ground link. It provides for both K-band and S-band reception of signals, using as much common circuitry and subsystems as possible. A more detailed version of this receiver is described in section 3.2 of this report.

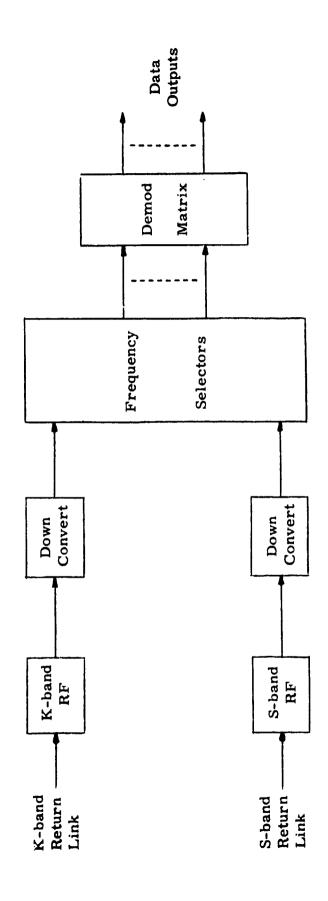
2.2.3 System Performance

The results obtained for the S-band multiple access return link Mode 2 synchronization analysis are summarized below. One of the objectives in the study was to establish the required length of the PN code sequence. A code length of 2047 chips was recommended. The performance objectives are:

Mean Acquisition Time	15 seconds
Probability of Detection	0.9
Probability of False Alarm	10 ⁻⁶
Probability of Detecting Interfering Signal	10-2

The results are obtained for the case where the signal is uncoded and for the case where a half-rate convolutional code with a Viterbi decoding algorithm is employed. One of the major steps in the analysis was the interfering signal analysis and the likelihood of false locking to an interfering signal.

O



Simplified Block Diagram of Ground Receiver Figure 2. 2-4.

3

7.

8

Ü

•

,,

The system constraints are:

4.

C'/No (without coding)

39.9 dB-Hz

C/N₀ (with coding)

34.9 dB-Hz

Total doppler and frequency uncertainty

+ 2.5 kHz

A fixed length test strategy was employed for the ground receiver synchronization analysis. The detection performance analysis results for both the desired and interfering signals is summarized in table 2.2-1. Although through the verification state, neither the detection probability objective of 0.9 nor the false alarm probability objective of 10⁻⁶ is satisfied, the code tracking and carrier lock thresholds can be set to achieve the above requirements. The average acquisition time analysis at threshold is summarized in table 2.2-2 for the dual mode fixed length test strategy. A single 5 kHz IF bandpass filter covering the total doppler and frequency offset uncertainty is assumed. Clearly, the acquisition times can be reduced considerably by multiple doppler resolution filters as recommended for the user transponder. For a code length of 2047 chips, both with and without coding, the average acquisition time objectives of 15 sec are achieved.

Table 2.2-1. Detection Performance of Desired and Interfering Signals Code Length $N=2^{11}-1$

Performance		Desire	d Signal		U	ndesired	i Signal	
	Acquis	ition	Verifi	cation	Acquis	ition	Verifi	cation
Link Condition	P _{FA}	P _D	P _{FA}	P _D	P _{FA}	P _D	P _{FA}	P _D
Without Coding	10-2	0.58	10-4	0.95	10 ⁻²	1.0*	10-4	2 x 10 ⁻⁴
With Coding	10-1	0.47	10-2	0.74	10-1	1.0*	10-2	7 x 10 ⁻²

^{*}This assumes one searches through all possible cell positions.

\$.

.

Table 2.2-2. Average Acquisition Time vs. Code Length

Code Length N	Average Acc	quisition Time,	T _{ACQ} (sec)
Link Condition	2 ¹¹ - 1	2 ¹³ - 1	2 ¹⁵ - 1
Without Coding	3. 9	15.4	61.5
With Coding	14, 7	58.6	234.5

APPENDIX A. 2

GENERAL COMPARISON OF BIPHASE AND QUADRIPHASE (DOUBLE-BINARY) MODULATION

A. 2. 1 Modulation

Biphase modulation is readily accomplished through use of a simple diode-balanced mixer. These are available from a number of manufacturers (Relcom, H-P, Mini-Circuits Lab, Varí-L, and others). Their equivalent circuit is shown in figure A. 2-1.

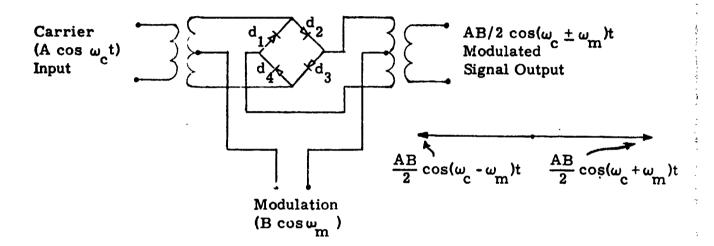
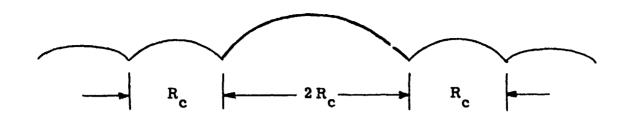


Figure A. 2-1. Biphase Modulator

Operation is such that the modulation input causes either d_1 and d_3 or d_2 and d_4 to conduct at any given time, with the other diode pair cut off. Thus, either one phase of the input carrier or the opposite phase (0° or 180°) is coupled to the output. If $B\cos\omega_m t$ is a code sequence, then a carrier, biphase modulated with the code, is the output signal.

The output signal has a power spectrum which has an envelope having a $(\sin x/x)^2$ shape, where the main lobe is $2R_c$ wide $(R_c$ is the code sequence clock rate) and the sidelobes are R_c wide. The first side lobes are 13 dB down, and the envelope falls off at a 6 dB per octave rate thereafter.

Approximately 10 percent of the energy falls outside the main lobe.



Quadriphase modulators are approximately three to four times as complex, on the basis of components required, as biphase modulators. (This is true whether the modulator is simple quadriphase or some form of offset quadriphase.) A quadriphase modulator commonly is constructed as in the following diagram (figure A. 2-2).

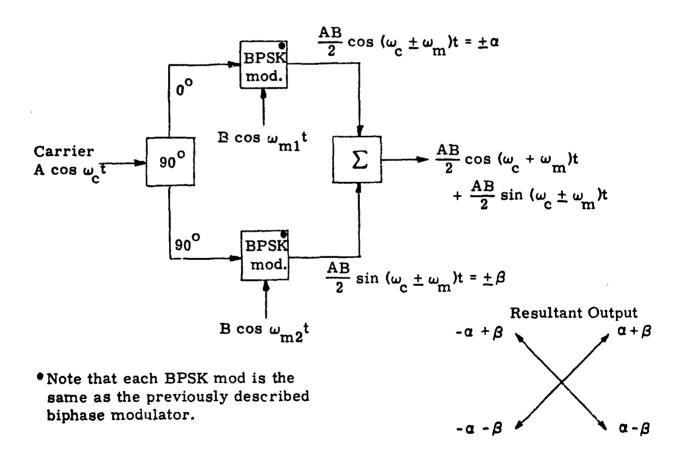


Figure A. 2-2. QPSK Modulator

^{*}R. C. Dixon, Spread Spectrum Systems, John Wiley & Sons, 1976, p. 21, 234.

The power spectra for both simple quadriphase and double-binary are the same as for biphase (when all modulating signals are at equal rates). Two advantages exist for the quadriphase signals, however:

- 1. They can tolerate passage through a limiter simultaneously with a narrowband coherent carrier, which a BPSK signal cannot do.
- 2. They can be filtered and subsequently limited, without appreciable reconstitution of the undesired sidebands, which is not true of BPSK signals. (In fact, this is true only of the double-binary or offset QPSK signal format.)

The offset quadriphase signal can be filtered to a desired BW and then passed through a saturated power amplifier. This is not practical for BPSK or simple QPSK signals, however. Therefore, in a spacecraft that employs a saturating TWT power amplifier, one must pay the hardware penalty for implementing QPSK modulation and demodulation, but the transmitted signal is more efficient, due to all of the relevant energy being packed into a $\pm R_c$ bandwidth around the carrier. Where 10 percent of the BPSK signal goes into sidelobe energy, only 5 percent or less goes into sidelobe energy in the offset QPSK format. Therefore, the savings in signal power can be translated into a direct signal improvement for offset QPSK signals.

A. 2. 2 Demodulation

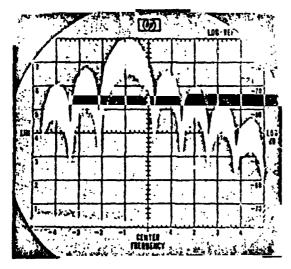
Demodulators for BPSK and QPSK signals are similar. Where data is sent phase-shift-keyed, a Costas demodulator or squaring demodulator is normally employed, and there is little difference in them, whether they are for BPSK or QPSK signals.

The amount of hardware needed is similar, so no further receiver demodulator comparison will be made.

The received signal bandpass filter should be considered in the light on sending either QPSK or BPSK signals. That is, if the power amplifier transmits a BPSK signal, it will have a $(\sin x/x)^2$ distribution whether it filters before amplification or not. For the offset QPSK signal, however, only the main lobe of the signal may be transmitted. If the

Costas and squaring demodulators are different, but there is little difference in a Costas demod for BPSK or one for QPSK. Squaring demods are in a similar vein.

receiver bandwidth is just wide enough to accept the main lobe, then it throws away the BPSK sidelabe energy. An increase in bandwidth to include the first two sidelabes causes a net signal loss, since the increase in receiver noise is greater than the increase in received signal. Therefore, it is seen that the BPSK signal format is advantageous from the standpoint of transmitter simplicity, but it loses in the area of effective transmitter power. This is illustrated in the patterns of figure A. 2-3, one of which is the spectrum of a BPSK signal after limiting, whether filtered or not, and the other shows an offset or staggered QPSK signal spectrum after filtering and limiting. This comparison is at the heart of the tradeoff between BPSK and QPSK, with the possible improvement in signal-to-noise ratio being a maximum of 0.9 dB for SQPN over simple biphase signal transmission.



1)

a. Filtered and limited QPSK signal, Note that the sidelobe level is the same as if filtering had not occured. (This reaction is typical of both biphase and quadriphase direct sequence signals.) Filter bandwidth = 2 R_{clock}.

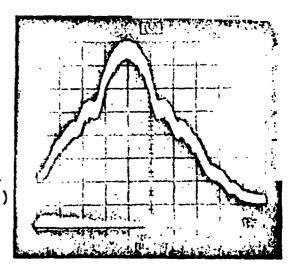


Figure A.2-3. Comparison of Normal and Offset QPSK Signal Spectra

b. Identical filtering and limiting of a doublebinary or staggered quadriphase signal. Firssidelobe level is now down 25 dB, or 12 dB blow the level of the signal in (a) above. We have not considered filtering after the power amplifier, as this does nothing to preserve signal power in any case.

(

A. 2. 3 PSK Modulation Considerations for Simultaneous TDRSS Signals

Phase shift keyed (PSK) modulation offers significant performance and implementation advantages in communication systems when compared to other forms of modulation. Phase shift keying provides the lowest threshold performance available. In addition, this modulation form is directly applicable in the spread spectrum and high data rate areas required in TDRSS.

Two forms of PSK are of primary interest for use in TDRSS: biphase and quadriphase modulation, wherein the information is conveyed as either one of two or one of four phases for each information symbol. These are of interest not only because of their spread spectrum and/or high data rate compatibility but because they lend themselves to transmission of multiple signals with minimal mutual interference between those being sent.

In the following paragraphs, we will examine various combinations of biphase and quadriphase signals to determine the effects of operating with them simultaneously in linear and saturating channels.

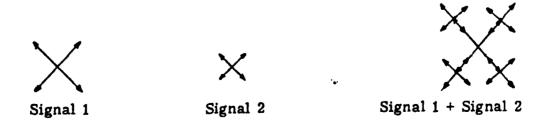
Signal 1	Signal 2
QPSK	QPSK
QPSK	BPSK
BPSK	QPSK

Modulation Possibilities

BPSK

8

Let us first consider that one signal (2) is always 10 dB smaller than the other signal (1). (See figures A. 2-4 through A. 2-7.)

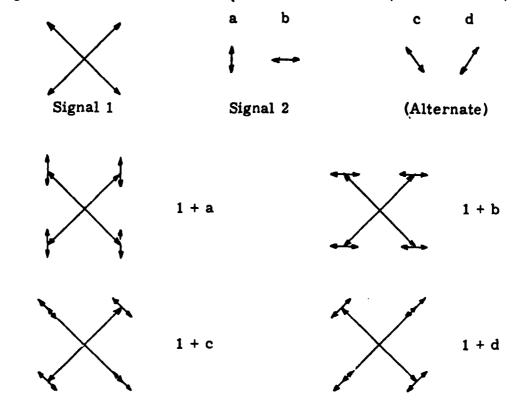


BPSK

Figure A. 2-4. Case 1 - Linear Summation, Two QPSK Signals

Note that amplitude modulation occurs for some phase states of signal 2. That is, signal 2 may add or subtract from signal 1.

Figure A. 2-5. Case 2 - One QPSK and One BPSK (10 dB Smaller) Signal



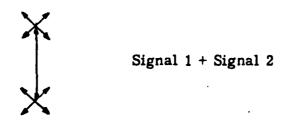
0

Ŋ.

8

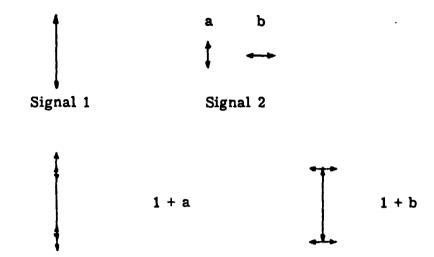
Figure A. 2-6. Case 3 - BPSK Signal with Smaller QPSK Signal





Amplitude modulation occurs for all phase states of case 3.

Figure A. 2-7. Case 4 - Two BPSK Signals, Different Amplitudes



Note that no amplitude modulation* is produced by combining the orthogonal signal pair {90, 270} and {0,180}.

How, then, can a signal be modified to produce a constant-amplitude* signal (steady state) when the desire is to transmit two QPSK signals?

The following signal combination would be satisfactory (figure A. 2-8):



Figure A. 2-8. QPSK Combined with Selected-Phase QPSK (Combined Signal)

$$\% AM = (1 - \cos \phi/2) \times 100$$
.

That is, the carrier signal can be expected to drop to an amplitude equal to $\cos \phi/2$ times its steady state value during a phase transition. Thus, it is easy to see the advantage of SQPN modulation (90° phase shifts) over standard QPSK modulation (90° and 180° phase shifts) since the incidental AM produced is 30% rather than 100%.

^{*}These signals are constant-amplitude only in their steady-state condition. Incidental amplitude modulation does occur in the transition from one phase state to another. Where a phase shift is ϕ degrees, the incidental amplitude modulation that can be expected is

This signal can be generated from a pair of QPSK signals, but the signals must be properly managed.

1.

Incidentally, it does not matter whether the signals in question are QPSK or SQPSK. The same considerations hold--since SQPSK differs from QPSK only in that the order of phase shifts is changed by modifying the data (or code) fed to the phase modulators used.

A further modification to the code used by the smaller signal (signal 2) can produce the desired orthogonal pair of QPSK signals.

If the phase mapping for signal 1 is:

Da	<u>tta</u>	
0	0	45 ⁰
1	0	135 ⁰
1	1	225°
0	1	315 ⁰

let the phase mapping for signal 2 be the same.

To produce the desired combined signal, the overall phase mappings allowable are:

Signal 1	Signal 2							
45°	135° or 315°							
135 ⁰	45° or 225°							
225°	135° or 315°							
315°	45° or 225°							

This means that only certain code states may be permitted for code pair 2, based on the state of code pair 1. These are:

Code pair 1	Code pair 2								
00	10 or 01								
10	00 or 11								
11	10 or 01								
01	00 or 11								

This can be accomplished by modifying one code in one of the code pairs used in a double-quadriphase signal set (two quadriphase signals) on the basis of the other code pair. Such a technique is illustrated in the example that follows.

1

Code pair 1	0	0	1	1	1	0	1	0	1	1	0	0	1	0	0	1	0	• • •
	0	1	0	0	1	1	0	0	0	1	1	0	1	1	1	0	1	•••
Code pair 2	1	0	1	1	0	0	0	1	0	1	1	1	0	1	0	1	1	•••
(unmodified)	0	1	0	1	1	0	1	1	1	0	0	0	1	0	1	1	0	
(Δ signifies notallowed state)		Δ	Δ				Δ	Δ	Δ		Δ			Δ	Δ		Δ	
Code pair 2	1	0	1	1	0	0	0	1	0	1	1	1	0	1	0	1	1	
(modified)	0	0	1	1	1	0	0	0	0	0	1	0	1	1	0	1	1	

The only question is - what happens to the correlation properties of the long code. An alternate coding rule would be to repeat the last allowed state when a not-allowed state is next. This would change the code also, but would be a more complex rule.

To summarize, where two unequal level signals are to be transmitted simultaneously, then it is recommended that both be either biphase or quadriphase. Combinations of biphase and quadriphase signals do not readily adapt to constant-amplitude signalling. Where saturating amplifiers are employed, both constant-amplitude signals and minimum incidental AM are desirable. For those cases where a combination of two signals produces AM, that AM would be lost in transmission through a saturating amplifier. The case for minimum incidental AM is made because bandpass filtering ahead of the saturating amplifier can suppress small amplitude modulation to an extent that it is not restored to any significant degree in the nonlinear amplification process. This in turn reduces transmitter sidelobe energy and improves signalling efficiency.

The signals that result from combining either two BPSK or two QPSK signals are shown in figure A. 2-9. (One of the two in each case is $10~\mathrm{dB}$ smaller than the others.)

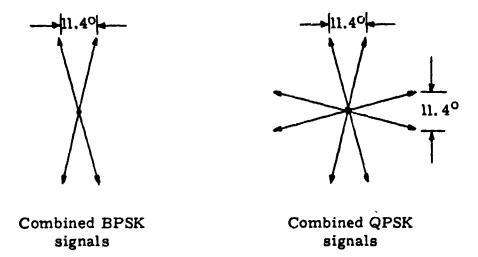


Figure A. 2-9. Comparison of Combined BPSK and QPSK Phase Diagrams

In both cases, incidental AM due to the combining of signals is only 0.49%. Incidental AM for the individual signals is the same, however, as if the other signal were not there (i.e., 100% for the biphase signals and 30% for staggered quadriphase signals).

II. Consider now the case of equal amplitude carriers, but those having arbitrary phase and/or frequency relationships. (It is considered that the phase and/or frequency of carriers used is known and controlled, but our interest here is in the effect of the relationships between the pair of postulated carriers.)

We will consider that this is the case for transmission of data group 1 and data group 2 signals. Data group 1 and 2 signal characteristics are summarized as follows:

Data Group 1

PN modulated (SQPN)

6 Mbps code, 2¹⁹ long

Data rate: 1-300 kb/sec

same on I and Q

data embedded in 6 Mbps code

Data Group 2

1

No PN modulation

Data QPSK

Data rate:

1 kb - 300 Mbps total

I:

1 kb - 150 Mbps

Q:

1 kb - 150 Mbps

I and Q rates independent and either synchronous or asynchronous

The Data Group 2 carrier may be asynchronous with the Data Group 1 carrier.

Assume the two following QPSK signals (figures A. 2-10 and A. 2-11):

Figure A. 2-10. DG1 and DG2 Signals

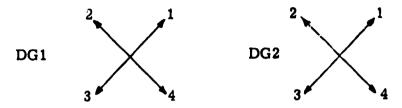
Data rate has little effect except to determine the rate of phase shifts. QPSK/SQPN also has little bearing except to determine rate of phase shifts and phase difference from shift to shift. (SQPN allows only 90° shifts. QPSK can shift 180° or 90°.)

Carrier amplitude, frequency, and relative phase have much more effect.

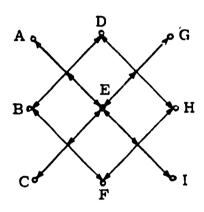
Let DG1 power = DG2 power

φ₁ = φ₂

DG1 carrier # DG2 carrier



Linear channel:



Loci of possible phase positions for two equalvalue 4-phase signals, linearly added. (Note ambiguity.)

Figure A. 2-11. Combination of Two Equal QPSK Signals

The same combined phase mapping results if the two carriers are offset in phase, except that the combined phase map is itself rotated.

There are 4^2 = 16 possible combinations of two four-phase signals. The combined, linearly-added signals have only 9:

$$1_{3} + 2_{1} = E$$
 $1_{3} + 2_{2} = B$
 $1_{3} + 2_{3} = C$
 $C = 2 P / 225$
 $1_{3} + 2_{4} = F$
 $F = \sqrt{2} / 270$
 $1_{4} + 2_{1} = H$
 $1_{4} + 2_{2} = E$
 $1_{4} + 2_{3} = F$
 $1_{4} + 2_{4} = I$
 $I = 2 P / 315$

I

ŧ

Occurrences:
$$A = 1$$
, $B = 2$, $C = 1$, $D = 2$, $E = 4$, $F = 2$, $G = 1$, $H = 2$, $I = 1$

This is not the case in the saturating or limiting channel (figures A. 2-12 and A. 2-13):

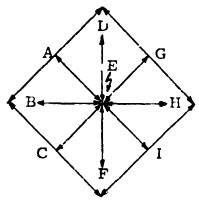


Figure A. 2-12. Combined QPSK Signals in a Limiting Chann l

This phase table is the same as for the linear channel, but the amplitude table is different:

G = P
$$\frac{45}{180}$$

D = P $\frac{90}{180}$
E = 0 $\frac{6}{180}$
E = 0 $\frac{6}{180}$
F = P $\frac{225}{180}$
H = P $\frac{6}{180}$
I = P $\frac{225}{180}$
A = P $\frac{180}{180}$

(letters correspond to linear channel phase diagram)

Occurrences: Same as linear channel if amplitudes of DG1 and carriers are precisely equal.

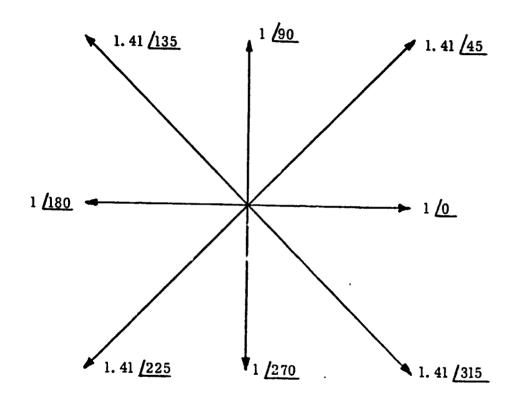


Figure A. 2-13. Eight-Phase Phase/Amplitude Resultant of Summed Equal-Amplitude QPSK Signals (Carriers Coherent)

If carriers are not equal in amplitude (and they seldom would be), then whichever is larger will dominate in positions A, C, G, and I, as in the following phase tables.

(Remember that the saturating amplifier we are discussing tends to drive any signal above a value α to the point of amplitude limiting. In such a case, if two carriers are not exactly equal, and their difference is $\geq \alpha$, then the larger signal will dominate and suppress the smaller signal.)

Assume PDG1 > PDG2:

Occurrences: 0 = 2, 45 = 2, 90 = 2, 135 = 2, 180 = 2, 225 = 2, 270 = 2, 315 = 2

Assume PDG2 > PDG1:

 $PDG2 - PDG1 \ge a: aK \ge P$

Z.

Occurrences:
$$0 = 2$$
, $45 = 2$, $90 = 2$, $135 = 2$, $180 = 2$, $225 = 2$, $270 = 2$, $315 = 2$

It is most notable that, for a pair of quadriphase signals of equal amplitude, passing through either linear or limiting channels, the combined phase mappings result in ambiguities that cause loss of information. That is, where two quadriphase signals separately represent 16 possible symbol-pairs (and thereby four bits of information), only eight phases result from their combination, with the same phase resulting from more than one signal pairing.

The examples shown consider that the two signals of interest maintain a constant phase relationship. What if the two carriers are not at the same frequency? Where this is true, then the same two QPSK phase diagrams hold, but one of the two may be considered to rotate with respect

to the other. This then effectively causes the signal that is rotating to add a continuous phase shift component, with rotation at the difference frequency between the two carrier signals. The combined phase diagram for two QPSK signals with different carrier frequencies would be (figure A. 2-14):

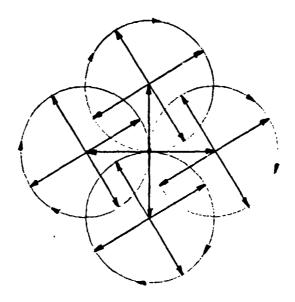


Figure A. 2-14. Rotating Phase Combination of Two Equal Value But Frequency Offset QPSK Signals

and 100 percent amplitude modulation would result, as well as phase rotation of 360° at the difference frequency rate. This would occur addition to independent discrete phase modulation by the two data signals

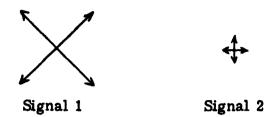
Such a signal would be difficult to handle in the linear channel and could degrade in the saturating channel to the point of being unusable.

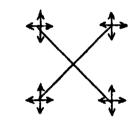
Extending Case 1 (the pairing of a QPSK signal with a second QPSK which is smaller by 10 dB and whose carrier is at 90 degrees), Case 1a, which follows, considers the same QPSK carriers but shifts the smaller signal so that it is at a 45° angle with respect to the larger signal.

The resulting composite signal is an amplitude- and phase-modulated resultant that has very small phase shifts, together with amplitude modulation of approximately 9 percent. Such signals are not useful in a system employing saturated traveling wave tubes (or even solid state RF power amplifiers) that exhibit AM/PM conversion on the order of 4 to 12 degrees per dB of amplitude shift, since the phase modulation produced by the incidental AM is larger than that produced by the intended phase modulation.

Case 1a (see figure A. 2-15) illustrates the problem faced with any form of modulation in TDRS that produces incidental amplitude shifts due to addition of two or more signals, where the composite signal is to be processed in a power amplifier. This especially applies to the two-signal or simultaneous signal approach to TDRS user synchronization and data transmission, whether the signals being sent are direct sequence signals (data group 1) or high speed data signals (data group 2).

Typical AM/PM conversion in a saturated TWT PA is as much as 6 to 8 degrees per dB. For this modulation, amplitude difference is 1.48 - 1.35 = 0.12 or $0.13/1.48 \times 100 = 8.78$ percent. This would be a 0.399 dB difference, for a 2.4° phase shift. Thus, a phase shift produced by an amplitude change would be greater than that produced by modulation of the phase by the data being sent.





Signal 1 plus Signal 2

Figure A. 2-15. Case 1a - Two QPSK Signals

Signals produced are:

ŧ.

1.35 $\sqrt{42}$	1.35 $\sqrt{222}$
1.48 $\sqrt{42.3}$	1.48 /222.3
1.48 $\sqrt{47.7}$	1.48 /227.7
1.35 /48	1.35 /228
1.35 /132	1.35 /312
1.48 $\sqrt{132.3}$	1.48 $\sqrt{312.3}$
1.48 /137.7	1.48 /317.7
1.35 /138	$1.35 {318}$

Phase mapping would be:

()

Compare this phase mapping with the first signal set:

In this quadrant, the unintended phase modulation due to AM/PM conversion would be 2.4° greater than the intended modulation, for the conservative estimate of 6 degrees per dB of amplitude shift.

3.0 SUBSYSTEM DESIGN

This report section describes user transponder and ground receiver subsystem designs that are postulated for TDRSS use. These subsystem designs do not represent either final recommendations or optimal designs, but are presented as practical configurations that may, in turn, be used as bases for comparison and for system configuration.

3.1 User Transponder

This section presents a transponder design which reflects possible implementation with contemporarily available components; that is, none of the subsystems presented depends on development of new or higher performance components than those presently available.

The selected approach for TDRS signal structure is the use of a direct sequence waveform for acquisition, as well as data transmission. A pair of direct sequence modulated signals will be transmitted simultaneously. One signal is BPSK modulated with a 1023 bit code sequence that is, in turn, sequence-inversion-modulated with data. The second signal is BPSK modulated with a 2¹⁸-256 bit code sequence, and has no data modulation. The second signal is transmitted at a level 10 dB below the first, and on a carrier signal phase-shifted by 90 degrees from it.

Both the 1023 bit (short) and 2^{18} -256 bit (long) codes will use the same $31f_1/96 = 3.077799$ Mbps clock, and the all-ones vectors in both the generators will be set to coincide at a given point in time. Thus, the long code will repeat in exactly 256 repetitions of the short code all-ones vector.

The receiver will then have to search a maximum of 1023 bits to acquire short code synchronization; once short code synchronization is achieved, the long code ambiguity is reduced to 1/256. This is true because a receiver synchronized to the short code knows when the long code all-ones vector will occur, except that it occurs only once every 256 short code all-ones occurrences. If the receiver then resets its long code at each short code all-ones vector, and monitors its correlator for synchronization until the next one, then all it needs to do is decide if it is synchronized. If so,

then it does not reset; but if not, then it resets and tries again during the next interval.

Actually, the long code monitoring or integration period is not just one but may be many periods of the short code. This is done to make up for the reduced (-10 dB) power in the long code modulated signal. If, for example, the integration period is an average of 10 short code periods, then long code acquisition time is $256 \times 10 \times 322 \, \mu sec = 824 \, msec$. (Actual long code acquisition time is expected to be <2 seconds.) This time is in addition to short code acquisition time, since the short code must be acquired first.

The short code modulated acquisition signal employed will be the data transmission signal, and will be transmitted continuously. Therefore, a user may acquire the signal at any time without a need for any special transmission or procedure. The long code modulated signal will be used only to resolve range and multipath ambiguities.

Figure 3.1-1 is a simplified block diagram showing the modulator and demodulator configuration for the selected TDRSS signal acquisition approach.

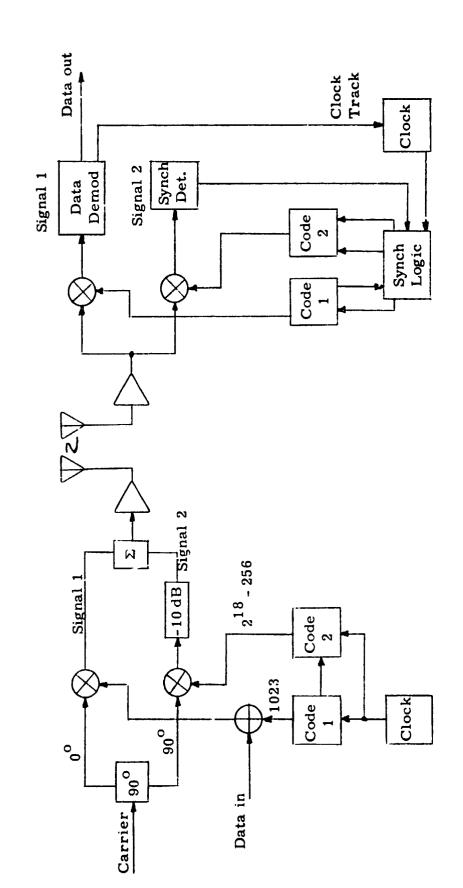
3.1.1 Overall Design

Figure 3.1-2 illustrates a transponder configuration using a 221/240 frequency turn-around ratio. The configuration shown departs from the Standard Transponder design, in that the second IF is a function of the f₁ reference oscillator frequency rather than an auxiliary f₂ oscillator. This configuration has the advantage that it does not employ an f₂ oscillator (about 12.25 MHz for a standard transponder) but it does have a second IF frequency that changes if the operating frequency is changed. For TDRS, with 221 f₁ at 2106.40625 MHz, f₁ and the second IF would be 9.53125 MHz.

A demodulator is part of this configuration. When relaying data, that data would preferably be demodulated to baseband and used to remodulate the relayed signal. This remodulation would be accomplished by modulo-2 addition with the transmit code. The alternative is to preserve

これは強い 一直はなる このをはないないない アフトングランド あななない こうかいれる はない

THE THE PROPERTY OF THE PROPER



Simplified Modulator and Demodulator Using Simultaneous Signal Approach Figure 3.1-1.

€,

ĸ

8

・・・・ ・ 大 をなるとこ・・

•

ている を見り 一日の神をからっていたいから、ころのです。 こうしきのはまます しんけん ゴルモーカ はてなななななな

1.

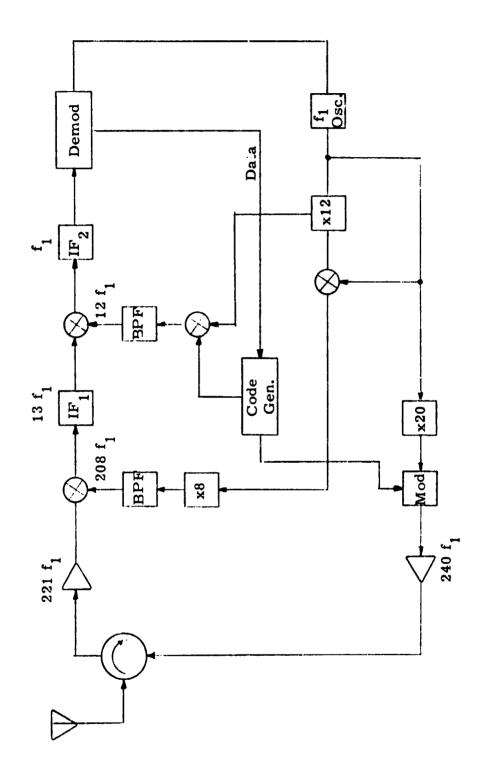


Figure 3.1-2. Basic Transponder Frequency Scheme and Signal Flow

the data as carrier PSK, translate this signal to 240 f_1 , and overlay it with code modulation.

In practice, the data would not go directly from the demodulator to be used as a signal for the modulator, but would be processed as required within the spacecraft.

Figure 3.1-3 shows a more detailed block diagram of the data demodulation channel. A 221 f₁ received signal would be converted to 13 f₁, where it would be power-divided (by 4). One signal would be multiplied with a local reference (BPSK modulated with the 1023 bit code) which would, when synchronized, produce a signal PSK modulated with data at the IF2 frequency. This would then be demodulated by a squaring loop, and the data signal output for processing. A squaring-loop demodulator is shown because it is somewhat simpler than a Costas demodulator, although a Costas loop could readily be substituted for it. Performance of Costas and squaring loop demodulators has been shown to be the same.*

The squaring loop VCO would be multiplied to produce the 240 f₁ frequency.

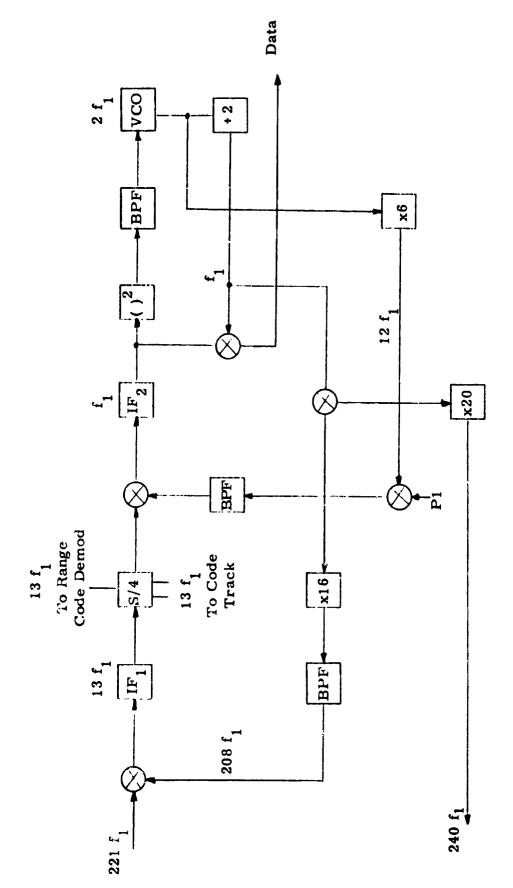
One of the signals from the IF1 power divider would be applied to a balanced mixer along with the range code (2¹⁸-128 bits). When the range code signal is synchronized, a CW output signal appears at the mixer output, passes through a bandpass filter, is amplified and envelope detected, integrated and applied to a threshold detector. When a signal is detected, the range code generator is allowed to continue without reset, and is traced by the data code loop. This range channel subsystem is illustrated in Figure 3.1-4.

The other two signals from the IFI power divider are fed to a pair of balanced mixers (see Figure 3.1-5) whose reference inputs are a pair of time-offset codes. These produce a differential in correlation output signals when filtered and detected, which are differentially amplified, filtered, and used to control the code clock frequency. Thus, the receiver code

^{*}R. L. Didday and W. C. Lindsey, "Subcarrier Tracking Methods Communication System Design," JPL Report 32-1317, August 1968.

I was made and

こうこう からない はんか アン・コー こうかん はっていまればない はんない



Data Channel Block Diagram and Frequency Scheme Figure 3.1-3.

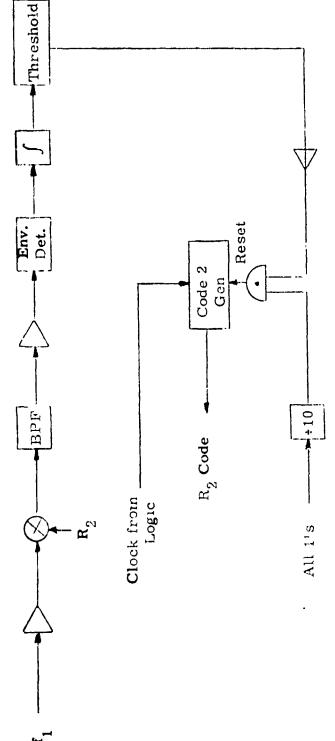


Figure 3.1-4. Range Channel Block Diagram

4,

٠.

いき はったってきるとうとうとうとうないということ

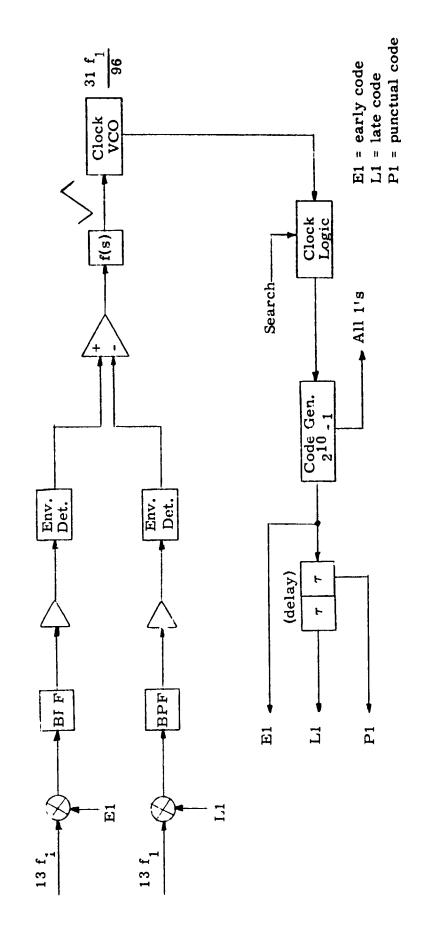


Figure 3.1-5. Tracking Channel Block Diagram

4

2

1

D

ことでいる

rate is tracked with the incoming signal's code rate. (This subsystem is a conventional delay-lock loop.) An alternate technique would be to employ an incremental phase modulator instead of the VCO. This incremental phase modulator would modify the phase of a $31\,f_1/96$ signal derived from the demodulator's f_2 VCO.

An accurate clock source is vital to any spread spectrum system, since code drift can drastically affect synchronization time. The quartz crystal oscillators appear to have the edge for on-board spacecraft use, because of their size, weight, power, and reliability. (It is interesting to note that a hydrogen maser has been flown as a frequency source.) One of the atomic standards (cesium or rubidium) would be good for ground use.

3.1.2 Electrical Specifications for User Transponders

A number of electrical specifications for user transponders may directly affect the performance of the TDRSS with respect to achievable data rate(s). Some of these are examined in the following pages, with their effects, in order to arrive at minimal specifications without causing the implementation task to be too difficult.

In addition to analysis oriented to determining the effects of the parameters of interest, prospective transponder designers have also been contacted for comments with respect to their estimates of difficulty of implementation. These comments have also been considered in determining specifications.

The specifications of specific interest, with suggested specification limits, ... e given in table 2.1-7. Considerations in determining these specifications are described in the following pages.

User Oscillator Phase Noise

8

X

It is desirable to hold user oscillator phase noise to as low a value as is practical for a voltage controlled oscillator. The noise produced by the oscillator is multiplied, and appears at both receive local oscillator frequencies and transmit frequencies as a much larger amount of random phase noise. Investigation of the capability to hold phase noise down shows

that present systems are capable of <15° phase noise, at S-band, where the measurement is made with integration over a 6 Hz to 2.5 MHz bandwidth.

Modulator/Demodulator Phase Imbalance

Phase imbalance is especially important to a quadriphase modulator. (It is equally important to a biphase modulator, but phase between halves of a transformer winding is difficult to maintain at anything other than 180°, which is that desired for BPSK.) Quadriphase modulation, on the other hand, can easily exhibit phase imbalance—usually occasioned by an offset in the carrier phase input to the two biphase modulators included in a QPSK modulator.

Phase offset in a QPSK modulator would be exhibited by producing signals similar to those seen in figure 3.1-6.

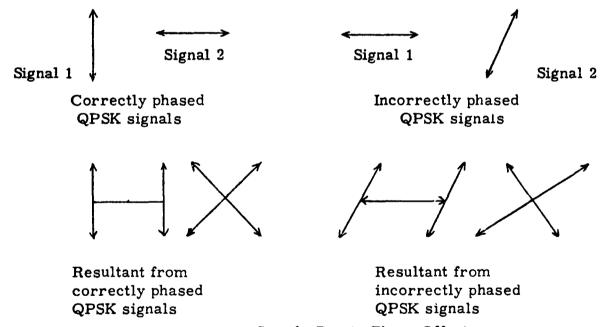


Figure 3.1-6. Signals Due to Phase Offset

This phase imbalance would produce an amplitude imbalance that could, in turn, cause large incidental phase shifts in the signal at the power amplifier output (see page 3-13).

It is suggested that amplitude imbalance be held to a maximum of 1 dB total, for both direct amplitude shifts and for incidental AM caused by paired-signal phase shifts. If 0.5 dB is allocated to each cause, then

signal amplitude would vary from 1 (normalized) to 0.891. Therefore, the maximum phase shift allowable would be approximately 6.5 degrees.*

Modulator/Demodulator Amplitude Imbalance

Where a pair of signals are unbalanced in amplitude, the signal resulting from their being combined is affected in both amplitude and phase angle. In a previous section of this memorandum, it was considered that amplitude balance could be held to within 0.5 dB. In that same section, it was shown that a 0.5 dB amplitude shift corresponds to a 6.5 degree phase shift.

Data Asymmetry

In a biphase or quadriphase modulator, the effect of data asymmetry is to cause a DC bias in the output, which in turn causes unbalance at the second harmonic of the data. (For code-driven modulators, the code is unbalanced.) This then produces a strong carrier component at the code sequence bit rate, which appears as a signal at the nulls of the cutput signal spectrum. (See figure 3.1-7.)

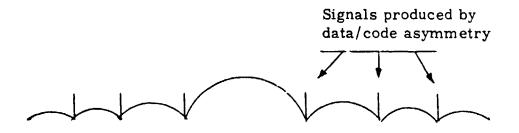


Figure 3.1-7. Direct Sequence Signal with Data/Code Symmetry

*From the formulae derived on page 3-13:

(sin 6.5 + 1) + j cos 6.5 = 1.492 41.75(sin 6.5 - 1) + j cos 6.5 = 1.331 131.75 $\frac{1.331}{1.492} = 0.892$.

If data signals are held to symmetry within 1%, then the signals seen at spectrum nulls should be ≥10 log 100 = 20 dB below the unsuppressed carrier signal.

Data Skew

Data skew primarily affects the signal shaping, since the effect of such skew is one of causing signal transitions to occur at times other than those for which the system is designed. As long as data transitions are not skewed to the point that both data transitions in a QPSK modulator occur simultaneously, there is no effect. (We restrict this argument, however, to one in which the receiver may separately track the two data streams. Where only one of the two signals is tracked, data skew should be avoided to as great a degree as practical.)

AM-to-PM Conversion

AM/PM conversion and distortion experienced by an amplitude modulated signal in being processed by a TWT power amplifier is discussed on page 3-16. For some of the signals proposed, this AM/PM conversion can produce phase shifting signals that are larger than those that convey the desired information. Therefore, the aim in choosing modulation formats has been to choose a format that has minimum steady-state amplitude shifts. (We note that some amplitude shifting is inevitable during phase transitions, but that proper signal selection can provide minimum amplitude shift after setting to a new phase.)

Phase Characteristics

Both sinusoidal and quadratic phase characteristics and their effect on PSK signals have been well defined by Jones.* The curves given by Jones may be employed to specify the allowable signal distortion, given a maximum allowable signal degradation or loss in performance.

^{*}J. J. Jones, "Filter Distortion and Intersymbol Interference Effects on QPSK," Proc. Hawaii Conf. Syst. Sci., January 1970.

Effect of Phase Shift Between Orthogonal Signal Pairs

A balanced biphase modulator's output (in the modulated signal band of interest) may be written as (see figure 3.1-8):

$$A^* \cos \omega_c t + \omega_m t$$

where the input carrier is B $\cos \omega_c t$ and the modulating signal for the case of interest here is C $\cos \omega_c t$.

The modulating signal is $\phi(t)$, where ± 90 degrees is the only accepted modulation, and the period of the modulating signal $\omega_{\rm m}$ is that of either a coded signal or data modulation. That is, a +1 is represented by A cos $\omega_{\rm c} t + 90^{\circ}$, and a -1 is represented by A cos $\omega_{\rm c} t - 90^{\circ}$.

This signal format may be extended to quadriphase (QPSK) modulation by realizing that the QPSK modulator is a pair of biphase modulators (figure 3.1-9) whose outputs are summed. The QPSK signal may be expressed as

A cos
$$\omega_c t + 90^\circ + D \sin \omega_c t + 90^\circ$$

which results in four possible output signals

A
$$\cos \omega_c t + 90^\circ + D \sin \omega_c t + 90^\circ$$

A $\cos \omega_c t + 90^\circ + D \sin \omega_c t - 90^\circ$
A $\cos \omega_c t - 90^\circ + D \sin \omega_c t + 90^\circ$
A $\cos \omega_c t - 90^\circ + D \sin \omega_c t + 90^\circ$

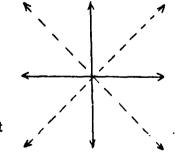
which correspond to signals

=

\$,

$$\sqrt{A^2 + D^2} / 135^{\circ}$$

$$\sqrt{A^2 + D^2} / 225^{\circ}$$
--- output



^{*}B cos $\omega_c t$ C cos $\omega_m t = (BC)/2 \cos \omega_c t + \omega_m t = A \cos \omega_c t + \omega_m t$.

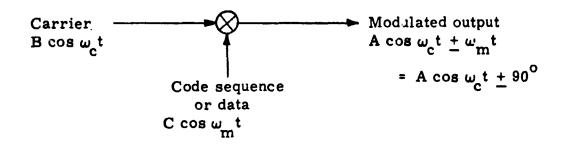


Figure 3.1-8. Biphase PSK Modulator

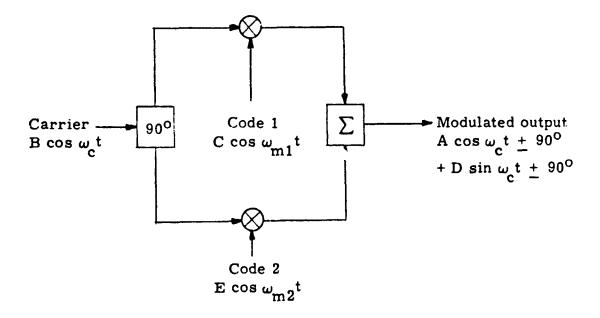


Figure 3.1-9. Quadriphase PSK Modulator

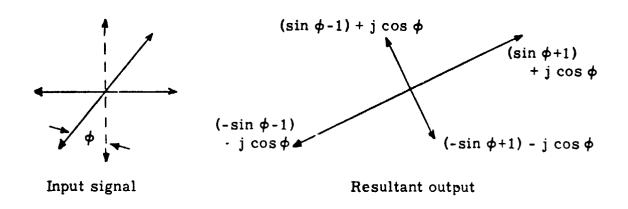
our occurrence wife within which the work the sign of the sign of

gi de a sperimentalista de

$$\sqrt{A^2 + D^2} / 45^{\circ}$$
 $\sqrt{A^2 + D^2} / 315^{\circ}$,

respectively.

Now if there is a phase shift (other than 90 degrees) between the carriers applied to the two siphase modulators contained in the QPSK modulation, then there is no longer a phase and/or amplitude balance in the output signal. Instead, the input and output signals will be



If, for example, we choose ϕ as 45 degrees, then the output signal resulting from a pair of equal amplitude input signals is

$$(\sin 45 + 1) + j \cos 45 = 1.847$$
 /22.5
 $(\sin 45 - 1) + j \cos 45 = 0.765$ /112.5
 $(\sin 45 - 1) - j \cos 45 = 1.847$ /202.5
 $(\sin 45 + 1) - j \cos 45 = 0.765$ /292.5

For this kind of signal, there is a large amplitude shift between output positions, which is highly undesirable because of the difficulty which could be engendered due to AM/PM conversion.

Here, for convenience, we have analyzed biphase and quadriphase modulators. We hasten to point out, however, that the signals existing in a quadriphase modulator are identical to those that exist in a linear channel wherein two biphase signals are processed.

AM-to-PM Conversion and Intermodulation Distortion in Spacecraft-Type Traveling Wave Tube Amplifiers

It is of interest in satellite systems, where traveling wave tube (TWT) amplifiers are employed, to be able to define the incidental phase modulation, and the intermodulation products resulting from processing one or more signals in a communication channel. This is especially true with respect to incidental phase modulation when the signals being processed contain low-deviation FM or PM signals.

Traveling wave tubes exhibit phase modulation as a function of their input signal level. This phase modulation is a result of a change in beam velocity in the TWT as input signal changes.

;;

The signals of most interest in TDRS are phase-modulated, and therefore, if they are selected properly should be constant-envelope signals. This is true, however, only in the steady-state case, and amplitude modulation does exist during the transitions from one state to another. Some signal alternatives do exhibit both steady-state amplitude and phase shift and these must be carefully considered before use, since it is possible that the phase modulation introduced by amplitude changes in the signal may be grater than the desired phase modulation.

In addition to characterization of AM/PM conversion, it is also of interest to know the degree of cross-modulation that may be expected when two signals are to be passed through a single TWT amplifier. This parameter is a measure of the self-generated noise that may be expected under the two-signal condition.

Table 3.1-1 shows typical AM/PM conversion measurements for TWT amplifiers for various frequencies and power levels. It is apparent that, depending on the tube type and its operation, AM/PM conversion may vary widely. For data considered, values covered a range from 1.5°/dB to 8.4°/dB, with a tendency for low power tubes to exhibit higher AM/PM

conversion.*

Cross-modulation in the saturated mode appears to produce thirdorder products that are approximately 8 to 12 dB below the desired signals in the two-signal case.

^{*}It is of some interest to note that a preliminary check with JPL brought a quotation of 120/dB for the tube type employed on the typical spacecraft transponder. This agrees with Hughes data.

			AM/PM Conversion	version
Source	TWT	Output Power	Saïurated	Linear
"Improved TWT's for Broad- band Jamming," Microwaves, November 1969	WJ 440	440 w (sat) (5-10 GHz)	6°/dB	6°/dB
"New Data Eases TWT Use in Communications," MSN, July 1971	STC-5215 & 52161 (Sperry)	250 w (sat) (4-8 GHz) 100 w (sat) (8-12 GHz)	2.5°-3.5°/dB	Same
RCA Technical Bulletin MWD-109, September 1969	RCA 4054	20 w (sat) (1.7-2.7 GHz)	7°-8°/dB	3.5°/dB
"Designing High Efficiency TWT's", Microwaves, July 1973	219 HX (Hughes)	28 w (sat) (7.7-8.0 GHz)	4.1°/dB	8.4°/dB
"Traveling Wave Tube for Satellite Applications," MW Journal, November 1972	Thomson- CSF	20 w (sat) (10. 95 - 11. 20, 11. 45 - 11. 7 GHz)	1.5°/dB	Same
"High Power Broadband T-W Tubes," MW Journal, April 1969	M5312 (Teledyne- MEC)	150 w (sat) (3.4 - 3.6 GHz)	2°/dB	1.6 ⁰ /dB

ï

4.

Ł

Measured AM/PM Conversion for Various Traveling Wave Tube Amplifiers (Linear 6 dB below s curation) Table 3.1-1.

3.2 Ground Receiver

The TDRSS receiver serves the function of receiving and demodulating all of the information sent down from the various user transponders on the return links. These signals are listed in section 2.2.2 of this report. The receiver description given here is for the purpose of clarifying the design, and does not represent a specified receiver, nor does it represent an "optimum" design. Figure 3.2-1 illustrates a possible receiver for the multiple signals expected, and the remainder of this section describes the operation of this receiver. Block diagrams are given to illustrate possible implementations of the subsystems of this receiver.

The receiver block diagram shown is for reception of signals in either (or both) K-band and S-band, since TDRSS is capable of and is expected to operate in both bands.

K-band signals would be amplified, split into two components, one of which would be taken for other K-band users. The second signal would be mixed with an 11.2375 GHz signal, producing a 2287.5 MHz intermediate frequency which is passed through a bandpass filter of 250 MHz BW (to pass the 225 MHz KSA signal). The signal is then amplified, mixed with a 1.975 GHz local oscillator, and output as a signal centered at 312.5 MHz. (The signal consists of a number of SMA signals separated at 6 MHz intervals.) After amplification again, the signal is the by 22 and applied to 22 separate demodulations, each of which is experienced for demodulating one downlink signal. These demodulators are not designal demodulation of all signals encountered, however. Instead, demodulation bandwidths are distributed as follows:

Demodulator	Demodulator Data Rate
1 through 8	100 bps to 10 kbps
9 through 12	10 kbps to 25 kbps
12 through 20	25 kbps to 40 kbps
21 and 22	40 kbps to 50 kbps

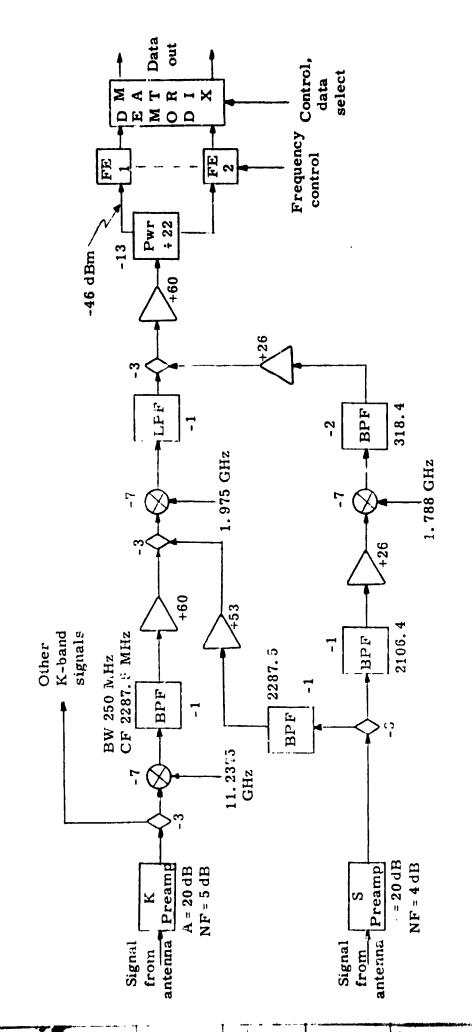


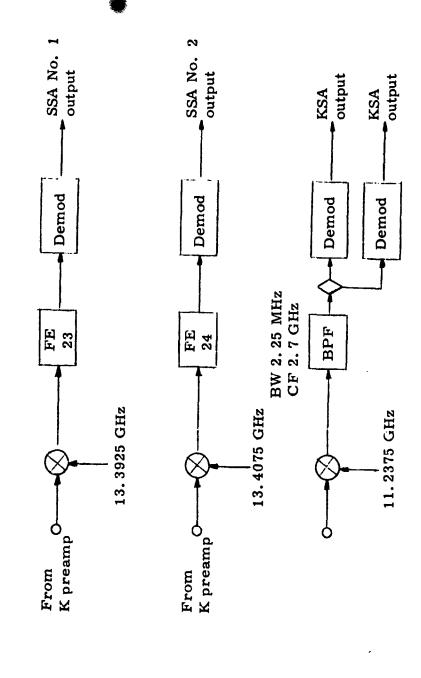
Figure 3.2-1. Block Diagram of Ground Receiver for TDRSS SMA, TT&C, and Test Signals

Each selector at the output from the ÷22 power divider would have channel selection capability which would be controllable from the TDRS conside in the ground station. A demodulator matrix would steer the signal outputs from the selectors to the right signal demodulator and then to the correct user output.

The second signal path in figure 3.2-1 is for S-band signals. Signals arriving at the S-band preamp would be amplified, split and routed to both the first IF in the receiver and to a second path that eventually reaches the ÷22 power divider. These alternate paths provide for use of the same subsystems for demodulation and signal switching, thus minimizing the ground receiver complexity. Signals at 2287.5 MHz would be routed to the second mixer and 312 MHz IF, while those at 2103.4 MHz would be routed to a mixing process which converts them to 318.4 MHz. Thus, if desired, these signals can be received simultaneously.

After power division, all input signals are applied to a set of tunable selectors (labeled FE1 through FE22) which are modified UHF communications receiver front ends. (The modifications entail broadening their frequency synthesizers by approximately 20%.) Each would be individually controllable to receive at any of the possible 42 MA and/or turn-around ranging channels. After signal selection, the signals would be routed to a demodulator and output data matrix, which allows the proper demodulator to be connected to any incoming signal frequency and the resulting data to be routed to the proper output.

Figure 3.2-2 shows the method for providing downlink frequency selection and demodulation of the single access signals, as a simplified block diagram. Figure 3.2-3 is a block diagram showing the modified UHF receiver front end and spread spectrum code correlator. Spread spectrum receivers at UHF (225 to 400 MHz) presently exist to perform this exact function. Therefore, it is suggested that a modified version of one of the existing receiver subsystems be investigated.



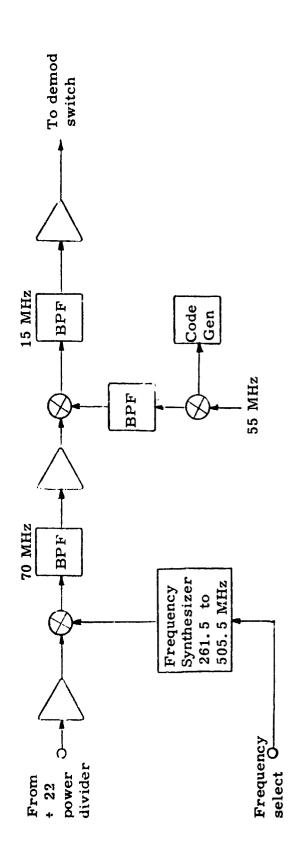
3

the standard was a second

:

()

Figure 3.2-2. Block Diagram of Ground Receiver for SA Signals



C

C

the section of the section of

Ç,

C

t.

Figure 3.2-3. Modified UHF Front End (One of 22)

The demodulator matrix is shown in block diagram form in figure 3.2-4. This matrix would route incoming signals, after frequency selection, to the proper demodulator. Twenty-two demodulators are shown, with varying data rate capabilities. This number could readily be modified or the type of demodulator could be changed to accommodate different requirements.

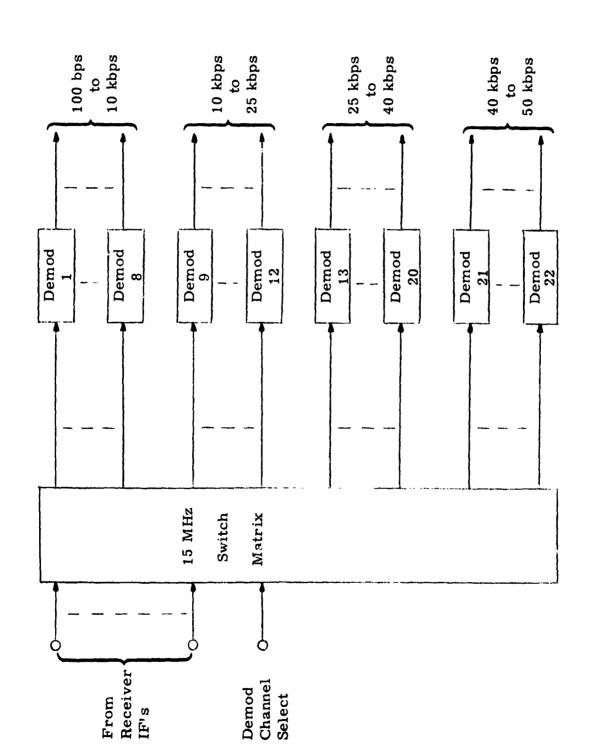


Figure 3.2-4. Demod Matrix for Ground MA Subsystem

materials of the state of

ž,

Ç.

4.0 SYNCHRONIZATION TECHNIQUES AND ANALYSIS

4.1 Introduction

One of the purposes of this investigation was to establish basic system parameters and signal design techniques for both the S-band forward link and the return links, with particular emphasis on the multiple access modes. Clearly, the synchronization requirements play a pivotal role in establishing the signal design parameters. Among the goals established at the beginning of this investigation were the desire to eliminate the requirements for a synchronization preamble, to limit the average synchronization time of the multiple access forward link to 20 seconds and on the return link to 15 seconds, and to limit the design to technologies for which there are space-qualified components. An additional consideration was the minimization of hardware complexity, in particular, in the user transponder.

In the first step to achieve the above objectives, a set of candidate techniques was selected for which a first-level analysis was performed. This analysis focused on the multiple access forward link to the user, as this is the link with the lowest threshold of performance. The acquisition techniques can be divided into two classes. The first class is termed component (composite) code acquisition. The second class is direct sequence code acquisition. Within each of these classifications, several approaches were analyzed. These include techniques such as serial search with fixed length tests and sequential tests, parallel search, and both digital and analog matched filtering techniques. From the preliminary assessment, a more detailed study was made of the techniques with the greatest likelihood of achieving the desired acquisition time performance goals and those which could be implemented with relatively low risk technology. The analysis and tradeoffs associated with the candidate techniques are detailed in the Interim Report. (1)

From these various candidate approaches, the fixed length and sequential test strategies of the direct sequence codes were selected for more detailed investigation. The details include a multiple mode acquisition strategy, doppler resolution, and the consideration of bandlimiting losses, subchannel power losses, and multiple access interference. Most of the details of this second-level analysis are given below.

C

The study concludes with an analysis of the impact of multipath on the recommended acquisition approach. Several ideas are presented for mitigating the effects of multipath. The actual multipath parameters were obtained from the Boeing Company under a subcontract to Robert Gold Associates. These multipath parameters were obtained through a simulation program with the specific TDRSS parameters as input data. The simulation model was verified by Boeing through extensive experimental testing for a satellite-to-aircraft link.

Even the more detailed analysis discussed in this section of the report is not optimized. With the use of a computer simulation, a "fine tuning" of the analysis could be performed to further reduce the mean acquisition times.

Both the delay lock chip tracking loop and carrier lock loops have lock times which contribute to the overall acquisition time. It is estimated that the code tracking and carrier pull-in and settling times are less than 1 second and hence are largely insignificant contributors the overall synchronization time. It is for this reason that the major emphasis in this study is directed toward the code acquisition analysis.

4.2 Synchronization of Receive System

4.2.1 Statement of the Problem

To demodulate the transmitted wideband noiselike signal, the receiver must have knowledge of the pseudorandom code employed during modulation. The receiver not only needs to know which particular code was used by the transmitter, but also the exact code epoch or phase. This is the synchrorization problem of the receiver.

A model of the synchronization circuitry is given in Figure 4.2-1.

The receiver removes the pseudorandom code from the received signal by cross-correlating the received signal plus noise with a reference signal. This involves first multiplying the signal plus noise with a reference signal generated by a local PN code generator. The locally generated replica is cross-correlated with the received signal plus noise and integrated in different relative phase positions until the correlation value indicates the two sequences are in phase. The number of correlations which must be performed depend upon the initial phase uncertainty of the received sequence, the length of the sequence before it repeats, the frequency offset between the local reference and the incoming signal, and the specified acquisition probabilities (i. e., probability of detection and false alarm). The acquisition time is a function of the number of correlations required.

Once the acquisition of the received signal is obtained, the codes are close enough in phase to enable the delay lock loop to begin tracking. During this time, the carrier recovery circuit or phase lock loop also begins operating and the data demodulation process can begin.

4.2.2 Outline of Candidate Acquisition Techniques

The basic direct sequence acquisition techniques considered as candidates for the TDRS receivers are summarized in Table 4.2-1.

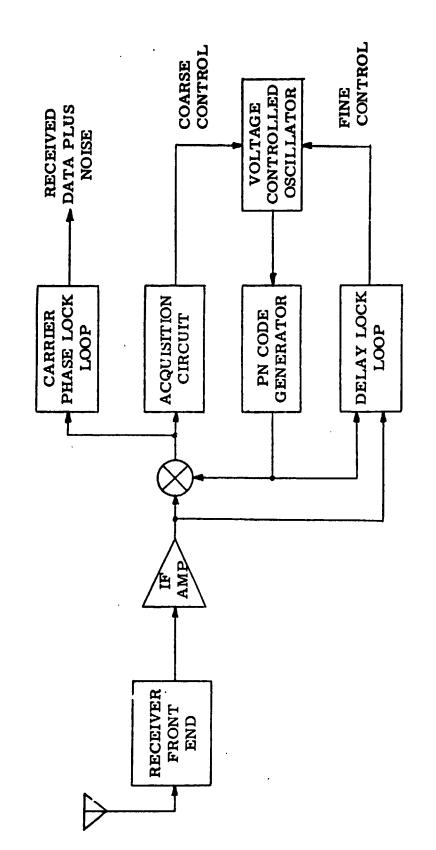


Figure 4.2-1. Pseudo Noise Synchronization Circuits

Table 4.2-1. Candidate Acquisition Techniques

Serial Search Techniques

- Component codes
- Direct sequence PN code

Parallel Search Techniques

- Component codes
- Direct sequence PN code

Matched Filter Techniques

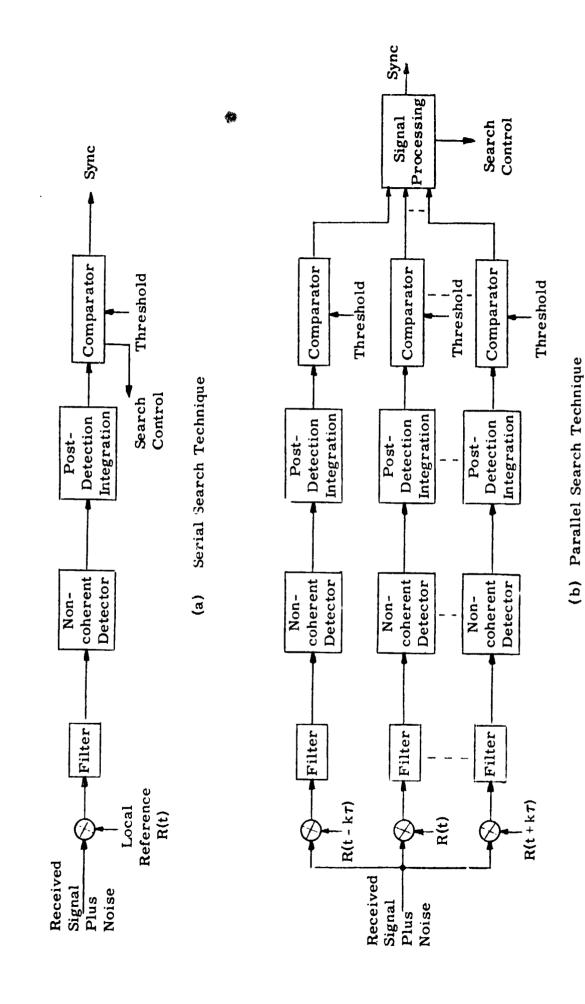
- Analog
- Digital

A simplified model for each of these techniques is given in Figure 4.2-2. In each of these techniques, some form of post-detection integration was employed. During the course of the study, each of the above techniques was analyzed and compared. A first-level summary of this comparison is given in Table 4.2-2. As a consequence of this analysis, the component code techniques were rejected because of their inherent complexity. The matched filter techniques were rejected because of their development risk. Hence, the direct sequence serial search techniques were analyzed in greater depth. The basic concepts and analyses of the techniques which were rejected for further consideration are documented in the Interim Report (1) and several of the monthly reports.

4.2.3 Basic Steps in the Acquisition Procedure

As noted above, the receiver must perform a search in time to find the correct code epoch to demodulate the transmitted signal.

There are a couple of basic assumptions for the synchronization model. One assumption is that the apriori distribution of the true code position is uniform over the entire PN code period. Another assumption made for the first-level analysis of the candidate techniques is that only



C

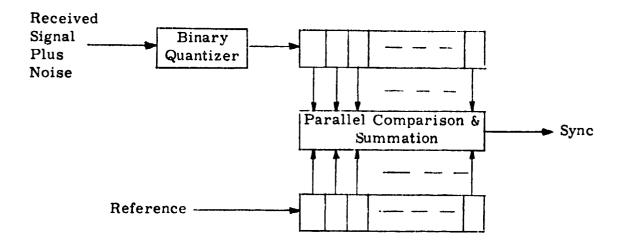
. Ъ

.

*

Figure 4.2-2. Models of Candidate Acquisition Techniques

1



(c) Matched Filter with Binary Quantization

Figure 4. 2-2. Models of Candidate Acquisition Techniques (continued)

3

Table 4.2-2. Comparative Evaluation of Candidate Acquisition Techniques

		Received			Average		
Acquisition	Acquisition Detection	Signal Level	Length of Code	Chip Rate	Acquisition Time		Develop- ment
Code Type	Technique	(dBm)	(chips)	(chips/sec)	(sec)	Complexity	Risk
3 Component	Serial search	-137.1	47, 63, 73	3 x 10 ⁶	41.5	Moderate	Low
	Parallel search	-137.1 @	47, 63, 73	3×10 ⁶	10.5	High	Low
	Parallel matched filter Coherent combining	-137.1	47, 63, 73	3×10 ⁶	0.23	High	High
	Parallel matched filter Noncoherent combining	-137.1	47, 63, 73	3 x 10 ⁶	1000	High	High
Direct Sequence PN	Digital matched filter Noncoherent combining	-137.1	1000	3 x 10 ⁶	0.13	High	Moderate
	Digital matched filter Majority detector	-137.1	8000	3×10 ⁶	0.15	High	Moderate
	Serial search 1/2 chip increments (fixed length test)	-137. 1	1000	3×10 ⁶	110	Low	Low
	Serial search 1/2 chip increments (sequential test)	-137.1	1000	3×10 ⁶	16.5	Low	Low

one code chip or time cell is the true synchronization position. This particular code position is the signal chip, and all other code positions are the noise positions. This assumption is removed in the second-level analysis of the recommended synchronization technique.

The most important parameter of the synchronization process for the present study is the average synchronization time, \overline{T}_{acq} , which is obviously to be minimized. A complete statistical description of the synchronization time would entail the calculation on higher order statistics which would allow confidence limits to be defined for the synchronization time. This is an area of future work which can come directly from the synchronization model developed below. The optimization or minimization of \overline{T}_{acq} was not performed.

The overall synchronization process can be broken down into a sequence of steps, as illustrated in Figure 4.2-3. The synchronizer dwells in a particular cell position for a fixed duration of time. T, or a variable length of time, t, in the case of the sequential test. In the fixed length test, a cell is rejected if no threshold crossing occurs after integrating for T seconds. In the sequential test, a cell is rejected if a lower threshold is crossed.

*

When cell rejection occurs, the synchronizer advances to the next time cell and repeats the above process. If there is a threshold crossing in the fixed length test and an upper threshold crossing in the sequential test, the synchronizer enters the verification mode in which it tries to arrive at a temporary decision as to whether the time cell under examination is indeed the true synchronization position. If it decides there was no signal, it resumes the search in the rext time cell. If it decides there was a signal, it enters the tracking or demodulation mode with the possibility of having made a false lock in a no-signal cell. If a false lock is recognized in the tracking mode, the loops are unlocked and the synchronizer again resumes the search.

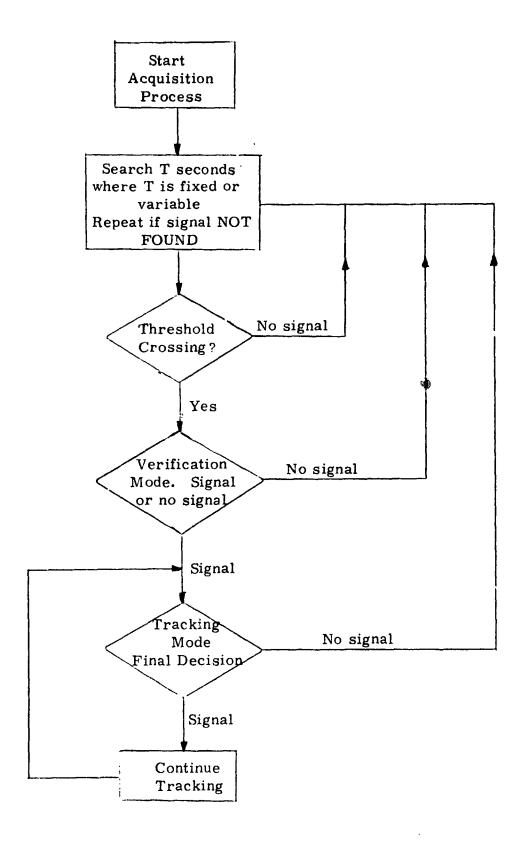


Figure 4.2-3. Overall Synchronization Process

In the initial acquisition process, there is no apriori knowledge limiting the number of cells which may contain the signal. However, during reacquisition, a different strategy should be implemented. The reacquisition search should begin from the cell position where synchronization was last detected and proceed to search from that point to its nearest neighbors and continue searching cells radiating out from that position. This technique of insuring that the cells are searched in order of their likelihood of containing the signal yields the optimum performance.

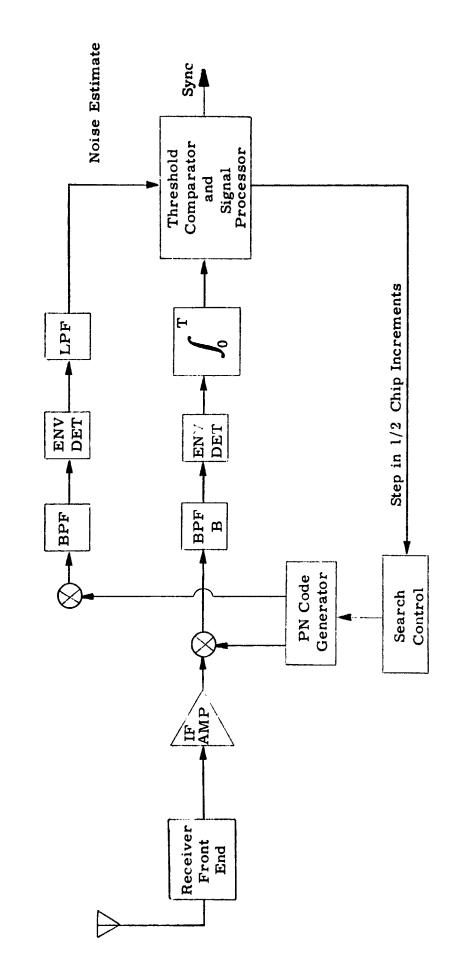
4.3 Analysis of Acquisition Techniques

4.3.1 Fixed Length Test

A block diagram of a noncoherent acquisition detector using an envelope detector and an adaptive threshold is shown in Figure 4.3-1. The search procedure of the fixed length test is relatively straightforward. The local code is correlated with the received signal for a period of time, T, after which the output is compared with a threshold and a decision is made. (The test is of fixed length because the integration period T is a constant.) If the output of the iniegrator falls below the threshold, the code phase is advanced (or retarded) by 1/2 chip time and another test is made. If the output at the sample time is above the threshold, additional tests are made according to the verification mode algorithm. A step size of 1/2 chip time is selected so that, for at least one step in the search sequence, the two codes will be within 1/4 chip of correct synchronization. Since the chip cross-correlation function is a triangular waveform, the basic effect of the synchronization error is to reduce the power spectral density of the despread signal. One can show that the power spectral density is reduced by a factor of $(1 - |\varepsilon|/T_c)^2$, where $|\varepsilon| \le \Delta$. Hence, for a maximum phase error of 1/4 cnip, the degradation is $(0.5)^2$ or -2.5 dB. Thus, the signal-to-noise ratio during acquisition is reduced by 2.5 dB.

The bandpass filter following the despreader is designed to maximize the predetection signal-to-noise ratio. It must be wide enough to accommodate the data modulation bandwidth and both the doppler and frequency uncertainty offsets.

When the local code is in synchronism with the incoming code, the output is a CW waveform which is envelope detected. If the codes are out of phase by more than one chip period, the signal-to-noise ratio is greatly reduced because the signal bandwidth will be spread at the filter input. The extent to which this occurs is investigated in Section 4.3.5.



C

ű

Functional Diagram of Acquisition Circuit for Fixed Length Test Figure 4.3-1.

1

4.3.1.1 Theoretical Analysis

The state of the s

For the fixed length test, the time required to search a given code phase is the integration time, T. Its value is determined by the requirements for the detection probability, P_D , and the false alarm probability, $P_{I^{\prime},i}$. The probability density of the noise and signal plus noise required to calculate these probabilities depends upon the BT product. For BT = 1, i.e., no post-detection filtering, the probability density functions (PDF) are Rayleigh and Rician. For BT = 10, the PDFs can be approximated very accurately by Gaussian densities for both noise only and signal plus noise. We now evaluate the signal-to-noise ratio required to provide a given P_D and P_{FA} as a function of BT.

Consider first the case for BT = 1, or no post-detection filtering. If the detector is assumed to be a perfect envelope detector, the PDF of the output noise in the absence of a signal (e.g., when the receiver is out of synchronization) is Rayleigh. Therefore, the probability of false alarm is

$$P_{FA} = e^{-Th^2/2\sigma^2}$$
 (4.3-1)

where

Th = threshold voltage

 $\sigma^2 = N_0 B = input noise power.$

The PDF of the detector output when synchronization is obtained is Rician and the probability of detection is given by

$$I_D = \int_{\text{Th}}^{\infty} \frac{V}{\sigma^2} \exp \left[\frac{-V^2 + 2S_0}{2\sigma^2} \right] I_0 \left(\frac{V \sqrt{2S_0}}{\sigma^2} \right) dV . \qquad (4.3-2)$$

This is the Marcum Q function,

$$P_{\rm D} = Q\left(\sqrt{\frac{S_0}{\sigma^2}}, \frac{Th}{\sigma}\right).$$
 (4.3-3)

For the range of $\mathbf{P}_{\mathbf{D}}$ of interest, an asymptotic expansion of the Q function yield:

$$P_{D} \approx 1 - \frac{1}{2} \operatorname{erfc} \left(\frac{\sqrt{S_{0}} - \operatorname{Th}}{\sqrt{2} \sigma} \right)$$
 (4.3-4)

where

C

erfc (x) =
$$1 - \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$$
. (4.3-5)

For large BT products, we may use the Central Limit Theorem to approximate the output PDF as Gaussian for both the in-synchronization and out-of-synchronization cases. Consider first the out-of-synchronization case, and assume that the detector is a square-law device. One can show that the mean value of the detector output signal is given by

$$M_n = 2 BTN_0$$
 (4.3-6)

and the variance is given by

$$\sigma_{\rm n}^2 = \frac{(2 \text{ BTN}_0)^2}{\text{BT}} = 4 \text{ BTN}_0^2.$$
 (4.3-7)

The false alarm probability is therefore

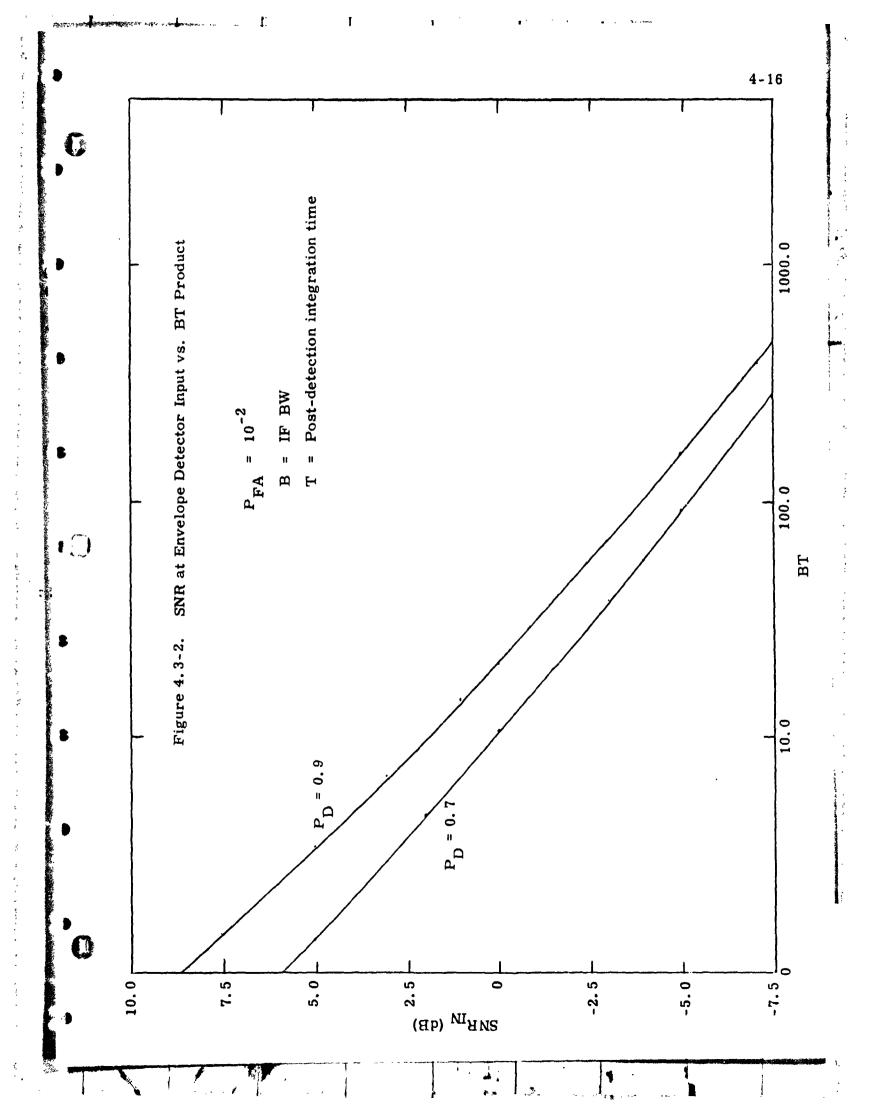
$$P_{FA} = \frac{1}{2} \left[1 - \operatorname{erf} \left(\frac{\operatorname{Th} - M_{n}}{\sqrt{2} \sigma_{n}} \right) \right]. \tag{4.3-8}$$

When the local reference is in synchronism with the received signal, then the mean and variance of the detector output can be shown to be

$$M_s = 2 BTN_0 \left[1 + \frac{S_0}{N_0 B} \right],$$
 (4.3-9)

$$\sigma_{\rm s}^2 = 4 \, {\rm BTN}_0^2 \left(1 + \frac{2 \, {\rm S}_0}{{\rm N}_0 \, {\rm B}} \right).$$
 (4. 3-10)

Thus, the probability of detection is given by



$$P_{D} = \frac{1}{2} \left[1 - \operatorname{erf} \left(\frac{\operatorname{Th} - M_{s}}{\sqrt{2} \sigma_{s}} \right) \right] . \qquad (4.3-11)$$

If we equate the thresholds, Th, in (4.3-8) and (4.3-11), we can plot the signal-to-noise ratio at the input to the detector, $S_0/N_0B = SNR_{in}$, as a function of BT. This relationship is plotted in Figure 4.3-2 for a $P_{EA} = 10^{-2}$ and two values for P_D , 0.9 and 0.7.

4.3.2 Sequential Detection Test

Introduction

Since it is important in the multiple access forward link to speed up the detection proces,, consideration was given to the sequential tests because of their optimum nature. (?) For such tests, the procedure is simply to introduce two thresholds at the detector output such that the signal in a particular cell position is declared present if one threshold is exceeded and declared absent if the other is exceeded. The length of the detection process or integration time is not fixed in advance, but is a random variable which depends upon the progress of the test. The major feature of this technique, which is referred to as sequential detection, is that it minimizes the average detection time.

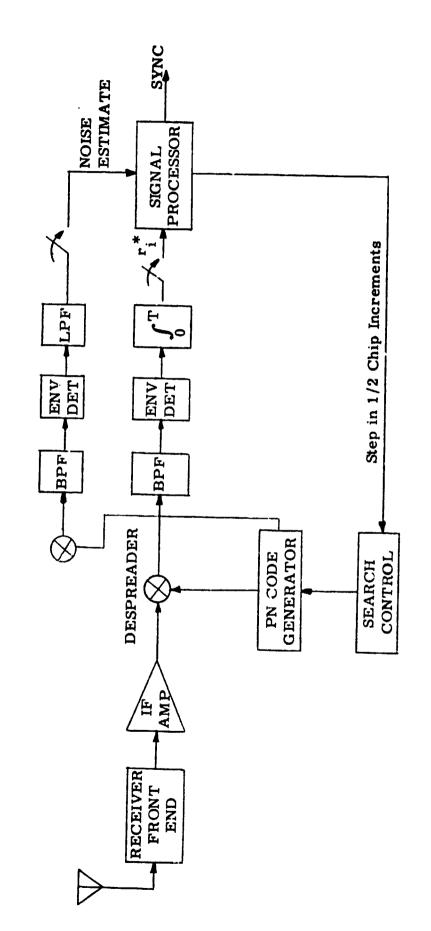
The sequential detection procedure is illustrated functionally in Figure 4.3-3.

Basic Theory

ť.

This acquisition technique is constructed to decide between two alternative hypotheses, these hypotheses being the absence or presence of a signal. However, the amplitude of the signal is usually not known a priori, so that the "signal present" hypothesis does not correspond to a unique statistical distribution of the received data. This is usually circumvented by choosing a "design" signal amplitude on the basis of which the sequential test is constructed. The probabilities of false alarm and detection are pre-chosen for this design signal amplitude.

_E



1

C

Ũ

Ċ

(

€.,

()

ſ

Ĭ

Į

Figure 4.3-3. Functional Diagram of Sequential Detection Circuit

The basic element within the signal processor is a sequential detection algorithm as developed by Wald. (3)

A sequential probability ratio test can be described as follows. Let $P_m(r|a)$ denote the conditional probability density function of the m data samples r_1, r_2, \ldots, r_m given the signal parameters a_1, a_2, \ldots, a_j and let $P_m(r|0)$ denote the probability density function of the m observed samples given that signal is absent. Then,

$$I_{\rm m} = \frac{P_{\rm m}(r|a)}{P_{\rm m}(r|0)}$$
 (4.3-12)

defines a conditional probability ratio or likelihood ratio for testing the null hypothesis H_0 against hypothesis H_1 that signal plus noise is present. Next, two positive constants A and B (B < A) are selected such that, at each stage of the test, if

$$B < \ell_m(r|a) < A$$
, (4.3-13)

the test is continued with an additional observation; if

$$\ell_{m}(r|a) \leq B$$
,

company and an arranged and arranged arranged and arranged and arranged and arranged arranged and arranged arranged and arranged arr

the test terminates with the acceptance of hypothesis \mathbf{H}_0 indicating a noise only condition. Similarly, if

$$\ell_{m}(r|a) \geq A$$
,

€.

the test terminates with the acceptance of hypothesis \mathbf{H}_1 . The sequential probability ratio test can be summarized as follows:

If
$$B < \ell_m(r|a) < A$$
, continue test.

If $BP_m(r|0) \ge P_m(r|a)$, accept H_0 . (4.3-14)

If $P_m(r|a) \ge AP_m(r|0)$, accept H_1 .

The thresholds A and B can be related to the false alarm probability α and the probability of detection $1-\beta$ by the following relationships:

$$A \approx \frac{1-\beta}{\alpha} \tag{4.3-15}$$

and

$$B \approx \frac{\beta}{1-\alpha} \tag{4.3-16}$$

If we assume that the in-phase and quadrature components of the noise are each white Gaussian random processes of zero mean and variance σ^2 , then the received signal plus noise can be represented by

$$y(t) = Ad_{i}(t) \cos \omega_{c} t + N_{c}(t) \cos \omega_{c} t - N_{s}(t) \sin \omega_{c} *, \qquad (4.3-17)$$

where A is the received signal amplitude and $d_i(t)$ is the ith data bit and can be either ± 1 .

Under in-synchronization conditions, the output of the envelope detector is given by

$$r_i(t) = \sqrt{\left[A d_i(t) + N_c(t)\right]^2 + N_s^2(t)}$$
 (4.3-18)

and, for out-of-synchronization conditions, it is given by

$$r(t) = \sqrt{N_c^2(t) + N_s^2(t)}$$
 (4.3-19)

Therefore, when the signal is present, the normalized signal plus noise envelope, \mathbf{r}_i , is governed by the Rician density function:

$$p(r_i|a) = r_i \exp \left(-\frac{r_i^2 + a^2}{2}\right) I_0(ar_i), \quad r_i > 0,$$
 (4.3-20)

where a^2 is the peak signal-to-noise ratio and is assumed to be the same for each sample value.

When the signal is absent, the normalized probability density of the envelope is given by the Rayleigh density function:

$$p(r_i|0) = r_i \exp -\left(\frac{r_i^2}{2}\right), \quad r_i > 0.$$
 (4.3-21)

A simpler technique than computing the likelihood ratio is the computation of the log likelihood ratio. If we let the logarithm of the likelihood ratio defined in equation (4.3-12) be denoted by $z_{\rm m}$, then for $a=a_{\rm d}$,

$$z_{m} = \ln \left[\frac{P(r_{i}|a_{d})}{P(r_{i}|0)} \right]$$
 (4. 3-22)

or

€,

$$z_{m} = \sum_{i=1}^{m} \ln \left[\frac{P(r_{i}|a_{d})}{P(r_{i}|0)} \right]$$
 (4.3-23)

The test procedure in terms of z_m is: (a) continue taking samples when $\ln B < z_m < \ln A$; (b) accept H_0 when $z_m \le \ln B$; and (c) accept H_1 when $z_m \ge \ln A$. Substituting (4.3.20) and (4.3-21) into (4.3-22), we arrive at the sequential test variate z_1 which is given by

$$z_i = -\frac{a_d^2}{2} + \ln I_0(a_d r_i)$$
 (4.3-24)

or substituting in (4.3-23), we get

$$z_{\rm m} = -\frac{{\rm ma_d}^2}{2} + \sum_{i=1}^{\rm m} \ln I_0(a_d r_i)$$
, (4.3-35)

where a is the design signal-to-noise ratio and is given by

$$a_d^2 = \frac{A^2}{N_0}$$
 (4. 3-26)

where $N_{\mathbf{G}}$ is the noise spectral density.

The test procedure may be simplified by adding the bias term - $(m a_d^2)/2$ to both sides of the test procedure inequalities, which can then be written as

$$\ln B + \frac{m a_d^2}{2} < \sum_{i=1}^m \ln I_0(a_d r_i) < \ln A + \frac{m a_d^2}{2}, \text{ continue test}$$

$$\sum_{i=1}^m \ln I_0(a_d r_i) \le \ln B + \frac{m a_d^2}{2}, \text{ accept } H_0$$

$$\sum_{i=1}^m \ln I_0(a_d r_i) \ge \ln A + \frac{m a_d^2}{2}, \text{ accept } H_1$$
(4.3-27)

where A and B are given by equations (4.3-15) and (4.3-16).

The sequential test concept is illustrated in Figure 4.3-4. There are two thresholds as shown above, each increasing linearly with the number of samples m. The detector outputs are also accumulated. When the accumulated sum exceeds the upper threshold, synchronization is indicated. When the accumulated sum falls below the lower threshold, it is assumed that no signal is present in that cell position. It is conceivable that the accumulated sum could drift between the two thresholds for a large amount of time; however, Wald has shown that the test is of finite duration. To avoid an excessive drift situation, it is recommended that, at some point, the test be terminated and an in-synchronization condition recognized.

The functional operation of the sequential detector is illustrated in Figure 4.3-5. In this configuration, the output of the envelope detector is integrated for time T. At the end of the integration interval, the output is sampled and quantized with an A/D converter. The quantized output is transformed by the process $\ln I_0(a_d r_i^*)$ and the variate z_i computed. This computation can be made with the use of a ROM lookup table. For a time-bandwidth product of 1, i.e., BT=1, the integration interval is the inverse of the IF bandwidth. At each sample time, the quantized variate z_i^* is added to the previous sum and compared with two thresholds $Th_1(m)$ and $Th_2(m)$. If the accumulated sum falls below $Th_2(m)$, the signal is not assumed to be present in that cell position and

(;

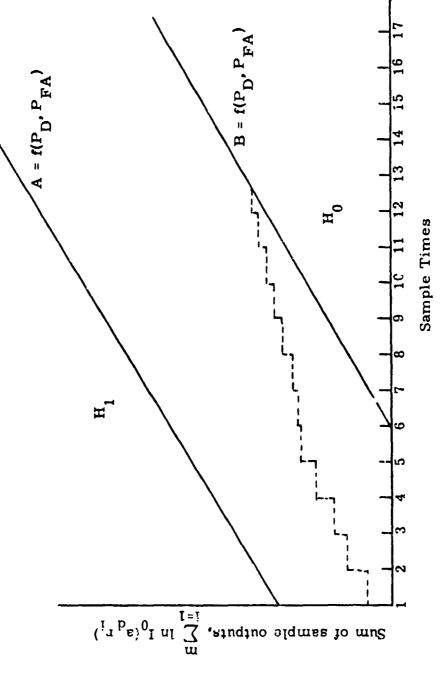
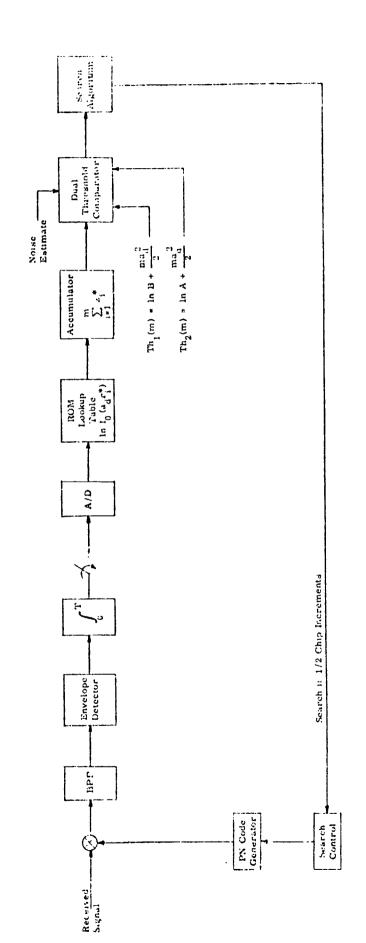


ILLUSTRATION OF SEQUENTIAL SEARCH STRATEGY Figure 4.3-4.

「一般のできることが、これのできることでは、これできることできることできます。 これのこと

45



.1.

Functional Diagram of Sequential Acquisition Detector Figure 4.3-5.

the search control moves the local PN code one half chip time. If the accumulated value exceeds Th₁(m), signal presence is assumed and is then verified. At this point, the accumulator is reset to zero and the thresholds are reset to their initial conditions. Once signal presence is established, the system falls into a tracking mode, at which time, the delay lock and carrier tracking loops are operating.

Operating Characteristic Function (OCF)

One of the relationships of interest in the sequential search test is the so-called operating characteristic function (OCF), which gives the detection probabilities for signals having amplitudes differing from the design amplitude. The OCF denoted by L(a) is required for the evaluation of the average sample number (ASN). L(a) is the conditional probability of accepting hypothesis H₀ at the end of the test or the probability of a miss. From the definition

$$L(0) = 1 - \alpha$$
 (4.3-28)
 $L(a) = \beta(a)$

and

$$L(a) = \frac{A^{\left[1 - 2(a/a_d)^2\right]} - 1}{A^{\left[1 - 2(a/a_d)^2\right]} - B^{\left[1 - 2(a/a_d)^2\right]}}$$
(4.3-29)

where $A = \frac{1-\beta}{\alpha}$ and $B = \frac{\beta}{1-\alpha}$, and α is the probability of false alarm, β is the probability of a missed signal, a^2 is the actual received signal-to-noise ratio, and a_d^2 is the design signal-to-noise ratio.

The OCF can be plotted as is shown in Figure 4.3-6.

Average Sample Number (ASN)

We now let m denote the number of observations or samples required by the test and let $E_a(m)$ be the expected value of m when a is the true value of the signal-to-noise ratio. If we let $\eta = E_a(m)$ denote the average number of observations (ASN) required to terminate the test,

The second second second second second second

then for independent observations, the average sample number (ASN) is given by

$$\eta = \frac{L(a) \ln B + [1 - L(a)] \ln A}{E(z|a)}$$
 (4.3-30)

where

$$E(z|a) = -\frac{a_{d}^{4}}{8} + \frac{a^{2}a_{d}^{2}}{4}. \qquad (4.3-31)$$

Substituting (4.3-31) into (4.3-30), we get

$$= \frac{L(a) \ln B + [1 - L(a)] \ln A}{-\frac{a_d^4}{4} \left[\frac{1}{2} - \left(\frac{a}{a_d}\right)^2\right]}.$$
 (4.3-32)

Hence, the ASN is inversely proportional to the square of the design (peak) signal-to-noise ratio.

Average Time to Threshold

At threshold, the peak signal-to-noise ratio is given by

$$a_d^2 = \frac{2C'}{N_0 B_W}$$
 (4.3-33)

where $2C'/N_0B_W$ is the peak effective design signal-to-noise ratio in the IF filter of bandwidth B_W .

If the output of the envelope detector is sampled at a rate 1/T, then the mean time to decision can be written as

$$T_{d} = \eta T$$

$$T \frac{L(a) \ln B + [1 - L(a)] \ln A}{-(\frac{C'}{N_0 B_W})_{d}^{2} [\frac{1}{2} - k^{2}]}, \qquad (4.3-34)$$

where $k = a/a_d$.

The mean time to cell dismissal, T_b , is the case where a = 0 in equation (4.3-34). For this case, $L(0) = 1 - \alpha$, and (4.3-34) reduces to

$$T_{b} = \frac{2T \left[(1 - \alpha) \ln B + \alpha \ln A \right]}{-\left(\frac{C'}{N_{0}B_{W}} \right)_{d}^{2}}.$$
 (4.3-35)

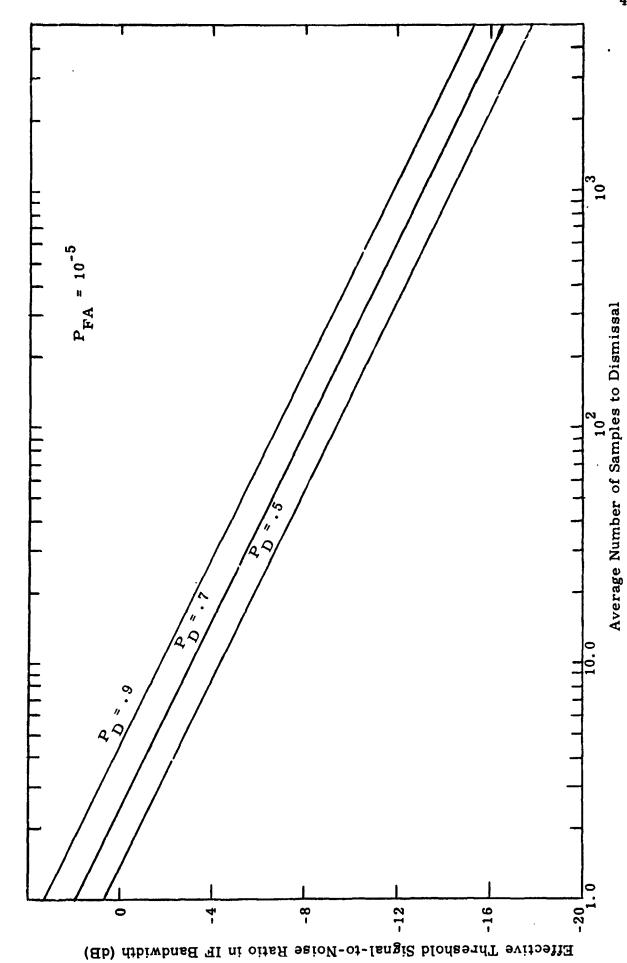
The relationship T_b/T versus C'/N_0B_w is plotted in Figure 4.3-7 for several values of the detection probability, $P_D = 1 - \beta$. The curves are almost insensitive to the false alarm probability.

For the low false alarm probabilities which are of interest in the TDRSS application, the greatest reduction in expected dwell time over the fixed length test occurs when noise alone is present or one is in an out-of-synchronization condition. The expected dwell or integration time is only slightly less than that of the fixed length test in the insynchronization position. Therefore, the benefits of using the sequential detection scheme are greatest when a time uncertainty exists over a large number of chip positions.

4.3.3 Direct Sequence Acquisition Using Dual Mode Detection

Introduction

The purpose of this section is to examine more completely the acquisition technique discussed in sections 4.3.1 and 4.3.2. A more sophisticated model of the acquisition technique will be considered. The model as illustrated in Figure 4.2-3 has both acquisition and verification tests prior to entering the tracking mode. The basic strategy to be employed is to lower the thresholds during acquisition, which thereby increases the miss and false alarm probabilities. When a signal is indicated, the verification mode is entered and a more careful examination of the cell is made (i.e., increased post-detection integration time corresponding to an increase in the threshold levels). The effect is that the



Average Sample Number Versus Threshold Signal-to-Noise Ratio Figure 4. 3-7.

こうこう かいい くきこう とうこう とう かん きゅうこう まんしょう そうじゅう そうじゅう ないない かんない ないない まっかい まってん 水温 はなれば はなれない なない

local reference may very likely cycle through the uncertainty region, which for initial acquisition is all the cells in the PN sequence, several times before locking onto the desired signal. Once the verification state is entered, the delay lock loop begins operating. Failure to confirm the signal presence during verification causes the code search to continue and the delay lock loop is reset. However, once synchronization is confirmed, the Costas loop sweep begins and the tracking mode is entered.

[_

In the tracking mode, a third set of threshold values are established to insure a very low false alarm rate and miss probability. The delay lock loop bandwidth is gradually narrowed. The thresholds are also set so that it is more difficult to drop out of the tracking mode than either of the other modes. This is to insure that rapid signal fades will not cause the receiver to drop out of lock.

The dual mode synchronizer has greater flexibility than the single mode technique. The thresholds can be optimized and yield acquisition times which, in many cases, are lower than the single mode technique. In addition, the thresholds can be optimized to minimize the probability of locking onto multipath signals.

The optimization of the parameters was not performed during this study. However, an attempt was made to yield results which are considered to be reasonably close to the optimum parameter values.

Theoretical Analysis

When using the sequential synchronization algorithm defined in section 4.3.2, the average number of samples required at the output of the envelope detector for dismissal can be calculated from equation (4.3-34) and is given by

$$\eta = \frac{8 \left[L(a) \ln B + \left(1 - L(a) \right) \ln A \right]}{- \left(\frac{2C'}{N_0 B} \right)_d^2}, \qquad (4.3-36)$$

where $2C'/N_0B$ is the peak effective design signal-to-noise ratio in the IF filter of bandwidth B at threshold. If the output of the envelope detector is integrated for time T and sampled, then the mean time to dismissal can be written as

$$T_b = \eta T = \frac{2T \left[L(a) \ln B + \left(1 - L(a)\right) \ln A\right]}{-\left(\frac{C'}{N_0 B}\right)_d^2}.$$
 (4.3-37)

If the length of the code sequence is N chips and the local code reference is stepped in one-half chip increments referred to as cells, then the signal is likely to be in any one of the 2N cell positions. In actuality, it can occur in two and, in some cases, even three half chip positions. This is due to the spread of the delay lock characteristics. The fact that the signal can occur in two cell positions will be accounted for later on in the analysis. The possibility that some of the signal is in a third cell position will be ignored.

We define P(i) as the probability that exactly i steps (i=1,2,...,2N) are required to reach the signal. Assume each step requires T_{α} seconds on the average. When N is large, then for all practical purposes, $T_{\alpha} = T_{b}$. The average time of first arrival is then

$$T_1 = \sum_{i=1}^{2N} i T_{\alpha} P(i) = \frac{T_{\alpha}}{2N} \sum_{i=1}^{2N} i = N T_{\alpha}$$
 (4.3-38)

since P(i) = 1/2N.

ŧ,

As above, we define α as the probability of a false acceptance and β as the probability of a false dismissal. Then the probability that the signal is dismissed upon its first arrival but detected upon its first repeat trial is $\beta(1-\beta)$. The probability that the signal will be initially detected on the jth repeat scan is

There is no set by agreement they agree the second

$$P(j) = \beta^{j} (1 - \beta) . (4.3-39)$$

The average time required for a repeat scan is $2N\ T_{\alpha}$. Therefore, the average time lost due to a false dismissal is

$$T_{2} = \sum_{j=1}^{\infty} j(2N) T_{\alpha} P(j)$$

$$= 2N T_{\alpha} (1 - \beta) \sum_{j=1}^{\infty} j \beta^{j}$$

$$= 2N T_{\alpha} \frac{\beta}{1 - \beta}$$
(4. 3-40)

Another basic assumption in this analysis is that the signals are assumed to remain uncorrelated in a single cell position throughout the search process. The time required for synchronization, T_{acq} , is then the sum of T_1 , the time required to arrive at the correlated cell for the first time, plus T_2 , the time lost due to false dismissals, plus T_3 , the time required to correctly accept the correlated cell after arriving at it. In all practical cases, T_3 will be negligible compared to T_1 and T_2 for large values of N and will be neglected in the subsequent analysis.

The total average synchronization time, ignoring T_3 , is

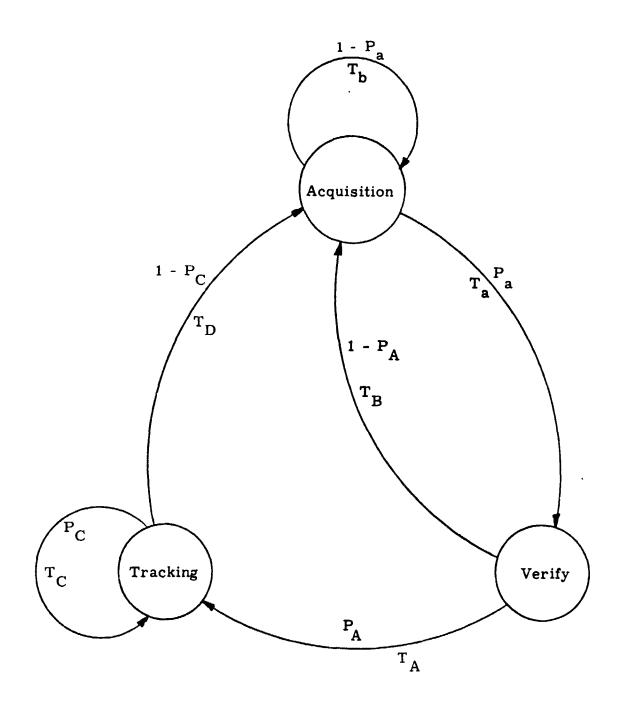
$$T_{\text{acq}} = T_1 + T_2 = N T_{\alpha} + 2N T_{\alpha} \left(\frac{\beta}{1-\beta}\right)$$
$$= N T_{\alpha} \left(\frac{1+\beta}{1-\beta}\right). \tag{4.3-41}$$

In Figure 4.3-8, the state diagram of the dismissal process of the two-step synchronizer with a tracking loop is illustrated. We define these states as follows:

State 1 Acquisition State

State 2 Verification State

State 3 Tracking State.



 \mathbf{c}

[*

Figure 4.3-8. State Diagram of the Dual Mode Synchronizer

Let us now define the following parameters:

T_a = average time required to perform an acquisition test leading to an accept decision

Tb = average time required to perform an acquisition test leading to a dismiss decisic.

T_A = average time to perform verification test leading to an accept decision

T_B = average time to perform verification test leading to a dismiss decision

T_C = average time required for tracking loop to perform a test leading to an accept decision

T_D = average time required for tracking loop to perform a test leading to a dismiss decision

P = probability of false acceptance by acquisition test

P_b = probability of false dismissal by acquisition test

 P_{Δ} = probability of false acceptance by verification test

 P_{B} = probability of false dismissal by verification test

P_C = probability of false acceptance by tracking loop

PD = probability of false dismissal by tracking loop

2N - number of cells to be tested.

In Figure 4.3-8, the transition probabilities are shown with the times required to perform the tests leading to a new state. If T_i is the time required for rejection by the ith path and $P(T_i)$ is the probability of traversing that path, then the average dismissal time is given by

$$T = \sum_{i} T_{i} P(T_{i})$$
 (4.3-42)

By inspection, the first few terms are

$$T_{\alpha} = T_{b}(1 - P_{a}) + (T_{a} + T_{B}) P_{a}(1 - P_{A})$$

$$+ (T_{a} + T_{A} + T_{D}) P_{a} P_{A}(1 - P_{C})$$

$$+ (T_{a} + T_{A} + T_{C} + T_{D}) P_{a} P_{A} P_{C}(1 - P_{C})$$

$$+ (T_{a} + T_{A} + 2T_{C} + T_{D}) P_{a} P_{A} P_{C}^{2}(1 - P_{C})$$

$$+ \dots \qquad (4.3-43)$$

This leads to the general expression

$$T_{\alpha} = T_{b}(1 - P_{a}) + (T_{a} + T_{B})P_{a}(1 - P_{A})$$

$$+ P_{a}P_{A}(1 - P_{C}) \sum_{j=0}^{\infty} (T_{a} + T_{A}^{+j}T_{C} + T_{D})P_{C}^{j}. \qquad (4.3-46)$$

which can be summed to yield

$$T_{\alpha} = T_{b}(1 - P_{a}) + (T_{a} + T_{B})P_{a}(1 - P_{A})$$

$$+ P_{a}P_{A}(1 - P_{C}) \left[\frac{(T_{a} + T_{A} + T_{D})}{1 - P_{C}} + \frac{T_{C}P_{C}}{(1 - P_{C})^{2}} \right]$$
(4. 3-45)

This can be simplified to yield for the dual mode synchronizer

$$T_{\alpha} = T_{b} + P_{a} (T_{a} - T_{b} + T_{B})$$

$$+ P_{a} P_{A} \left(T_{A} - T_{B} + T_{D} + \frac{P_{C} T_{C}}{1 - P_{C}} \right). \tag{4.3-46};$$

The remaining parameter needed to specify the average synchronization time is β , where for the dual mode synchronization

$$\beta = P_b + (1 - P_b) P_B + (1 - P_b)(1 - P_B) P_D$$
 (4.3-47)

4.3.4 Code Doppler Analysis

Because of the frequency error between the local reference and the received code, the local code will slide past the incoming signal over the entire integration interval. The code doppler error is given by

$$d_{c} = \frac{\Delta f R_{c}}{f_{c}}, \qquad (44.3-48)$$

where

 f_{c} is the rf carrier frequency

R is the chip rate

 Δf is the frequency uncertainty.

As an example, in the multiple access forward link,

$$f_c = 2.1064 \times 10^9 \text{ Hz}$$

 $R_c = 3.0778 \times 10^6 \text{ chips/sec}$

 $\Delta f = \pm 3 \text{ kHz}$.

Substituting these parameters in equation (4.3-48), we get

$$d_c = \pm 4.38 \text{ chips/sec}$$

as the code drift rate between the local code and the received signal.

During the ith step, the phase change is

$$\Delta \phi_i = d_c T_i - \frac{\Delta T_c}{T_c} , \qquad (4.3-49)$$

where $\Delta T_c/T_c$ is the coarse step size, and we assume $\Delta T_c/T_c=0.5$; that is, we step in one-half chip increments. Therefore, the total change in phase difference between two codes expressed in chips after N steps is

$$\Delta \phi = \sum_{i=1}^{N} \Delta \phi_i = d_c \sum_{i=1}^{N} T_i - 0.5N$$
 (4.3-50)

Since N is large, the summation can be expressed in terms of the average dwell time, T_d , where

$$T_d = \frac{1}{N} \sum_{i=1}^{N} T_i$$
 (4.3-51)

Clearly, T, is mode dependent. Therefore,

A server and

$$\Delta \phi = d_c N T_d - 0.5N = N(d_c T_d - 0.5)$$
.

Hence, the average step size in the worst case direction is

$$0.5 - d_c T_d$$
 (4.3-5.2)

On the average, the code drift will aid in the performance, as well as degrade the performance. For the purposes of this analysis, we will assume the worst case condition.

Summary of Acquisition Time Equations

Fixed Length Test - Noncoherent Detection

For the dual mode fixed length test, the mean (average) acquisition time is given by the following equation:

$$\overline{T}_{acq} = N \left[\frac{T}{|1-2 d_c T|} + T_{\beta} \right] \left(\frac{1-\beta}{1-\beta} \right)$$
 (4.3-53)

T is the post-detection integration time or dwell time $T_{\beta} = T_{\alpha} - T_{b}$, where

 T_{α} is given by equation (4.3-46)

Also, β is given by equation (4.3-47) and N is the number of chips to be searched in the PN sequence.

The degradation due to code doppler is only assumed to occur during initial acquisition. We assume that the code tracking loop is operating during the verification mode.

Sequential Test - Single Mode

Noncoherent Detection

$$\overline{T}_{acq} = \frac{NT_b}{|1-2d_cT|}$$
 (4.3-54)

Ί.

where

$$T_{b} = \frac{2 T \left[L(a) \ln B + (1 - L(a)) \ln A \right]}{-\left(\frac{C'}{N_{0}B}\right)_{d}^{2}}$$
(4.3-55)

Coherent Detection

$$\overline{T}_{acq} = \frac{NT_b}{|1-2d_cT|}$$
 (4.3-56)

where

$$T_{b} = \frac{T\left[L(a) \ln B + (1 - L(a)) \ln A\right]}{-2\left(\frac{C'}{N_{0}B}\right)_{c!}}$$
(4.3-57)

Sequential Test - Dual Mode

Noncoherent Detection

$$\overline{T}_{acq} = N \left[\frac{T_b}{\left| 1 - 2 d_c T \right|} + T_{\beta} \right] \left(\frac{1 + \beta}{1 - \beta} \right)$$
 (4.3-58)

where T_{β} and β are defined above and T_{b} is given by equation (4.3-55).

Coherent Detection

Coherent detection is the same as in (4.3-58), with T_b given by equation (4.3-57).

4.3.6 Interfering Signal Acquisition Analysis

Introduction

The primary objective of this analysis is to establish the acquisition parameters of the S-band multiple access return link. The baseline system model is developed; this is followed by a discussion of the receiver model. The analysis is then directed to determining the desired signal power, the interfering signal power and the total noise power at the input to the envelope detector. The effective signal-to-noise ratio at the detector input is determined for both the desired signal in its synchronized condition and, similarly, the interfering signal when it is synchronized to a cross-correlation peak.

System Model

The model for the TDRSS S-band multiple access return link is shown in figure 4.3-9. For the purposes of this analysis, the desired signal-to-noise ratio is

SNR =
$$\frac{S_0}{\sum_{i} I_i + N}$$
, (4.3-59)

where S₀ is the desired signal power

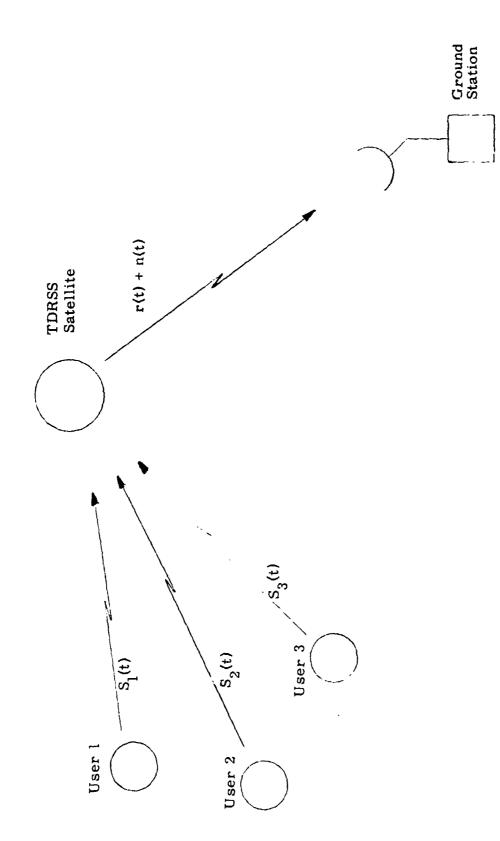
I_i is the ith interfering power level

N is the receiver noise power.

One of the objectives of this study is to compute for the above system model the probability of acquiring one of the interfering signals rather than the desired signal.

Receiver Model

The model of the acquisition detector is shown in figure 4.3-10. The input r(t) is given by



()

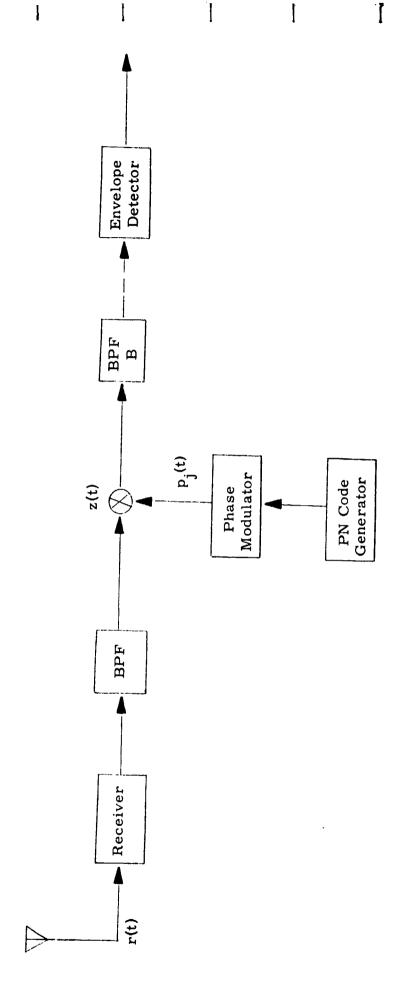
ű

€.

٤.

 \mathbb{C}

Figure 4, 3-9 Model of TDRSS Aultiple Access Return Link



ŧ.

Model of Receiver Front End and Despreader

Figure 4.3-10

こうしょうけん いっぱい いちょう かんしょう しゅうじゅう かいかい かいかい かいかい かいかい かいかい かいかい かんない からない かんない かんない かんない かんない かんない かんしょう かんしょう かんしょう かんしょう かんしょう かんしょう かんしょう かんしょう しゅうしゅう しゅうしゅう しゅうしゅう しゅうしゅう

$$r(t) = \sum_{i=1}^{3} \sqrt{2 S_i} \quad a_i(t) X_i(t) \sin[\omega_c t + \theta_i] + n(t)$$
 (4.3-60)

where $old X_i^{}$ is the pseudorandom PN code of the i $^{ ext{th}}$ signal

- a, is the data modulation of the ith signal
- $\boldsymbol{\theta}_i$ is the relative phase shift of the $i^{\mbox{th}}$ transmitter
- n(t) is the thermal noise
- S, is the received power of the ith signal.

The local reference is given by p(t) where

$$p(t) = 2 X_1(t) \sin(\omega_1 t + \theta_1)$$
 (4.3-61)

and

$$\omega_{\rm IF} = \omega_{\rm c} - \omega_{\rm l}$$
.

For the purposes of this analysis, it will be assumed that the local reference is in chip synchronism with the signal transmitted by User 2. We will assume that it is not in chip synchronization with the desired signal $S_1(t)$ and the other interfering signal $S_3(t)$. Clearly, this is the worst-case condition since we maximize the received signal level of $S_2(t)$ and minimize the impact of $S_1(t)$ and $S_3(t)$ which become noise sources. We will also assume that $S_1(t)$ and $\tilde{S}_3(t)$ are both uncorrelated with the local reference.

SIGNAL-TO-NOISE RATIO ANALYSIS

Based on the model developed above, we will compute the probability of acquiring the 50 kbps data rate signal, $S_2(t)$, when the local reference is set to lock onto $S_1(t)$ or the 1 kbps data rate signal. This acquisition probability will be computed for three code sequence lengths and assumes the PN codes for each of the three signals are of equal length and are balanced Gold codes. The cross-correlation code spectrum for the three code lengths assumed in this investigation are summarized in table 4.3-1.

Table 4.3-1.	Cross-Correlation	Spectrum
--------------	-------------------	----------

n = 1	ength of code			
k	$n = 2^k - 1$		Spectrum	annanna dell'illico co confer dir al representa dell'antiqui dell'antiqui dell'antiqui dell'antiqui dell'antiqui
11	2,047	63 (528)	-1 (1023)	-65 (496)
13	3,191	127 (2080)	- 1 (4095)	-129 (2016)
15	32,767	255 (8128)	-1 (16383)	-257 (8256)

The value in parentheses associated with the cross-correlation quantity denotes the number of chip positions containing the particular cross-correlation value. However, before we compute the detection probabilities, we will determine the IF signal-to noise ratio.

Signal Power

If the signal power of the received signal $S_2(t)$ is given by S_2 , then the spectra at the output of the despreader is given by

$$S_{z}(\omega) = S_{2} T_{2} \rho_{1,2} \left[\frac{\sin(\omega - \omega_{IF}) T_{2}/2}{(\omega - \omega_{IF}) T_{2}/2} \right]^{2}$$
 (4.3-62)

where T_2 is the data band interval and $1/T_2 = 50$ kbps. The parameter $\rho_{1,2}$ is the cross-correlation coefficient between the local reference, S_1 (t) with code i, and the signal S_2 (t) with code 2. For the peak sidelobe condition,

$$\rho_{1,2} = \frac{(65)^2}{2047}. \tag{4.3-63}$$

The signal power at the output of the bandpass filter is given by

$$S_0 = \int_{-\infty}^{\infty} S_z(f) |H(f)|^2 df$$
 (4.3-64)

201

where H(f) is the frequency response of the bandpass filter preceding the envelope detector. If we assume that the filter has at least four poles, then an ideal filter approximation can be made so that

$$S_0 = \frac{1}{2\pi} \int_{\omega_{IF}}^{\omega_{IF}} \int_{B/2}^{+B/2} S_z(\omega) d\omega$$
 (4.3-65)

which can be written as

$$S_0 = \frac{S_2}{\pi} \rho_{1,2} \int_{-\pi BT_2/2}^{\pi BT_2/2} (\sin x/x)^2 dx.$$
 (4.3-66)

The bandwidth of the bandpass filter is assumed to be 5 kHz since the data rate is 1 kbps and the total frequency uncertainty is \pm 1.5 kHz. Hence,

$$S_0 = \frac{S_2 \rho_{1,2}}{\pi} \int_{-0.157}^{0.157} \frac{\sin^2 x}{x^2} dx \qquad (4.3-67)$$

$$S_0 = \frac{S_2 - \rho_{1,2}}{\pi} (0.157) (2)$$

$$S_0 = (0.1) S_2 \rho_{1.2}$$
 (4.3-68)

Interfering Signals as Noise

If we define signals $S_1(t)$ and $S_3(t)$ as interfering signals, where

$$S_1(t) = \sqrt{2 S_1} a_1(t) X_1(t) \sin \left[\omega_0 t + \theta_1\right]$$
 (4.3-69)

and

$$S_3(t) = \sqrt{2} S_3 a_3(t) X_3(t) \sin [\omega_c t + \theta_3]$$
, (4.3-70)

then at the output of the despreader, the cross-correlation between the local reference p(t) and $S_i(t)$ is given by

$$R_z(\tau) = \frac{1}{2T} \int_{-T}^{T} X_i(t) X_i(t+\tau) p(t) p(t+\tau) dt, i = 1, 3. (4.3-71)$$

Since the signals $S_1(t)$ and $S_3(t)$ are assumed to be uncorrelated with p(t),

$$R_{z}(\tau) = R_{X_{i}}(\tau) R_{p}(\tau)$$
 (4.3-72)

or
$$S_{z}'(\omega) = S_{X_{i}}(\omega) * S_{p}(\omega)$$
. (4.3-73)

Now,
$$R_{X_{i}}(\tau) = S_{i}\left\{1 - \left|\frac{\tau}{T_{c}}\right|\right\} \cos \omega_{c} \tau, \quad 0 < |\tau| < T_{c}$$

$$R_{p}(\tau) = 2\left\{1 - \left|\frac{\tau}{T_{c}}\right|\right\} \cos \omega_{\tilde{1}} \tau . \qquad (4.3-74)$$

Therefore,

$$R_{z}(\tau) = 2 S_{i} \left\{ 1 - 2 \left| \frac{\tau}{T_{c}} \right| + \left| \frac{\tau}{T_{c}} \right|^{2} \right\} \cos \omega_{c} \tau \quad \cos \omega_{1} \tau$$

$$0 \le |\tau| < T_{c}$$

$$(4.3-75)$$

$$|\tau| > T_{c}$$

1.

where T_c is the chip period.

If we take the Fourier transform in the neighborhood of ω_{IF} , we get (where $\omega_{IF} = \omega_{c} - \omega_{1}$),

$$S_{z}'(\omega) = \frac{2 S_{i}}{(\omega - \omega_{IF})^{2} T_{c}} \left[1 - \frac{\sin(\omega - \omega_{IF}) T_{c}}{(\omega - \omega_{IF}) T_{c}}\right]. \quad (4.3-76)$$

The resulting interfering signal power at the output of the IF bandpass filter is given by an equation similar to 4.3-65; that is

$$I_{i} = \frac{1}{2\pi} \int_{\omega_{IF}}^{\omega_{IF}} \frac{B/2}{B/2} S_{z}'(\omega) d\omega$$
 (4.3-77)

Clearly, the maximum occurs in the vicinity of $\omega_{\rm IF} = \omega_{\rm c} - \omega_{\rm l}$. Since B $<< 1/T_{\rm c}$, substituting 4.3-76 into 4.3-77, we get

$$I_i = \frac{2}{3} S_i T_c B.$$
 (4.3-78)

Noise Density Reduction

We will attempt in this section to compute the spreading effect of the receiver noise due to the reference signal p(t). Since the noise is uncorrelated with p(t), the cross-correlation function of the noise with the PN signal is given by

$$R_{z}(\tau) = R_{n}(\tau) R_{p}(\tau).$$
 (4.3-79)

7

The spectral density at the despreader output is

$$S_1(f) = \int_{-\infty}^{\infty} R_n(\tau) R_p(\tau) e^{-j\omega\tau} d\tau$$
 (4.3-80)

Since the bandwidth of the received signal is much greater than the bandwidth of the IF filter, the effective spectral height into the IF filter is given by S(0) where

$$S_1(0) = \int_{-\infty}^{\infty} R_n(\tau) R_p(\tau) d\tau$$
. (4.3-81)

We can then write the spectral response of the output of the IF filter as

$$S_{n}(0) = \frac{1}{2\pi} \int_{-\infty}^{\infty} N_{0} \left| H(\omega) \right|^{2} T_{c} \left(\frac{\sin (\omega - \omega_{IF}) T_{c}}{(\omega - \omega_{IF}) T_{c}} \right)^{2} d\omega . \tag{4.3-82}$$

Using the same argument for $|H(f)|^2$ as given above, we can write

$$S_{n}(0) = \frac{N_{0}}{\pi} \int_{-\pi}^{\pi B_{1}} \frac{T_{c}/2}{T_{c}/2} \left(\frac{\sin x}{x}\right)^{2} dx. \qquad (4.3-83)$$

Therefore, $S_n(0) \approx N_0$

and
$$N = N_0 B$$
. (4.3-84)

Effective Undesired Signal-to-Noise Ratio

Substituting equations 4.3-68, 4.3-78 and 4.3-84 into 4.3-59, we get the signal-to-noise ratio at the output of the bandpass filter:

$$SNR_2 = \frac{(0.1) S_2 \rho_{1,2}}{\sum_{i=1,3} \frac{2}{3} S_i T_c B + N_0 B T_c},$$
 (4.3-85)

which can be rewritten as

$$SNR_{2} = \frac{0.1 \rho_{1,2}}{\sum_{i=1,3} \frac{2}{3} \left(\frac{S_{i}}{S_{2}}\right) T_{c} B + \frac{N_{0}B}{S_{2}}}$$
(4.3-86)

Effective Desired Signal-to-Noise Ratio

The desired signal-to-noise ratio about which the design parameters of the acquisition technique are established is summarized below. With 0 dB design margin, $C/N_0 = 39.9 \text{ dB-Hz}$.

IF filter bandwidth - 5 kHz	37.0 dB
PN filter loss	0.9 dB
One-half chip offset loss	2.5 dB
Total losses	40.4 dB

Therefore, effective $SNR_1 = C/N_0 - 40.4 dB$

$$SNR_1 = -0.5 \, dB$$
.

Now, based on the link analysis given, in section 1.3 for the multiple access return link, the signal-to-noise ratio at the receiver for $S_2(t)$ is

$$\frac{C_2}{N_0}$$
 = 33.1 + EIRP - System losses (dB-Hz).

If we allow 5 dB for system losses, then with an EIRP of 31.8 dBW, we get

$$\frac{C}{N_0} = 59.9 \text{ dB-Hz.}$$

Now,

$$S_3/S_2 = 1$$

and

$$S_2/N_0B = 59.9 dB-Hz - 10 log 5000$$

= 22.9 dB.

Therefore,

$$S_1/S_2 = -23.4 dB.$$

Substituting these values into 4.3-86, we get

SNR₂ =
$$\frac{0.1 (1 \times 10^{-3})}{\frac{2}{3} (1.67 \times 10^{-3}) (1 + 4.57 \times 10^{-3}) + 5.13 \times 10^{-3}}$$

= 1.6×10^{-2}

or $SNR_2 = -17.96 \, dB$.

Therefore, the signal-to-noise ratio at the input to the envelope detector for an interfering signal at a peak cross-correlation condition is approximately 17.5 dB below the design signal-to-noise ratio. If we assume that the signal is encoded with a rate 1/2 code and decoded using a Viterbi decoding algorithm, the transmitters can then operate with 5 dB less output power. For this case $SNR_1 = -5.5$ dB and $SNR_2 = -23$ dB.

The results of this analysis for the desired and interfering received signal-to-noise ratios are summarized in table 4.3-2. Two cases were considered for both the acquisition and verification modes. In the first case no error detection and correction coding was assumed on the multiple access return link. In the second case a rate 1/2 Viterbi convolutional decoding algorithm was assumed. By use of this coding technique it is assumed that a 5 dB performance gain can be achieved. The signal-to-noise ratio for the verification mode is 2 dB higher than that for the acquisition mode. This is because code tracking is assumed during verification and the 0.5 dB toss is due to timing jitter.

Table 4.3-2 Baseline IF Signal-to-Noise Ratios

S NB * 0(dB)	Desire	d Signal	Interfer	ing Signal
Link Conditions	Acquisition	Verification	Acquisition	Verification
Without Codi n g	- 0. 5	1.5	-18. 0	-16, 0
With Coding R=1/2	-5.5	- 3. 5	-23.0	-21, 0

^{*}B is assumed to be a 5 kHz IF bandwidth.

Ĉ

4.3.7 Multiple Filter Acquisition Approaches

In addition to optimizing the parameters of the acquisition strategies described above, further decreases in acquisition time can be achieved by the use of multiple bandpass filters as shown in figures 4.3-11, and 4.3-12. In these cases a band of contiguous bandpass filters is used to cover the doppler uncertainty range.

7

A straightforward parallel approach is shown in figure 4.3-11. A set of k bandpass filters cover the frequency uncertainty band. Each filter output is envelope detected and post detection integrated. The outputs are sampled and digitized. Since the sampling rates are relatively slow (less than 6,000 times per second) a single A/D converter can be time shared among the k channels. Each A/D output is then transformed by log $(I_0, (a_d r_i))$ which is simply accomplished by a ROM lookup table. The outputs are demultiplexed with each channel being independently accumulated and compared with the thresholds using the sequential search strategy. The same basic technique is also applicable to the fixed length test str The local reference is shifted by one-half chip position only when $\epsilon > 0$ of the k frequency cell accumulated outputs fall below the lower the shold. Hence, the dwell time is determined by the longest frequer of cell test. If we denote the individual false alarms by α_k and the regral false alarm by α , then the probability of no overall false alarm equals the joint probability of no individual false alarms. Therefore, if $\alpha \ll 1$,

$$1 - \alpha = (1 - \alpha_k)^k \approx 1 - k \alpha_k$$

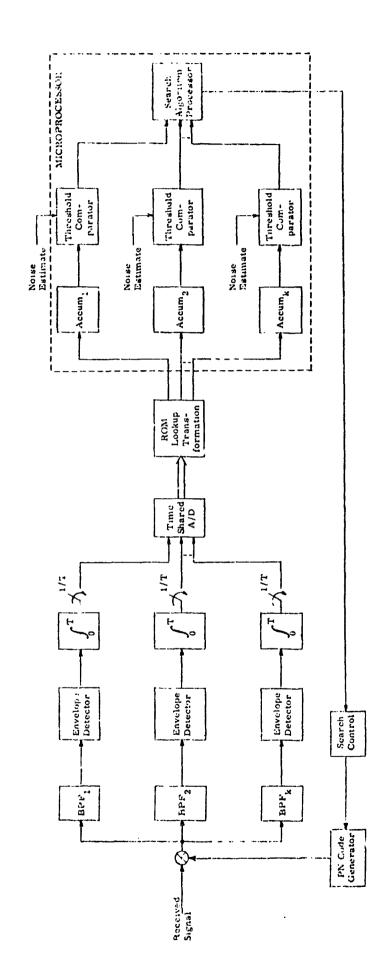
and hence,

$$c \approx k \sigma_{\rm b} \tag{4.3-87}$$

Since we are testing for the presence of exactly one signal in one of the k drequency wells, the overall probability of a missed detection, β is equal

5

The second secon



Parallel and Sequential Analysis Acquisition Circuitry for Frequency Resolution Figure 4.3-11.

•

₹. ₹.

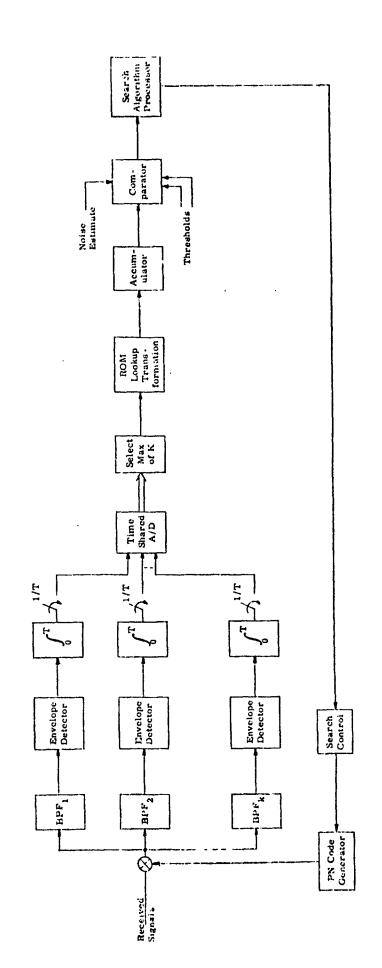
\$

S USAN AND SE

•

3

the second of th



I

I

1.

l

The same of the sa

*

£

The store and

Parallel Sequential Analysis Acquisition Circuitry for Frequency Resolution with Maximum Detector Figure 4.3-12.

to the joint probability that the signal is missed in the ith cell, multiplied by the joint probability of no false alarms in all the other k-l cells.

Hence,

$$\beta = \beta_{k} (1 - \alpha_{k})^{k-1} = \frac{\beta_{k} (1 - \alpha_{k})^{k}}{1 - \alpha_{k}}$$

$$= \frac{\beta_{k} (1 - \alpha)}{1 - \alpha_{k}}$$
(4.3-88)

If $\alpha_k \ll 1$, then $\alpha \ll 1$; hence, the overall probability of missed detection is approximately

$$\beta \approx \beta_{k} \tag{4.3-89}$$

The average sample number (ASN) when noise alone is present is given by

$$\bar{\eta}_0 = \alpha \quad \bar{\eta}_{\alpha} + (1 - \alpha) \quad \bar{\eta}_{1 - \alpha} \tag{4.3-90}$$

where $\bar{\eta}_{\alpha}$ is the average test length when signal presence is falsely declared, $\bar{\eta}_{1-\alpha}$ is the average test length when no signal is correctly indicated. When $\alpha \ll 1$,

$$\bar{\eta}_0 \approx \bar{\eta}_{1-\alpha}$$
 (4.3-91)

Since the number of cells without a signal greatly exceed the number of cells with a signal, the performance is dominated by the average length to reject a cell position. DiFranco and Rubin (4) derive an expression for the average sample number

$$\bar{\eta}_0 = \sum_{\eta=0}^{\infty} \left[1 - P(\eta)^k\right] \qquad (4.3-92)$$

Where
$$P(\eta) = \frac{1}{\beta} \Phi \left(\frac{-2 \ln \beta}{a_d^2 \sqrt{\eta}} + a_d^2 \sqrt{\eta} \right) + \Phi \left(\frac{-2 \ln \beta}{a_d^2 \sqrt{\eta}} - a_d^2 \sqrt{\eta} \right)$$
 (4.3-93)

Where
$$a_d^2 = \frac{2 C'}{N_0 B_k}$$
 (4.3-94)

Which is the peak signal-to-noise ratio in the IF filter of bandwidth $\, B_k^{} \, . \,$ Typically,

$$B_k = \frac{\text{Total Frequency Uncertainty}}{K}$$

and Φ () is the error function.

Hence, equation (4.3-92) replaces equation (4.3-32) when used to compute the average acquisition time with the multiple filter model given in figure 4.3-11. An alternate multiple filter approach is shown in figure 4.3-12. As above a band of contiguous bandpass filters is used to cover the doppler uncertainty range. At each sample interval the maximum output from a set of filters is selected for processing by the sequential decoding algorithm. A detailed analysis of this technique was not made. However, some simulation results by Marcus and Swerling (5) can be used to estimate the performance gains. In [5], the average sample number (ASN) versus the number of resolution elements is plotted for a noncoherent detector. The number of resolution elements corresponds to the number of contiguous filters utilized. These results only go as low as a 0 dB design signal-to-noise ratio. Extrapolating the results to the threshold SNR pertinent to this study, we can estimate that the ASN is divided by the number

of filters and increased by 20 and 50 percent for the 2 and 5 filter cases, respectively. The narrowing of the filter bandwidths increases the signal-to-noise ratio at the filter output with the signal. However, the average time to dismissal is increased over what one might compute for a single filter because one must make a choice between several filter outputs. In a Gaussian noise environment, the best choice is maximum likelihood which was the approach used in the simulation.

4.4 Application of Analysis to User Transponder - Forward Link

4.4.1 Performance Summary

A summary is given in this section of the analysis for the average acquisition time of the recommended signaling technique given in section 2.

Short Code

The short code consists of a 1023 chip sequence which is biphase modulated in quadrature with a similarly niodulated 2¹⁸ chip "long" code sequence. The long code channel is transmitted with a signal power which is 10 dB below that in the short code channel.

At threshold, the received signal power-to-noise spectral density ratio is given by C/N_0 = 32.3 dB-Hz. The total doppler and frequency uncertainties are ± 3 kHz. The data modulation rate is 125 bps. The parameters for the short code are as follows:

IF Filter Bandwidth - 6 kHz	37.8 dB
PN Filter Loss	0.9 dB
Power Loss Due to Long Code	0.4 dB
One-Half Chip Offset Loss	2.5 dB
Total Losses	41.6 dB
C/N ₀ at Threshold	32. 3 dB-Hz
Effective Signal-to-Noise Ratio, C'/N ₀ B	-9.3 dB

Long Code

Since the acquisition of the long code follows that of the short code, it is possible (if desired) to coherently acquire the long code. This is because it is assumed that, when the long code acquisition begins, code lock and carrier recovery is achieved. It is also assumed that the code doppler is tracked by each of these loops. Hence, the basic timing losses are timing jitter.

The losses associated with the long code are.

IF Filter Bandwidth - 6 kHz	37.8 dB
PN Filter Loss	0.9 dB
Power Loss Due to Short Code	10.5 dB
Timing Jitter Losses	0.3 dB
Total Losses	49.5 dB
C/N ₀ at Threshold	32.3 dB-Hz
Effective Signal-to-Noise Ratio, C'/NoB	-17.2 dB

As seen from equations (4.3-55) and (4.3-58), the average time to dismissal is inversely related to the effective signal-to-noise ratio in the IF bandwidth. Also, the effective SNR in the IF bandwidth is clearly a function of the IF bandwidth. Table 4.4-1 summarizes the relationships between the IF bandwidths and the threshold signal-to-noise ratios. In the case where the IF bandwidth is 1200 Hz or ±600 Hz, the total 6 kHz frequency uncertainty band is divided into 5 frequency cells. Similarly, with an IF bandwidth of ±300 Hz, there are 10 frequency cells.

Table 4.4-1. Threshold SNR Versus IF Bandwidth

' 11	C'/N _C	B (dB)
Bandwidth	Short Code	Long Code
6 kHz	-9.3 dB	-i7.2 dB
3 kHz	-6.3 dB	-14.2 dB
1.2 kHz	-2.3 dB	-10.2 dB
600 Hz	+0.7 dB	- 7.2 dB

For both the long and short codes, the following detection parameters were assumed for acquisition, verification, and tracking.

Acquisition

The detection probability is based on having two chances during the 2×1023 trials for the short code and 1×256 trials for the long code.

$$P_{D1} = 0.51$$
 $P_{FA1} = 10^{-3} = P_{a}$

Verification

$$P_{D2} = 0.9$$
 $P_{FA2} = 10^{-4} = P_{A}$

Tracking

$$P_{D3} \gg 0.9 = 1 - P_{D}$$
 $P_{FA3} = 10^{-6} = P_{C}$

For the noncoherent dual state acquisition strategy of the short code, the mean acquisition time is shown to be

$$\overline{T}_{acq} = N \left(\frac{T_i}{|1 - 2 d_c T|} + T_{\beta} \right) \left(\frac{1 + \beta}{1 - \beta} \right)$$
 (4. 4-1)

where

T_i = T for fixed length test = T_b for sequential test

with the other parameters as defined above. For a good approximation at threshold,

$$T_a \approx T_b$$
 and $T_A \approx T_B$.

Therefore,

$$T_{\alpha} \approx T_{b} + P_{a}T_{B} + P_{a}P_{A}\left(T_{D} + \frac{F_{C}T_{C}}{1 - P_{C}}\right).$$

$$T_{b} \gg P_{a}T_{B}, \text{ since } P_{a} = 10^{-3}$$

$$T_b \gg P_a P_A \left(T_D + \frac{P_C T_C}{1 - P_C} \right)$$

since $P_a P_A = 10^{-7}$.

Thus, $T_{\alpha} \approx T_{b}$.

Also, from (4.3-47),

$$\beta = P_b + (1 - P_b)P_B + (1 - P_b)(1 - P_{D3}) . \qquad (4.4-2)$$

The last term in (4.4-2) is small compared to the first two terms on the right side of the equation; hence,

$$\beta \approx P_b + (1 - P_b) P_B$$
.

For the fixed length test, to a good approximation,

$$\overline{T}_{acq} \approx N \left[\frac{T}{|1-2d_cT|} + P_a T_B \right] \left[\frac{1+P_b+(1-P_b)P_B}{1-P_b-(1-P_b)P_B} \right]. \quad (4.4-3)$$

Similarly, for the sequential test,

$$\overline{T}_{acq} \approx \frac{NT_b}{|1-2d_cT|} \left[\frac{1+P_b+(1-P_b)P_B}{1-P_b-(1-P_b)P_B} \right]$$
(4.4-4)

where

$$T_{b} \approx \frac{2 T \ln \beta_{1}}{-\left(\frac{C'}{N_{0}B}\right)_{d}^{2}}$$
 (4.4-5)

The parameters used in this analysis for the short code of the multiple access forward link are:

N = 1023

 $d_c = 4.38 \text{ chips/sec}$

 $\beta_1 = 0.76$

 $P_{b} = 0.49$

 $P_B = 0.1$

T = 1/BW for sequential test

T: Variable for fixed length test.

Substituting these parameters into equations (4.4-3), (4.4-4), and (4.4-5), we get the results summarized in table 4.4-2. These results are also plotted in figure 4.4-1. In comparing these two search strategies, one finds that the sequential test strategy is about 50 percent faster than the fixed length strategy for the case where there is only one IF filter. As the IF signal-to-noise ratio increases, the difference in acquisition times increases between the two test approaches. For the case of 10 contiguous IF bandpass filters, the sequential strategy is almost five times as fast as the fixed length strategy. The average acquisition time is given in figure 4.4-2 as a function of the received signal-to-noise ratio. This relationship only holds true if the design signal-to-noise ratio, a corresponds to the received signal-to-noise ratio. Therefore, if the input signal-to-noise ratio increases and the thresholds do not track the change in signal-to-noise ratios the effective acquisition time do not change.

The parameters used in this analysis for the long code of the multiple access forward link are similar to those of the short code with the exception of the number of uncertainty cells. The long code is of length 2^{18} - 256 chips. The relationship of the codes is such that, when the short code is acquired, the uncertainty of the long code is reduced to the number of cells given by

Long code uncertainty =
$$\frac{2^{18}-256}{1023}$$
 = 256 cells.

Hence, the search for the long code requires selecting one of 256 cell positions.

The acquisition time results for the long code are summarized in table 4.4-3 with the results plotted in figure 4.4-3. The analysis was performed for only the sequential tests, using equations (4.4-4) and (4.4-5) for the noncoherent test and equation (4.4-4) with T_b given by

5 5

一日 となっているとのでは、

Comparative Summary of Mean Acquisition Times for the Multiple Access Forward Link Short PN Code Table 4.4.2.

ないとう とう とない 大変 のない といれていいからい ない かい とおかか まましている はまなな ないまない

			Fixed Length	Fixed Length Test Strategy	Sequential T	Sequential Test Strategy
Number of Doppler Cells	IF Bandwidth (Hz)	SNR in IF Bandwidth (dB)	Tacq (sec)	Mean Search Rate (chips/sec)	Tacq (sec)	Mean Search Rate (chips/sec)
	6009	-9.3	42.9	23.8	28.6	35.8
83	3000	-6.3	27.5	37.2	14.2	72
2	1200	-2.3	16.5	62.0	5.7	179
10	009	0.7	13.7	74.7	2.9	353

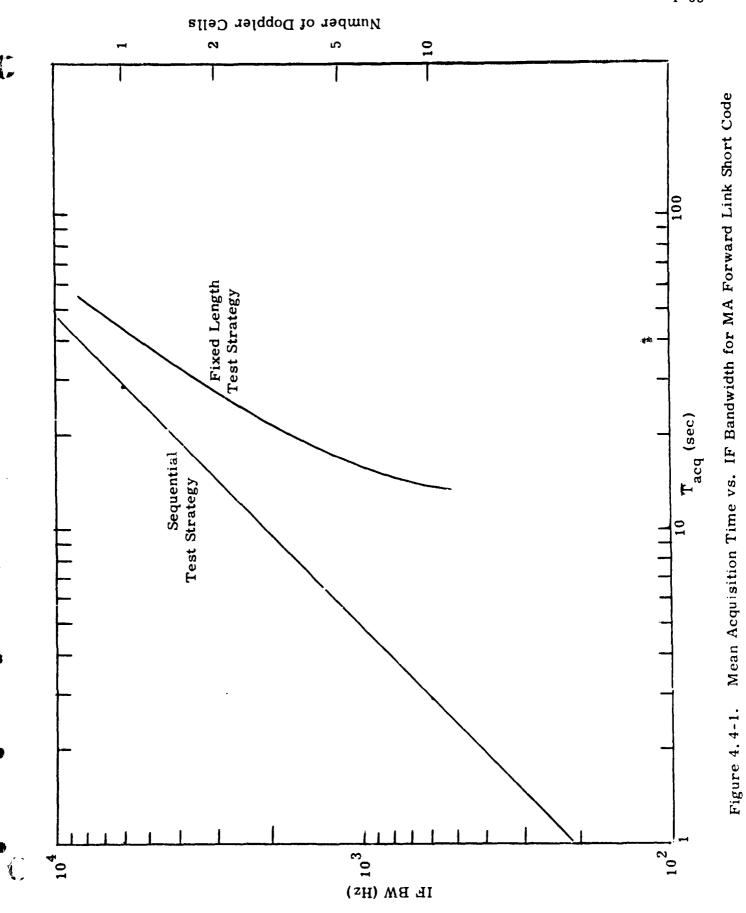
Į

I

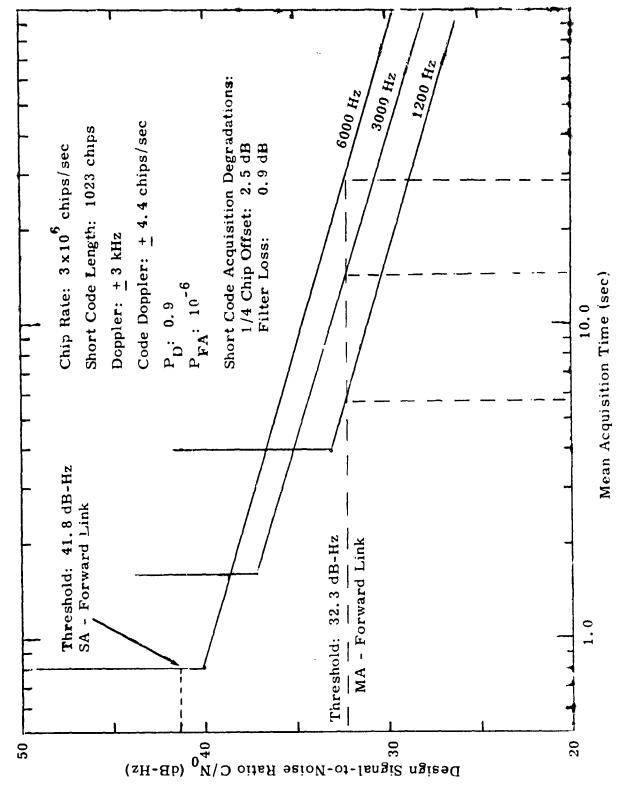
1

STATE SECTIONS ASSESSED TO SECURITY SEC

1



. 1.



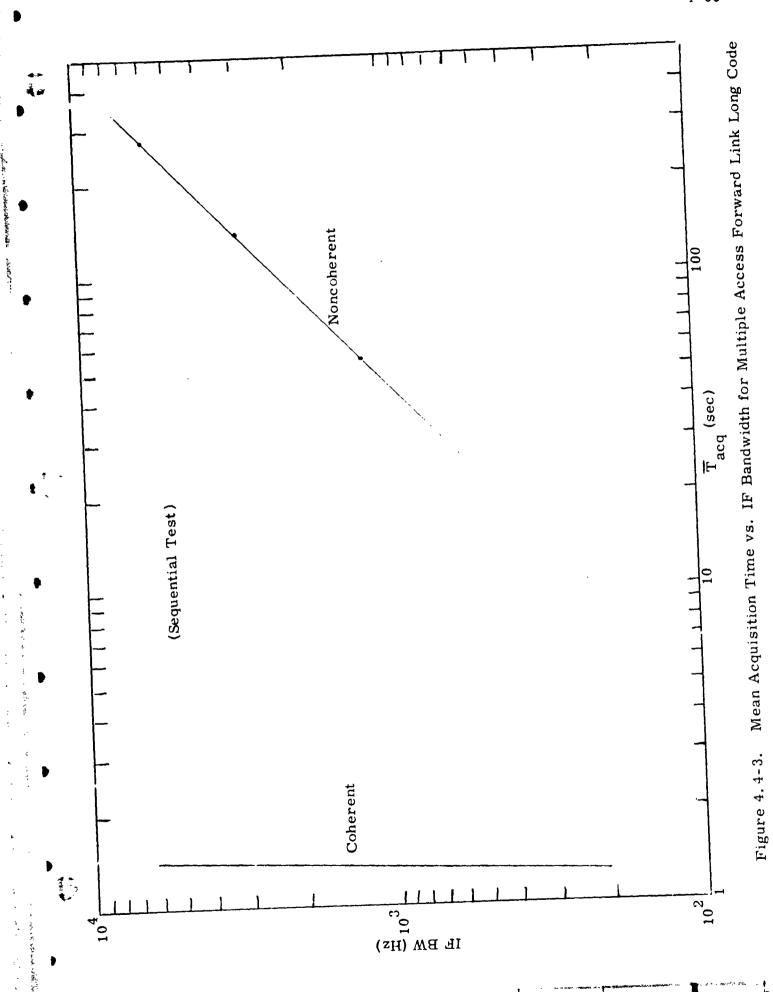
Ì

Ţ

Figure 4. 4-2. Average Acquisition Time Versus Design Signal-to-Noise Ratio for Bouble Step Sequential Acquisition Analysis

Comparative Summary of Mean Acquisition Times for Multiple Access Forward Link Long PN Code Table 4. 4. 3.

		Sequential Col	Sequential Test Strategy Coherent	Sequential Test S Noncoherent	Sequential Test Strategy Noncoherent
IF Bandwidth (Hz)	SNR in IF Bandwidth (dB)	Tacq (sec)	Mean Search Rate (chips/sec)	<u>⊤</u> acq (sec)	Mean Search Rate (chips/sec)
0009	-17.2	1.4	182.9	273	0.93
3000	-14.2	1.35	189.6	138	1.9
1200	-10.2	1.3	196.9	55	4.7
009	-7.2	1.3	196.9	27	9.5



$$T_{b} \approx \frac{T/2 \ln \beta_{1}}{-\left(\frac{C'}{N_{0}B}\right)_{d}}$$

$$(4.4-6)$$

for the coherent test and T_b given by equation (4.4-5) for the noncoherent test. For these tests it is assumed that the local reference is stepped in one-half chip increments. Since chip synchronism occurs at the conclusion of the short code acquisition, the long code could be stepped in single chip increments. For this case the average acquisition times are one-half of the values given in table 4.4-3. Another important factor is that carrier lock occurs at the conclusion of short code synchronization. Given carrier lock and the capability for tracking the doppler frequency offsets, the IF bandwidth can be narrowed significantly. Thus, the performance could actually be significantly better than the acquisition times given in table 4.4-3.

4.4.2 Analysis With an Interfering Signal - Forward Link

Introduction

A model of the forward link with two TDRSS satellites in view of the user receiver is shown in figure 4.4-4. The desired signal is $S_1(t)$ and the interfering signal is $S_2(t)$. The objective of this analysis is to determine the probability that the noncoherent acquisition circuitry locks onto the interfering signal rather than the desired signal as a function of their relative signal levels.

4

71.

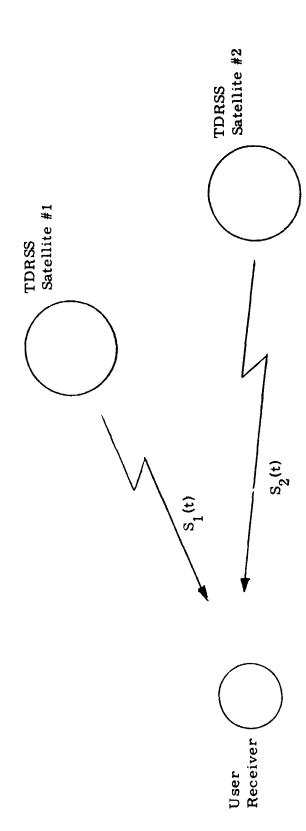


Figure 4.4-4. Model of TDRSS Multiple Access Forward Link

4. (

Ü

*

or sector Mandaton. It is not Programing and not been not assign different

•

* /

to a second deliver and the second deliver an

Analysis

Both the desired and interfering signals can be represented in general as

$$S_{i}(t) = \sqrt{2S_{i}} a_{i}(t) X_{i}(t) \sin \left[(\omega_{c} + \Delta_{i})t + \theta_{i} \right] \qquad (4.4-7)$$

where X_i = pseudorandom PN Gold code of the i th signal with code length n = 1023 chips

a; = data modulation of the ith signal

 θ_i = relative phase shift of the ith received signal

S; = received power of the ith signal

 Δ_i = sum of the doppler and frequency uncertainties of the ith signal.

The cross-correlation code spectrum for the two codes $a_1(t)$ and $a_2(t)$ is given by

where the value in parentheses associated with the cross-correlation quantity denotes the number of chip positions containing the particular cross-correlation value. That is, out of a total of 1023 chip positions, 136 positions have a cross-correlation value of 63, 767 have a cross-correlation value of -1, and 120 have a cross-correlation value of -65.

In the noncoherent detection analysis, the sign of the cross-correlation value is irrelevant. Since the difference between to ross-correlation values of 63 and 65 is so small, for the purposes of this analysis we will assume that there are 256 positions in which the cross-correlation value is 65. Typical autocorrelation and cross-correlation functions for the 1023 Gold codes are shown in figure 4.4-5.

The frequency spectrum of the interfering signal power at the output of the despreader is given by equation (4.3-62). For the forward link, the data bit rate is assumed to be a nominal 125 bits per second. Hence, T_2 equals 8×10^{-3} seconds. The bandwidth of the bandpass filter is assumed to be 6 kHz since the total frequency uncertainty is \pm 3.0 kHz. Therefore,

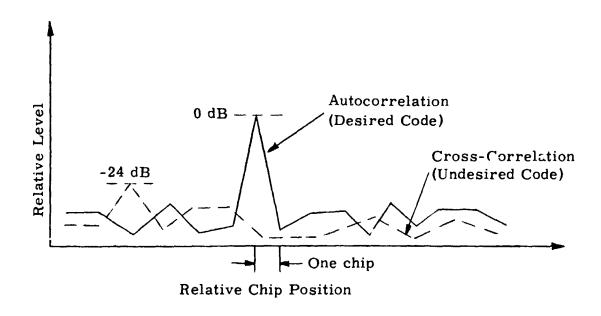


Figure 4.4-5. Typical Auto- and Cross-Correlation Functions for the 1023 Gold Codes

\$

•

3

The state of the s

the signal power at the output of the bandpass filter is given by equation (4.3-66) and for the parameters given above, it can be written as

$$S_0 = \frac{S_2 \rho_{1,2}}{\pi} \int_{-94.5}^{94.5} \frac{\sin^2 x}{x^2} dx$$
 (4.4-8)

$$S_0 \approx \frac{S_2 \rho_{1,2}}{\pi} [\pi] = S_2 \rho_{1,2}$$
 (4.4-9)

With the use of equations (4.3-78) and (4.3-84), we can write the following relationship for the signal-to-noise ratio of the interfering signal at the output of the bandpass filter:

$$SNR_2 = \frac{\rho_{1,2}}{\frac{2}{3} \left(\frac{S_1}{S_2}\right) T_c B + \frac{N_0 B}{S_2}}.$$
 (4.4-10)

In this particular example, the various parameters of (4.4-10) are given by

$$\rho_{1,2} = \left(\frac{65}{1023}\right)^2$$

$$B = 6000 \text{ Hz}$$

$$T_{c} = 0.333 \times 10^{-6} \text{ sec}.$$
(4.4-11)

When the threshold signal-to-noise ratio was computed for the desired signal, a one-half chip offset loss of 2.5 dB was assumed. In comparing the signal-to-noise ratio of the interfering signal, we will take the worst-case position and assume that there is no chip timing loss. From section 4.4.1, we have shown that the threshold signal-to-noise ratio of the desired signal is given by

$$\frac{S_1}{N_0 B} = -9.3 \text{ dB}.$$

Therefore, we can write the relative signal-to-noise ratio of the interfering signal with respect to the desired signal threshold as

$$\frac{S_2}{N_0 B} = \frac{S_1}{N_0 B} \begin{vmatrix} at & +2.5 dB + \frac{S_2}{S_1} \\ threshold \end{vmatrix} . \tag{4.4-12}$$

Substituting (4.4-11) and (4.4-12) into (4.4-10), we get the following relationship between the relative ratios of the two signals and the signal-to-noise ratio of the interfering signal:

$$\frac{S_2}{N_0 B} = 0.21 \rho_{1,2} \frac{S_2}{S_1}$$
 (4.4-13)

or

$$\frac{S_2}{N_0 B} = -30.8 + \frac{S_2}{S_1} \Big|_{dB} . \tag{4.4-14}$$

The relationship between the interfering signal and the desired signal threshold or operating point of the sequential test can be given as a function of the relative ratios of the interfering signal level and the desired signal level at the user receiver. This is derived from (4.4-14) and is given by

$$\frac{a}{a_d} = -21.5 + \frac{S_2}{S_1} \Big|_{dB} . \tag{4.4-15}$$

The probability of detecting the interfering signal for a given trial is given by 1-L(a) where L(a) is defined by equation (4.3-29). This relationship is plotted in figure 4.4-6 for several sets of false alarm probabilities and detection probabilities at threshold.

During the acquisition mode, the detection probability is set equal to 0.5, whereas for verification, it is set at 0.9.

The probability of detecting the interfering signal as a function of the ratio of the desired signal level to the interfering signal level is given by

$$P_{DI} = 1 - (1 - P_{DA} \cdot P_{DV})^{m}$$
 (4.4-16)

where m = number of trials or sidelobe peaks = 256

PDA = probability of detecting the interfering signal during acquisition and is plotted in figure 4.4-6 as a function of a/a_d

P_{DV} = probability of detecting the interfering signal during verification and is also plotted in figure 4.4-6 as a function of a/a_d.

The relationship between a/a_d and S_2/S_1 is given by equation (4.4-15).

Analysis Results

The probability of detecting the interfering signal in the process of scanning through each of the cells in the uncertainty range is plotted in figure 4.4-7 as a function of the interfering signal level. This analysis does not consider the probability that the desired signal may be detected prior to detecting the interfering signal and, hence, the results may be slightly pessimistic. The curves in figure 4.4-7 rise rapidly and, as the interfering signal increases to 20 dB above the desired signal, the probability of detecting and verifying the interfering signal in the course of initial acquisition approaches unity.

A nominal worst-case interfering signal level relative to the desired signal level may be 15 dB. This results from a -9 dB user antenna gain in the direction of the desired signal and a +3 dB antenna gain in the direction of the interfering signal. In addition, the desired signal is transmitted with 0 dB design margin, whereas the interfering signal design margin is +3 dB. For this relative ratio of 15 dB, the probability of detecting the interfering signal ranges between 10⁻³ and 10⁻⁴ depending upon the threshold false alarm probability during acquisition, as seen in figure 4.4-7. This is a very low probability; however, as already noted, the detection probability increases rapidly for a small increase in the relative signal-to-noise ratios and, consequently, means for further reducing the false detection probability should be considered.

-12

-14

-16

-18

Ratio of Desired Signal-to-Interfering Signal, S/I (dB)

-20

-24

-22

Aids to the Minimization of False Detection

6

We have seen that, for relatively high interfering signal levels (i.e., greater than 20 dB above the desired signal), the probability of a false lock is high. Once the false lock condition occurs, the local reference is no longer advanced and code tracking begins. One may assume that, by choosing the code loop noise bandwidth B_L such that the interfering signal-to-noise ratio in B_L is below loop threshold, the noise will, with high probability, cause a loss of lock after several time constants. This would probably work if the maximum interfering signal level were 15 dB above the desired signal level. However, if the interfering signal should go to a level 20 dB above the desired signal, then there is insufficient margin to cause the loop to drop lock.

While the delay lock loop is tracking, the carrier tracking circuit is attempting to lock to the carrier of the received signal. The same problem as was indicated above for the delay lock loop may exist with the carrier recovery circuit in discriminating against the interfering signal. However, the quadrature output of the phase recovery circuit or the coherent amplitude detector (CAD) is enabled once carrier lock is accomplished. With the CAD operating, the AGC is thus controlled by the received signal level rather than the receiver noise level. As an example, the signal voltage at the input to the phase detector may be held constant at a 1 v rms level, regardless as to whether the signal is the desired or interfering signal. For this condition, the thresholds associated with the verification mode can be set to a predetermined fixed value independent of the noise. Hence, the mean values of the distributions associated with the interfering and desired signals are separated at their peak by $\rho = (65/1023)^2$ or 24 dB. Thus, even if the interfering signal level is noncoherently acquired and verified, and if the code tracking and phase lock loops lock to the interfering signal, these circuits would be unlocked if the verification test were continued with fixed thresholds that are switched in at the instant the CAD begins functioning.

The probability of unlocking the interfering signal can be made as high as desired by proper selection of the detection threshold. When an interfering signal is detected subsequent to initial acquisition and verification and the acquisition circuitry, code tracking and carrier recovery loops are unlocked, the system should continue searching the cells from the previous point where it had stopped when it had erroneously locked onto an interfering signal.

At the same time the short code is being verified at the conclusion of carrier acquisition, the long code is also in the process of being acquired. Because the thresholds of the long code can be constant values due to the operation of the coherent AGC, it also can be used to unlock the receiver when it falsely locks to an interfering signal. It could in fact be used instead of the short code verification procedure described above. The only drawback is that it would require a longer overall acquisition time. The suggested steps in the synchronization algorithm, with the exception of the multipath test which is discussed in section 4.5, are summarized in the flow di gram given in figure 4.4-8.

Impact on Acquisition Time

When the interfering signal is detected, the effect is one of a false alarm. The difference from a false alarm based on noise is that there is a much greater probability of code lock and carrier lock to the interfering signal (provided, of course, that the level is high enough) than there is to noise alone. This necessitates the continuing verification of the short code subsequent to carrier lock. This additional verification test is one unich was not considered in the previous sections of this report. From figure 4.4-6 and equation (4.3-58), we can compute the mean acquisition time as a function of the ratio of the desired signal-to interfering signal. The results for a single doppler cell are shown in figure 4.4-9. The mean acquisition time thresholds sharply as the interfering signal approaches 20 dB above the desired signal. This can be seen by looking at figure 4.4-6. As the signal level, a, approaches the design signal level, a, the detection

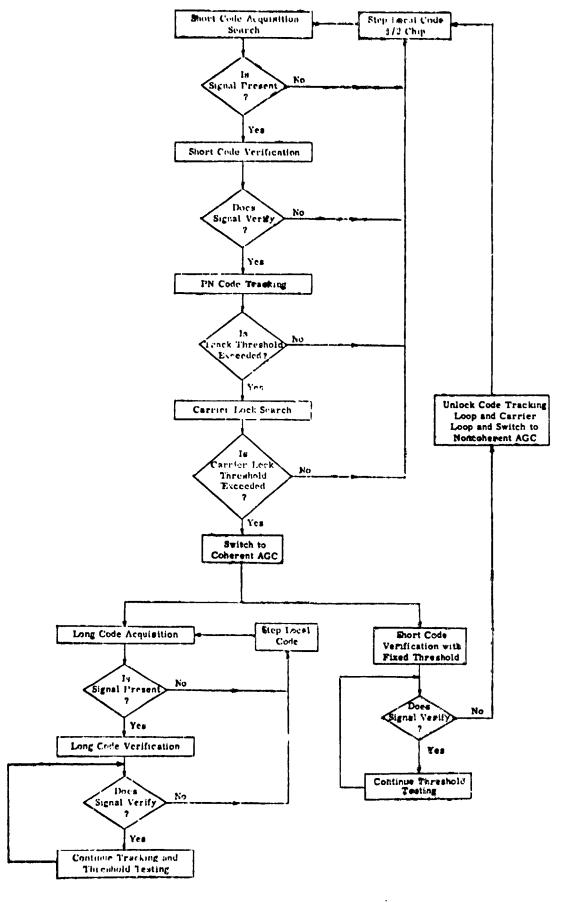


Figure 4.4-8. Simplified Flow Graph of Forward Link Synchronization Algorithm

ķ,

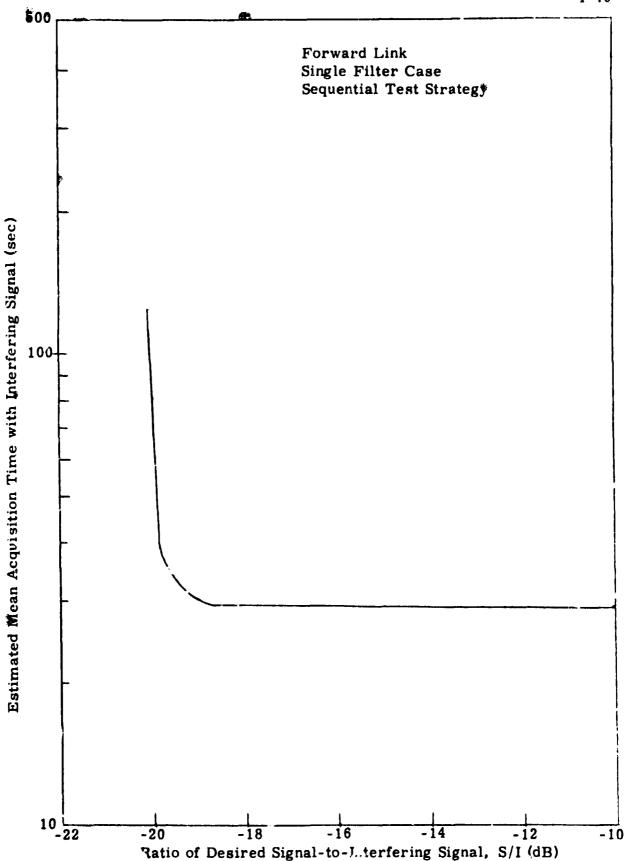


Figure 4.4-9. Estimated Mean Acquisition Time Versus Ratio of Desired Signal-to-Interfering Signal

probabilities in both the acquisition and verification modes approach the design detection probability levels. Since the cross-correlation sidelobes are 24 dB below the autocorrelation peaks, when the interfering signal level approaches 20 dB above the desired signal level, the false alarms due to the cross-correlation peaks approach the design detection probabilities. Therefore, as the code search progresses, each time the cross-correlation sidelobe peak occurs (which is about one-fourth of the time), there is a high likelihood of it appearing as a real signal. It then progresses through the various synchronization steps and is finally rejected with the short code verification test with a fixed threshold after the coherent AGC is switched in. The time to PN code lock, carrier lock, and perform the post-lock verification test was estimated to be 0.5 seconds. This accounts for the "estimated" mean acquisition times given in figure 4.4-9.

Impact on Hardware

The impact of the post-lock verification test is very small when microprocessor techniques are employed in processing the synchronization algorithm. It busically involves a few additional instructions and some logic to unlock 'the code tracking loop, carrier lock loop, and switch back to a nonceherent AGC operation.

4.4.3 Sidelobe False Alarm Analysis

Introduction

The short codes of the forward link are pseudorandom Gold codes of length 1023 with properties enumerated in section 5. The autocorrelation spectra of the Gold codes is similar to the cross correlation spectrum given in section 4.4.2. To simplify this analysis we will assume that there are 256 positions in which the autocorrelation value is 65, one position where it is 1023, and the remaining 766 positions where the autocorrelation value is -1.

The dynamic range of the received signal is assumed to be 35 dB. The objective of this analysis is first to determine the probability of erroneously detecting the sidelobes as in-synchronization positions and then second to consider techniques for either detecting false alarms due to sidelobe detection or reducing the false alarm probability due to sidelobes. A conceptual approach for achieving the former of these objectives is recommended. The impact of this technique on the overall acquisition time is considered, as well as its hardware implications.

The subsequent discussion is primarily conceptual with a level of analysis which is intended to give a first-cut estimate of the system performance. It should be noted that there is room for considerable optimization which could further enhance the overall system performance.

False Sidelobe Detection Probability

The first step in this analysis is to determine the probability of false alarms due to the "self noise" of the received signal (i.e., sidelobe partial correlations) as a function of the received signal level.

The probability of detecting a sidelobe in a given trial for the sequential test algorithm is 1 - L(a) where L(a) is defined by equation 4.3-29. The parameter a is the normalized received signal level. The function L(a) is also dependent upon the normalized threshold or design signal level, a_d, which has a preset value.

The probability of false detection on a sidelobe in a given cell position is plotted in figure 4.4-10 as a function of the received signal level above threshold. This is the probability that a sidelobe of the 1023 Gold code passes both the acquisition and verification tests. The sidelobe levels are 24 dB below the peak correlation level. If the signal is 24 dB above threshold, then the sidelobe level is at threshold and, hence, the probability of detecting the sidelobe equals the probability of the product of the detection and verification probabilities, which are 0.45. As the signal level becomes even greater, the detection probability of the sidelobes rapidly

approaches unity. These results do not consider the effect of the "self noise" which contributes more significantly to the total noise as the received signal level increases. The results also assume a perfect noise estimate which is used in normalizing the design and received signal levels. Both of these factors tond to make the sidelobe false alarm probability higher than would actually be the case.

Sidelobe Rejection Algorithm

;

From figure 4.4-10, we can see that, as the input signal level increases, the partial correlation of a sidelobe is sufficiently high to result in a high probability of false detections. The partially correlated signal level may also be high enough so as to achieve both code and carrier lock. A method must therefore be provided to detect a false synchronization condition, unlock the receiver, and permit it to acquire the correct synchronization position.

There are several ways of detecting a sidelobe lock position. One particularly attractive approach will be considered. The technique takes advantage of the Gold code properties in that the sidelobes with no noise are deterministic and in the case of this code are 24 dB below the peak correlation level. The following discussion presents the case for the sidelobe rejection algorithm.

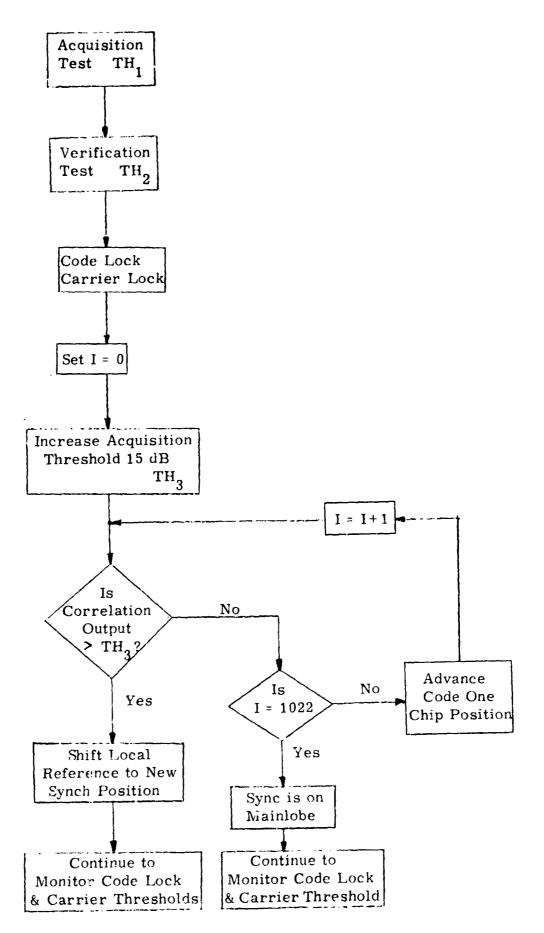
After initial acquisition, verification, code and carrier lock, a post-detection verification algorithm is employed. This algorithm can be similar to the initial acquisition algorithm with the exception that the threshold is increased by some factor. Two cases are considered. In one case the threshold is increased by 15 dB and in the other it is increased by 20 dB. If the sidelobe rejection algorithm is performed with a sequential test, increasing the threshold corresponds to increasing the design signal level, ad. For a fixed length test, it implies that the post-detection integration time is such that a pre-established detection and false alarm probability will be achieved for some higher signal-to-noise ratio. Let us first consider the case where the threshold is increased by 15 dB. If the received

signal level is so high that it exceeds the first threshold by 35 dB, then it will also exceed the second threshold by 20 dB. The partially correlated sidelobe is 24 dB below the peak. It nominally exceeds the first threshold by 11 dB which results in its high likelihood of being detected. However, it falls below the second threshold by 4 dB on the average; therefore, from figure 4.4-10, its probability of exceeding the second threshold on a per trial basis is 1×10^{-5} for the maximum received signal level case. Since there are 256 sidelobes with close the same average partial correlation level, the probability that any one of them will exceed the threshold in the process of scanning through all 1023 chip positions is

$$1 - (1 - 1x10^{-5})^{256}$$
,

which equals 2.5×10^{-3} . However, the probability is almost unity that the mainlobe will exceed the increased threshold given that a partially correlated sidelobe has exceeded the initial thresholds. This assumes that the AGC level is held constant and is controlled by the partial correlation sidelobe level throughout the duration of the sidelobe rejection test. By increasing the sidelobe rejection threshold to 20 dB above its previous level, the probability of the maximum sidelobe level exceeding the new threshold on a per trial basis is decreased to 6×10^{-7} , which yields a probability of 1.5×10^{-4} when scanning through all 1023 cell positions. This reduces the margin between the mainlobe exceeding the increased threshold given that a sidelobe has exceeded the initial synchronization thresholds. However, this margin is still sufficient to yield a detection probability well in excess of 0.9.

The sidelobe rejection test sequence as outlined in the flow chart of figure 4.4-11 can be summarized as follows. After the initial acquisition, verification, code tracking and carrier lock tests are satisfied, the acquisition threshold is increased by 15 dB or 20 dB. The same cell position is checked with the new design parameters. If the new threshold is exceeded, then the position tested is the mainlobe fully correlated cell position. If the threshold is not exceeded, then either the position tested is the mainlobe



Sidelobe Rejection Algorithm Figure 4.4-11.

cell position or a sidelobe position. The local reference is stepped in successive chip positions and the same test is made at each successive cell position. Because code lock exists, single chip steps are sufficient. If the test indicates a signal in any one of the 1023 positions, that position is assumed to be the mainlobe cell. The local reference is then shifted to the new synchronization position. If the threshold is not exceeded in any one of the 1023 potential synchronization positions, then the original cell position is assumed to be the mainlobe synchronization position. For this case, the received signal level is with high probability above threshold but less than 15 or 20 dB above the original design threshold. This sidelobe rejection test can be either a fixed length or a sequential test. For the sequential test, the probability of detecting a sidelobe for a given trial with the new design signal-to-noise ratio 15 dB above the original design threshold is also plotted in figure 4.4-10.

Impact on Acquisition Time

۶

Ś.

ţ.

In this subsection, we will estimate the increase in the overall synchronization time which is due to the sidelobe rejection test. The estimate is made based on a fixed length test for reasons given below. Also, it should be noted that no attempt was made to optimize the synchronization parameters.

The test is to occur after code lock and carrier lock are achieved. When the signal level is near threshold, the probability of false lock to a ridelobe is very small. Since this condition is not known a priori, the sidelobe rejection test must be made. In this case, all 1023 cells will be tested once code and carrier lock are obtained. Thus, in considering the impact on overall acquisition time, we must consider the case where all the cells are tested with the new threshold. Fither a coherent or non-coherent test can be made. We will assume the latter. We also assume that the code lock detection probability is high enough that it establishes the overall synchronization detection probability. Therefore, only one scan through the sidelobe rejection test is anticipated per acquisition

attempt. Hence, we can just compute the time required to dismiss each position with the threshold SNR set 15 or 20 dB above the threshold for the initial acquisition test. The new threshold 15 dB above the acquisition threshold yields a design SNR greater than 0 dB ir the detection bandwidth. The mean time to dismissa omputations given in section 4.3.2 are generally only valid if the design SNR is less than 0 dB. Hence, to simplify the analysis, a fixed length test is assumed. If we draw upon the analysis given in section 4.3.1.1, we obtain the relationship shown in figure 4.4-12, which is a plot of the signal-to-noise ratio at the input to the detector as a function of the time-bandwidth product BT, where $P_{EA} = 10^{-6}$ and $P_{D} = 0.99$. The design SNR threshold was calculated to be -9.3 dB for the sequential analysis acquisition test with a single doppler cell of 6 kHz (cf. page 4-57). Increasing this threshold by 15 dB yields an SNR of 5.7 dB. To achieve a detection probability of 0.99 with a false alarm probability of 10⁻⁶ requires, as determined from figure 4.4-12, a BT of 9. Hence, the time to search all 1023 cells with this BT requires approximately 1.5 seconds. These results are slightly optimistic since the sidelobe noise is neglected and does become a significant factor at the higher signal-to-noise ratios. This time can be reduced as shown in table 4.4-4 by increasing the number of doppler cells. The results, however, are only approximate since the analysis for computing the results in figure 4.4-12 are based upon BT products much greater than unity. If one reduces the detection probability to 0.9 and the false alarm probability to 10^{-5} , then with five doppler cells, a BT of 1 is all that is required and this yields a sidelobe rejection test time of 0.85 seconds.

Because of the potential frequency offset between the local reference and the incoming signal, the code doppler shift may be as great as 1 chip per second or more. This shift does not present a problem since the side-lobe rejection test occurs after code lock is attained and consequently the relative code drift is continuously tracked.

The results discussed above are extended to the case where the threshold is increased by 20 dB. These estimated results are summarized

Y

· V / 144 7

Maximum Estimated Time for Sidelobe Rejection Test (Fixed Length) With Threshold 15 dB Above Acquisition Threshold Table 4. 4-4.

10-6	ise Required Time- Time to Search ased Bandwidth Product 1023 Cells (B) (BT) (sec)	9 1.5	4 1.4	1.5
$P_{FA} = 10^{-6}$	Signal-to-Noise Ratio for Increased Threshold (dB)	5. 7	8.7	12. 7
$P_{\rm D}$ = 0.99	Bandwidth per Cell, B (Hz)	6000	3000	1200
	Number of Doppler Cells	1	2	က

 $P_{\rm D} = 0.9$ $P_{\rm FA} = 10^{-}$

5 Doppler Cells, BT = 1

Time to Search 1023 Cells = 0.85 seconds

in table 4.4-5 and show that the impact on acquisition time of the sidelobe rejection test can be reduced to below 0.5 seconds.

Impact on Hardware Complexity

The additional impact of the sidelobe false alarm detection algorithm to the hardware complexity is small. A separate correlator with a bandpass filter, envelope detector and post-detection integrator as shown in figure 4.3-3 is part of the receiver hardware for the purpose of estimating the receiver noise and the "self noise" level. This hardware can also serve in performing the decorrelator part of the sidelobe rejection test. The other logic, counter and control operations contribute minimally when microprocessor techniques are employed in processing the overall synchronization algorithm.

Maximum Estimated Time for Sidelobe Rejection Test (Fixed Length) With Threshold 20 dB Above Acquisition Threshold Table 4.4-5.

Ī

!

ł

,	$P_{\rm D} = 0.99$	$P_{FA} = 10^{-6}$	9-01	
Number of Doppler Cells	Bandwidth per Cell, B (Hz)	Signal-to-Noise Ratio for Increased Threshold (dB)	Required Time- Bandwidth Product (BT)	Time to Search 1023 Cells (sec)
1	0009	10.7	2.5	0.43
<i>c</i> 1	3000	13.7	1.2	0.41
ស	1200	17.7	0.45	0.4

The second secon

4.5 Application of Analysis to Ground Receiver

4.5.1 Performance Summary - Multiple Access Return Link

A summary is given in this section of the analysic of the average acquisition time for Mode 2 of the multiple access return link. The modulation technique is staggered QPSK with a recommended chip sequence consisting of 2¹¹-1 chips.

At threshold, the received signal power-to-noise spectral density ratio without coding is given by $C/N_0 = 39.9$ dB-Hz and $C/N_0 = 34.9$ dB-Hz with 1/2 rate Viterbi coding. For the single IF filter configuration, an IF filter bandwidth of 5 kHz is required to accommodate the frequency uncertainties and data modulation. Losses were given in section 4.3.5 with a summary of the 1F signal-to-noise ratios in table 4.3-2. The signal-to-noise ratio is assumed to increase by 2 dB in the verification mode because the code tracking loop in operating.

An equation which closely approximates the mean acquisition time was derived above and is given below.

$$T_{ACQ} = N \left[\frac{T}{|1-2 d_c T|} + P_a T_B \right] \left(\frac{1+\beta}{1-\beta} \right)$$
 (4.5-1)

where

N = number of chips in code length

T = Post Detection Integration Time

TB = Average time to perform verification test leading to a dismiss decision

P = probability of false acceptance by acquisi-

d = code doppler error

$$\beta \approx P_b + (1 + P_b) P_B$$

Three code lengths were considered: $N = 2^{11} - 1$, $2^{13} - 1$ and $2^{15} - 1$. In order to avoid the problem of partial correlations, the post detection integration interval was selected to correspond to at least as a minimum one complete cycle of the PN code. Since B is assumed to be 5 kHz, for the code length $N = 2^{11} - 1$,

BT =
$$\frac{2^{11}-1}{3}$$
 (5 x 10³) = 3.4

as a minimum to satisfy the above conditions. If BT is much greater than 3.4, whether or not the integration time is integrally related to the college length period is not all that critical.

No Coding Case

¥

₹.

If we consider first the case without coding, we have from table 4.3-2 a signal-to-noise ratio of -0.5 dB during acquisition for the desired signal and 1.5 dB during verification for the desired signal. If we assume a false alarm probability of 0.01 during acquisition, then the detection probability for the desired signal is

$$P_{D} = 1 - (1 - P_{D}^{'})^{2}$$
 (4.5-2)

where

$$P_{D}' = \frac{1}{2} \left[1 - \text{erf}(.292) \right] = .35$$

from 4.3-11.

and hence, $P_D \approx .58$.

Equation (4.5-2) is used because during acquisition there are at least two chances for detecting the synchronization position when the local reference is stepped in one-half chip increments.

The interfering signal is at -18.0 dB during acquisition. Since the threshold is set for the desired signal with some minimum false alarm probability, the detection probability of the interfering signal for a given trial is 1.18×10^{-2} , which is very close to the false alarm probability. The total detection probability is a function of the number of trials. For the Gold codes, we will assume that half of the cell positions have sidelobe cross-correlation power corresponding to an SNR_{IN} = -18 dB. Therefore, the overall probability of detection is

$$P_D = 1 - (1 - 1.18 \times 10^{-2})^{2047} \approx 1$$

For all practical purposes, if the sidelobe cross-correlation $\rm SNR_{IN}$ is as low as -18 dB, the undesired signal appears as noise and the probability of detecting the interfering signal is about the same as the false alarm probability. This leads to the verification mode which is designed to reject the acquisition mode false alarms.

During verification, we set the false alarm probability at 10^{-4} . We will also assume a BT = 25. In other words, the post-detection integration interval is set for 5 ms. From table 4.3-2, the SNR_{IN} for the desired signal is 1.5 dB and for the interfering signal is -16.5 dB. With these parameters, using equations 4.3-8 and 4.3-11, we get

$$P_{II}$$
 (interfering signal) = 2×10^{-4}

In the verification mode, there is only one cell position in which the interfering signal will be detected and that is the position where acquisition is indicated. From the above results, we see that the probability of detecting the interfering signal for the above conditions is only twice that of the false alarm probability.

We can now substitute the above parameters into (4.5-2) to compute the average acquisition time, $T_{\mbox{ACQ}}$ of the desired signal. A summary of the parameters is:

$$P_b = .42$$
 $d_c = 2.02 \text{ Hz}$ $P_B = .05$ $T = 6.8 \times 10^{-4} \text{ sec.}$ $P_a = 10^{-2}$ $T_B = 5 \times 10^{-3} \text{ sec.}$ $P_A = 10^{-4}$

Hence,
$$T_{ACQ} = 3.85 \text{ sec.}$$

If we assume the same time-bandwidth products, for the code lengths 2^{13} - 1 and 2^{15} - 1, then the acquisition times for each of these cases is 30.8 sec. and 123 sec., respectively. This is a lower bound since the post detection integration time during acquisition for these two cases results in a partial correlation condition.

Coding Case

Now, if we consider the case with coding we have during acquisition a C/N_0B for the desired signal of -5.5 dB. If we set the threshold

for a false alarm probability of 0.1, then the probability of detection is given by (4.3-12) where

$$P_D = \frac{1}{2} \quad [1 - erf(.432)]$$

and $P_D = .47$

Since the cross-correlation sidelobes with an undesired signal are 17.5 dB below the desired signal, the ${\rm C/N}_0{\rm B}$ for this condition is -23 dB. This corresponds to a detection probability per trial of 0.1015, which is essentially the false alarm probability.

If during verification, the time bandwidth product is set at 50 and the false alarm probability is set for 0.01, then the probability of detection is 0.74 for the desired signal. The probability of detection of the undesired signal is 7.25 \times 10⁻². If we substitute the following parameters into 4.3-12,

$$P_{\rm b} = .53$$
 $d_{\rm c} = 2.02 \, {\rm Hz}$ $P_{\rm B} = .26$ $T = 6.8 \times 10^{-4} \, {\rm sec.}$ $P_{\rm a} = .1$ $T_{\rm B} = 10^{-2} \, {\rm sec.}$ $P_{\rm A} = .01$ Code length = $2^{11} - 1$

then $T_{ACQ} = 14.65 \text{ sec.}$

Ξ,

Again, if the code lengths are increased to 2^{13} - 1 and 2^{15} - 1, the average acquisition times with the parameters given above are 58.6 seconds and 234.5 seconds, respectively.

The nonoptimized performance results are summarized in tables 4.5-1 and 4.5-2.

Ĭ.

The desired average acquisition time is 15 seconds. Since it is currently planned to use rate 1/2 coding on the multiple access return link, the code length $N=2^{11}-1$ is the only one which can realistically meet the specified acquisition time requirements. Seven percent of the acquired interfering signals are verified, on the average. The parameters of the code tracking loop need to be such that the likelihood of locking onto the interfering signal is very low. Hence, an interfering signal which triggers a false a arm during verification would be rejected. This subject requires further investigation.

Conclusions

(&

3,

We have shown that, based on an analysis of the acquisition and verification modes, a code length of 2^{11} -1 is sufficient. This, of course, assumes that the parameters of the code tracking loop are selected to effectively reject interfering signals which pass both the acquisition and verification tests.

Although the sequential testing strategy was not analyzed in this investigation for the return link, it also is a candidate technique for reducing the mean acquisition time. There is only one potential problem with the sequential test in this application: The fixed length test has a threshold set for fixed detection and false alarm probabilities and a fixed integration interval. In the sequential test, the integration (accumulation) interval is variable and the thresholds are set for fixed false alarm and detection probabilities about a design signal-to-noise ratio. The capability of the sequential test to reject an interfering signal and the degree of test truncation required bears more detailed investigation.

There are other possibilities for shortening the acquisition time, some of which were discussed above. One solution is to use parallel correlation, each correlator independently searching separate cells. Two

Table 4.5-1 Detection Performance of Desired and Interfering Signals

Performance		Desire	d Signal		ι	Indesire	d Signal	
Link	Acquis	ition	Verifi	cation	Acquis	sition	Verif	ication
Condition	P _{FA}	P _D	P _{FA}	PD	P _{FA}	PD	P _{FA}	P _D
Without Coding	10 ⁻²	0.58	10-4	0.95	10-2	1.0*	10-4	2 x 10 ⁻⁴
With Coding	10 ⁻¹	0.47	10-2	0.74	10 ⁻¹	1.0*	10-2	7 x 10 ⁻²

^{*}This assumes one searches through all possible cell positions.

Table 4.5-2 Average Acquisition Time vs. Code Length

Code Length N	Average Acquisition Time, TACQ (sec			
Link Condition	2 ¹¹ - 1	2 ¹³ - 1	2 ¹⁵ - 1	
Without Coding	3.85	15.4	61.5	
With Coding	14.65	58.6	234.5	

such correlators would, except for some power losses, approach the possibility of halving the acquisition time. Optimization of the acquisition parameters (i. e., optimum selection of BT products for both acquisition and verification) can be used to shorten the mean acquisition time. Another approach is to use a bank of contiguous doppler resolving filters instead of just one IF filter. At the same time, the maximum output of each filter can be selected for further processing, or each path can be processed independently as discussed above for the forward link.

4.6 Impact of Multipath on Direct Sequence Acquisition Parameters

4.6.1 Introduction

47

4.5

The purpose of this investigation was to assess the impact that multipath may have on the candidate acquisition techniques. The primary acquisition technique of concern is the recommended short code/long code technique described in Section 2. As part of this study, a short subcontract was granted to the Boeing Company to characterize multipath parameters between a low orbiting (200 km altitude) user satellite and the synchronous TDRS satellite. A short summary of these results is presented below. A detailed summary of the results is given in the Interim Report. (1) The impact of these various parameters is discussed relative to acquisition of the 3 Mcps PN signal on the forward link to the user satellite. This is followed by an analysis of the data in an attempt to quantify the multipath impact upon the user receiver. A detailed theoretical analysis, taking into account fading parameters, etc., was not performed.

The Boeing Company has been investigating multipath parameters of satellite-to-aircraft links at L-band for several years. Tests have been run, and computer models have been developed. These models were compared with the test results and a close correlation with the test results was achieved. Thus, the theoretical model is considered to be quite adequate for predicting the results.

4.6.2 Multipath Parameters

The purpose of this section is to define the multipath parameters used in the subsequent discussions.

The multipath channel is a linear system and may be characterized by a time-invariant transfer function which we denote by $T_m(f,t)$. The time-invariant impulse response is denoted by $h_m(t,\zeta)$. If the transmitted signal is denoted by Z(t) with transfer function Z(f), then the input-output relationships corresponding to the use of T(f,t) and $h(t,\zeta)$ are

$$w(t) = \int Z(f) T(f, t) e^{j2\pi ft} df$$
 (4.6-1)

$$w(t) = \int Z(t-\zeta) h(t,\zeta) d\zeta \qquad (4.6-2)$$

where w(t) is the output signal (complex) and Z(f) is the spectrum of Z(t).

The transfer function $T_{m}(f,t)$ and the impulse response $h_{m}(t,\zeta)$ are Fourier transform pairs,

4

٠.

8

$$T_{m}(f,t) = \int h_{m}(t,\zeta) e^{j2\pi f\zeta} d\zeta \qquad (4.6-3)$$

$$h_{m}(t,\zeta) = \int T_{m}(f,t) e^{j2\pi f\zeta} df$$
 (4.6-4)

The width of the spectrum of a received carrier, i.e., the spectral width of $T_{\rm m}(f,t)$ with f fixed, is called the Doppler spread of the channel at f_0+f . This doppler spread determines the rate of fading of the channel.

If another carrier is transmitted at a different frequency, $f_0+f+\Omega$, sufficiently close to f_0+f it will be found that the envelopes and phases of the two received carriers essentially fade in step. As the separation frequency Ω is increased, $T_m(f,t)$ and $T_m(f+\Omega,t)$ will begin to depart. The term coherence bandwidth, w_{coh} , will be used to define the frequency interval for which $T_m(f,t)$ and $T_m(f+\Omega,t)$ are 50 percent correlated.

If the spectrum Z(f) of the transmitted signal occupies a bandwidth $w < w_{coh}$, then the output is given approximately by

$$w(t) \approx Z(f) T(0, t)$$
. (4.6-5)

That is, the channel acts as a complex multiplier T(0,t), causing all the frequency components of Z(t) to fluctuate in step. This is referred to as flat fading. If the input signal bandwidths exceed w_{coh} , frequency selective distortion or fading will result, i.e., not all the frequency components will fluctuate in unison.

A complete description of the channel multipath statistics is obtained from the delay Doppler scatter function, $S(\tau, \omega)$, which represents the power spectral density (PSD) of energy returned with a specified delay τ and Doppler ω . Equivalent and lower order multipath parameters are obtained via Fourier and integral operations on $S(\tau, \omega)$.

A summary of the channel parameters pertinent to this study and their mathematical relationships to $S(\tau, \omega)$ is given below.

Delay Spectrum - Fower spectral density (PSD) of energy arriving at the receiver with specified delay τ :

$$Q(\tau) = \int_{\omega} S(\tau, \omega) d\omega. \qquad (4.6-6)$$

Doppler Spectrum - PSD of energy arriving at the receiver with specified Doppler frequency shift ω :

47

٤.

$$D(\omega) = \int_{\tau} S(\tau, \omega) d\tau. \qquad (4.6-7)$$

Frequency Autocorrelation Function - Complex cross-correlation between two received surface modulated carriers transmitted Ω Hz apart:

$$R(0,\Omega) = \int_{\tau} Q(\tau) e^{-j2\pi\tau\Omega} d\tau . \qquad (4.6-8)$$

<u>Time Autocorrelation Function</u> - Time autocorrelation function of the received surface modulated carrier signals complex amplitude:

$$R(\zeta,0) = \int_{\omega} D(\omega) e^{-j\omega\zeta} d\omega. \qquad (4.6-9)$$

<u>Tap-Gain Autocorrelation Function</u> - Autocorrelation function of energy arriving at the receiver with specified delay:

$$Q(\tau,\zeta) = \int_{\omega} S(\tau,\omega) e^{-j\omega\zeta} d\omega. \qquad (4.6-10)$$

Mean Square Energy - Total mean square multipath signal strength intercepted by the receive antenna:

$$\Gamma = \int_{\tau} \int_{\omega} S(\tau, \omega) d\tau d\omega . \qquad (4.6-11)$$

1

Channel Parameter Spreads - The spread measure provides a compact description of the effective width of a given channel parameter. Figure 4.6-1 illustrates the definitions of the 3 dB and 10 dB measures as they pertain to $Q(\tau)$, $D(\omega)$, $|R(0,\Omega)|$, $|R(\zeta,0)|$, and $|Q(\tau,\zeta)|$.

4.6.3 Multipath Prediction Model Description

The following section was extracted to a large extent from the Boeing report. (6)

The choice of an appropriate model for the analysis of electromagnetic surface scatter is determined almost exclusively by the roughness characteristics of the reflecting medium. Surfaces are usually classified as slightly rough, very rough, or composite, depending upon the magnitude of the height irregularities. In general, different scatter theories are utilized in each of these situations.

For the rise of oceanic scatter at a frequency of 2.1 GHz, the surface will st always appear to be very rough; this implies that the following is approximately satisfied:

$$\frac{2\pi\sigma_{\mathrm{H}}}{\lambda}\cos\theta_{\mathrm{i}} > 1.0 \tag{4.6-12}$$

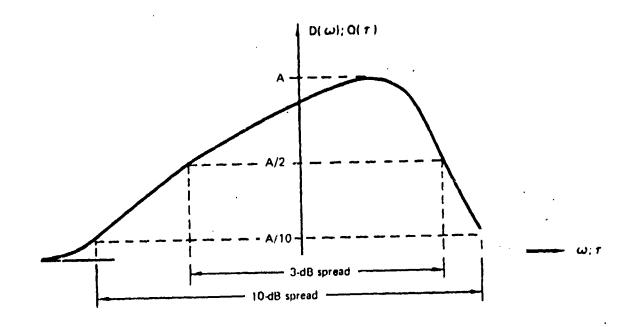
where

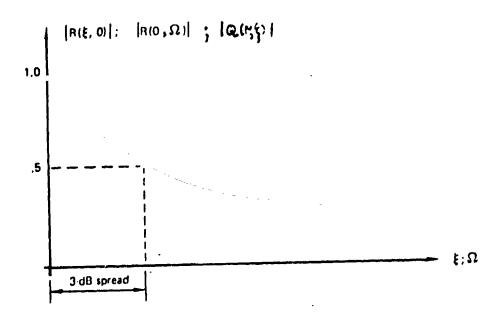
 λ = electromagnetic wavelength

 $\sigma_{\rm H}$ = standard deviation of surface height irregularities

 θ_{i} = incident angle of ray upon the surface as measured from the normal .

Analysis of scattering from very rough surfaces is usually developed through the physical optics tangent-plane method. Commonly called the Kirchoff approximation, this model is based upon the assumption of a locally plane surface over the distance of many wavelengths. This constraint is considered to be satisfied if the radius of curvature of the surface undulations (ρ_c) is much greater than λ , i.e.,





Spread Parameter Definitions Figure 4.6-1

4

For this study, we have employed the vector formulation of the physical optics model and are thus able to properly account for the electromagnetic polarization dependencies of each particular scattering facet on the surface. Due to the complexity of this model, it is not possible to arrive at adequate channel parameter solutions in a closed form. This is circumvented through use of a computerized technique which subdivides the spherical scatter surface into incrementally small areas and then determines the scatter cross-section (including polarization transformation factors), Doppler shift, and time delay associated with each area. The complex vector representation of the scattered signal is coupled to the receiver antenna characteristics, thereby providing an estimation of the received power from the particular surface patch. This allows the channels delay Doppler scatter function, $S(\tau, \omega)$, to be constructed. From $S(\tau, \omega)$, integral and Fourier transform steps identical to those described in Section 4.6.2 are employed to determine the channels delay spectrum. Doppler spectrum, time autocorrelation function, frequency autocorrelation function, total energy content, tap-gain autocorrelation function, and spread values of the unidimensional distributions.

4.6.4 Analysis Parameters

Predictions were generated for the following ensemble of system and sea surface parameters:

Transmitter altitude Synchronous

Receiver altitude 200,000 meters

Receiver speed 7.8 km/sec

Receiver heading (a) ward transmitter; great

circle path, and (b) broadside to transmitter; great circle path

Transmitter polarization RHC

Receiver polarization Vertical, horizontal, RHC, LHC

Antenna directivities Isotropic

Grazing angles 7°, 30°, 60°, 85°

Surface type Sea water

Surface total RMS slope 6°

Although all combinations of the above parameters were analyzed, detailed spectra and correlation function prediction were generated only for the circular polarization receiver conditions. A coarser and correspondingly less expensive surface integration procedure was used to predict total RMS scattered energy coefficients for the vertical and horizontal polarizations. In general, one may use the LHC results to provide a relatively close estimation of the linear polarization spectra and correlation function distribution.

4.6.5 Prediction Results

₹

As previously outlined, the multipath channels delay-Doppler scatter function, $S(\tau, \omega)$, is the basic parameter calculated by the computer model. The delay and Doppler coordinates of this function are evaluated with respect to the attributes of the return arriving from a scattering element located at the specular point. For this part colar analysis, the delay bins (referred to in the following figures and tables delay taps) were chosen to be $2\mu s$ in width and tap number 2 was

selected to have a capture interval beginning with the specular point multipath arrival. Another way of representing the receiver is shown in Figure 4.6-2. The tap spacings are $2\mu s$. Each tap output is multiplied with a locally generated PN sequence and the mixed output is envelope detected. The integrated and sampled tap outputs provide a continuous delay signature of the scattered signal. Taps are aligned side by side with no overlap; hence, tap 1 captures no energy and the n^{th} tap will uniformly capture energy with delays falling between 2(n-1) and 2n μsec with respect to the specular point return. This τ, ω coordinate reference is related to the delay and Doppler signatures of the direct signal through parameters referred to as the channels differential delay (τ_{diff}) and differential Doppler (f_{diff}).

1.

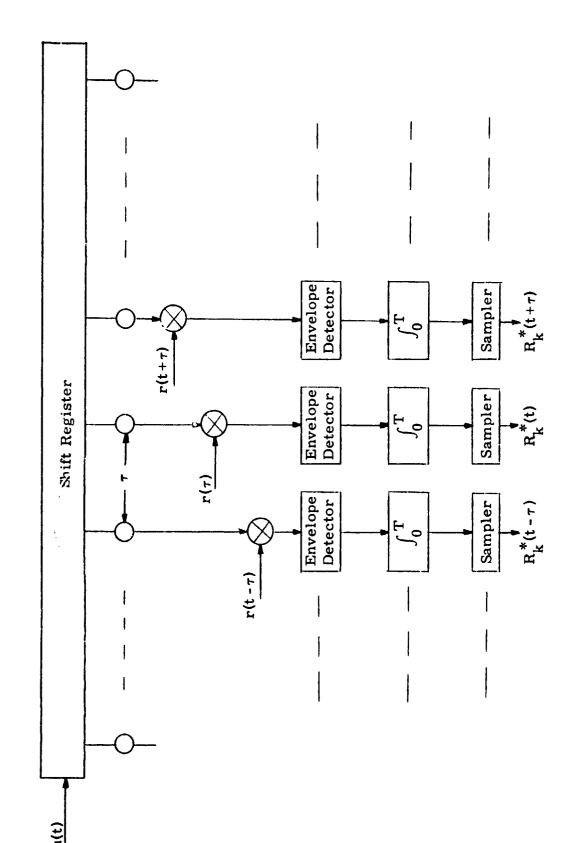
For the grazing angles considered in this study, we present the differential de'ay and Doppler parameters in table 4.6-1.

Channel Parameter Spread Measures

Spreads of the delay spectra, Doppler spectra, frequency autocorrelation function (coherence bandwidth), and time autocorrelation function (decorrelation time) are given in tables 4.6-2 and 4.6-3 for the RHC and LHC polarization cases, respectively. These parameters refer to the characteristics of the total multipath signal and consequently may be thought of as pertaining to the multipath effects upon a CW signal (or signals).

Q(τ, ζ) Spreads and Tap Energy Percent Capture

Tables 4.6-4 and 4.6-5 present the $Q(\tau,\zeta)$ spreads and tap energy percent capture for the RHC and LHC polarization cases, respectively. The spread of $Q(\tau,\zeta)$ represents, in essence, the decorrelation time (0.5 correlation coefficient) of the multipath signal which is captured in tap τ .



地震のある はっているので はないないと かっちゃ こうしきからい

Figure 4.6-2 Tapped Delay Line Representation of Receiver

Table 4.6-1 Differential Delay and Doppler

	TO:00 4: 1	Differential Doppler			
Grazing Angle	Differential Delay	Cross-Plane	In-Plane		
70	98 µs	0 Hz	2.0 kHz		
30°	634 µs	0 Hz	2.9 kHz		
60°	1150 µs	0 Hz	1.8 kHz		
85 ⁰	1330 µs	C Hz	0.3 kHz		

Table 4.6-2 Channel Parameter Spread Measures (RHC Polarization)

Spread		Grazing	g Angle	
Measure	7 ⁰	30 ⁰	60 ⁰	85 ⁰
Delay (3dB)	2.1µs	8.0µs	10.0µs	41.8µs
Delay (10dB)	14.6µs	29. 7 _J us	37.8 µs	80.2µs
Coherence B.W.	37.1 KHz	18.6 KHz	16.4 KHz	9.3 KHz
Doppler (3dB) In-Plane	. 25 KHz	6.1 KHz	13.6 KHz	11.9 KHz
Coppler (10dB)	.83 KHz	11.8 KHz	24.6 KHz	26.9 KHz
Doppler (3 dB) X-Plane	2.2 KHz	7.5 KHz	17.0 _{KHz}	30.0 KHz
Doppler (10dB) X-Plane	4.2 KHz	15.3 KHz	28.0 KHz	45.0 KHz
Decorr. Time In-Plane	8.9 x 10 ⁻⁴ s	$6.7 \times 10^{-5} \text{s}$	3.2 x 10 ⁻⁵ s	2.8 x 10 ⁻⁵ s
Decorr. Time X-Plane	1.9 x 10 ⁻⁴ s	5.1×10^{-5} s	2.8×10^{-5} s	1.7 x 10 ⁻⁵ s

Table 4.6-3 Channel Parameter Spread Measures (LHC Polarization)

SPREAD	GRAZING ANGLE				
MEASURE	70	300	60 o	850	
DELAY (3dB)	2.36 µ s	8.1µs	8.9µs	8.84 µs	
DELAY(10dB)	18.1 μ s	28.8µs	32.0µs	32.4 Jus	
COHERENCE B.W	28.3 KHz	.20.4 KHz	19.8 Kliz	19.5 KHz	
DOPPLER(3dB)	.341 KHz	7.5 KHz	12.5 KHz	15.6 KHz	
DOPPLER (10dB)	1.21 KHz	13.7 KHz	26.3 KHz	30.9 KHz	
DECORR.TIME	$5.7 \times 10^{-4} s$	5.9 x 10 ⁻⁵ s	2.9 x 10 ⁻⁵ s	2.5×10^{-5} s	

Table 4.6-4 $Q(\tau, \zeta)$ Spreads and Tap Energy Capture (RHC)

Tap Number	% Energy Capture	Q(τ,ξ) (In-Plane)	η(τ,ξ) (X-Plane)
2	2%	.12 ms	.093 ms
3	3	.10	. 054
4	3	.098	.042
5	4	.085	.035
6	4	.076	.031
7	4	.095	.028
8	5	. 094	.026
9	4	.065	.023
10	4	.066	.023

 \mathcal{E}

Grazing Angle = 85°

Receiver Polarization = RHC

Table 4.6-4 (continued)

ľ

1.

Tap Number	% Energy Capture	Q(τ,ξ) (In-Plane)	Q(τ,ξ) (X-Plane)
2	11%	.11 ms	.095 ms
3	10	.063	. 052
4	9	.048	. 042
5	8	.043	.035
. 6	7	.039	.031
7	6	.038	.028
8	6	.034	.027
9	5	.034	.025
10	4	.034	.024

Grazing Angle = 60°

Receiver Polarization = RHC

È

1

•

(continued) Table 4.6-4

T..

Tap Number	% Energy Capture	Q(τ,ξ) (In-Plane)	η(τ,ξ) (X-Plane)
2	14%	.24 ms	.12 ms
3	12	.14	.07
4	9.4	.11	.056
5	7.9	.086	.050
6	7.7	.074	.045
.7	6.0	.066	.043
8	4.9	.058	.042
9	4.4	.055	.039
10	3.6	.052	.039

Grazing Angle = 30° Receiver Polarization = RHC

ţ

Table 4.6-4 (continued)

Tap Number	% Energy Capture	Q(τ,ς) (In-Plane)	Q(τ,ζ) (X-Plane)
2	32%	2.1 ms	.25 ms
3	17	1.2	.17
4	11	.82	.17
5	8	.72	.17
6	6	.57	.17
7	5	. 54	.17
8	4	.45	.17
9	3	.42	.17
10	3	.38	.17

Grazing Angle = 70

Receiver Polarization = RHC

Table 4.6-5 $Q(\tau,\zeta)$ Spreads and Tap Energy Capture (LHC)

Tap Number	% Energy Capture	Q(+,1) (In-Plane)
2	14%	9.6 x 10 ⁻⁵ s
3	11	5.1
-4	10	3.9
5	9	3.2
6	8	2.8
7	6	2.5
8	6	2.3
9	5	2.1
10	4	1.8

Grazing Angle = 85⁰

Receiver Polarization = LHC

(continued) Table 4.6-5

Tap Number	% Energy Capture	Q(τ,ς) (In-Plane)
2	13%	.11 ms
3	12	.061
4	10	.045
5	9	.039
6	7	.034
7	6	.030
8	6	.027
9	5	.026
10	4	.024

Grazing Angle = 60° Receiver Polarization = LHC

Table 4.6-5 (continued)

Tap Number	% Energy Capture	Q(τ,ξ) (In-Plane)
2	15%	.25 ms
3	. 12	.14
4	10	.10
5	8	.085
6	8	.073
7	6	.066
8	5	.054
. 9	5	. 053
10	4	.047

Grazing Angle = 30°

Receiver Polarization = LHC

Table 4.6-5 (continued)

Tap Number	# Energy Capture	Q(τ,ξ) (In-Plane)
2	28%	2.2 ms
3	15	1.2
4	10	.85
5	8	.80
6	6	.63
7	5	.55
8	4	. 52
9	4	.49
10	3	.45
6		

Grazing Angle = 70

Receiver Polarization = LHC

Total Mean Square Scatter Coefficient (Γ)

The parameter Γ which represents the ratio of the total multipath signal power to the direct line of sight signal level is given in figure 4.6-3. These data are given for horizontal, vertical, RHC, and LHC polarization modes of the receiving antenna. It is noted that for the LHC results, we assume the antenna polarization is RHC towards the synchronous satellite and LHC everywhere else. For the other polarization cases, the antenna is taken to have the same polarization regardless of elevation or azimuth angle.

MEAN SOURRE TOTAL SCATTER COEFFICIENT (dB)

き会

4.6.6 Extension of Model Predictions

The results generated for this study have direct application only to the list of system parameters delineated in Section 4.6.4. Although these parameters were chosen to represent typical TDRSS configurations and operating environments, one may desire to extend the study results to alternate altitudes and velocities of the low orbit satellite and to different sea surface RMS slope conditions. To provide this extension, we make use of: (1) Model predicted results for both the TDRSS channel and for an AEROSAT channel, and (2) Closed form solution to the scatter channel characterization.

Closed form multipath characterizations, (7,8) applicable to "very rough" surface forward scatter, have been generated for a somewhat restrictive set of surface and geometrical conditions which allow one to apply steepest descent integration techniques to the surface integral formulations. Although this procedure has a variety of shortcomings (for example, the steepest descent model predicts no polarization dependence apart from the absolute magnitude of the total scattered energy), it provides a compact description of the altitude, velocity, and surface RMS slope dependencies of the multipath signal. In particular, the dispersion of $S(\tau,\omega)$ in the delay and Doppler variables has the following approximate functional relationship to altitude (h), velocity (v), frequency (f), and RMS slope (η) :

Delay Dispersion $\alpha h \eta^2$ Doppler Dispersion* $\alpha v f \eta$

これのでは、これにはなっていていませんのというかとういうなななないからない、おおおのななないないが

Apart from the effects of f and h on the spherical earth divergence factor and the Fresnel reflection coefficient, respectively, the above parameters are predicted to have only a minor influence upon the total received signal power level. A measure of the applicability of the above

^{*}Doppler dispersion is also very weakly dependent upon altitude.

dispersion relationships is given in table 4.6-6, where we present data pertaining to model predictions for an AEROSAT channel at 1.65 GHz and for the TDRSS channel. For both channels, sea surface and grazing angle conditions were identical (6° RMS slope and 30° grazing angle). The entry under the column titled, "TDRSS EXTRAP," pertains to the results extrapolated from the AEROSAT predictions via the relationship contained under column, "APPROX CLOSED FORM DEPENDENCE." In general, the extrapolated values are seen to be in fairly close accord with the actual TDRSS model predictions. However, it is also noted that the actual predictions tended to lie below the extrapolated results and, as one would expect, the data for the LHC mode provides a somewhat closer fit to the extrapolated results.

Table 4.6-6 Comparison Between Actual TDRSS and AEROSAT Extrapolated Spread Measures

SPREAD PARAMETER ¹	AEROSAT PREDICTION ²	APPROX CLOSED FORM DEPENDENCE	TDRSS EXTRAP ³	ACTUAL TDRSS MODEL PREDICTION ⁴	ACTUAL TDRSS MODEL PREDICTION ⁵
Delay (3dB)	.46ju s	hs/ha	9.2µs	8.0 J.(s	8.1 µ s
Delay(10dB)	1.76 µs	h _{s/ha}	35.2 µs	29.7 µs	28.8 µ.s
Doppler (3dB)	188 Hz	Vs/Vafs/fa	9.3 KHz	6.1 KHz	7.5 KHz
Doppler (10dB)	326 Hz	Vs/Vafs/fa	16.1 KHz	11.8 KHz	13.7 KHz

- 1 Grazing Angle = 30°
- 2 In-plane geometry (horizontal polarization) with aircraft at 10 KM altitude (h_a) flying 200 m/s (V_a); frequency of 1.65 GHz
- 3 In-plane geometry with low orbit satellite at 200 KM altitude (h_s) traveling at 7800 m/s (V_s); frequency of 2.1 GHz (f_s)
- 4 From Table 4.6-2 RHC polarization
- 5 From Table 4.6-3 LHC polarization

4.6.7 Analysis Results

The primary purpose of this analysis was to examine the multipath parameters and assess their impact upon the recommended TDRSS signal waveform and, in particular, the acquisition strategy of this waveform. The analysis is preliminary and was intended to try to cover each of the areas to the extent necessary to determine the seriousness of the multipath problem relative to the recommended signal waveform.

As can be observed from the data presented in the tables of Section 4.6.5, the multipath parameters are in most cases greatly dependent upon the antenna configuration and the orientation of the user spacecraft relative to the synchronous satellite.

The period of the 1023 chip short code, as described in Section 2, is 341 µsec. The width of the main lobe of the autocorrelation function at mid-amplitude is about 1 chip period or 334 nsec. The differential delay and differential Doppler between the direct signal and the first tap out; ut of the multipath signal is shown in table 4.6-1 as a function of the grazing angle. The differential delay varies from 98 µsec to greater than 1300 usec as the grazing angle increases from 7° to 85°. Thus, at the low grazing angles, the differential delay is such that the multipath signal falls between the main lobes of the direct signal. Hence, there is no impact to the main lobe of the direct signal and the basic problem is one of false locking to a multipath component. However, as the grazing angle increases, the differential delay increases to a point where the multipath component could overlap the main lobe and therefore result in some fading of the direct signal. The overlap is probabilistic and the intensity is a function of the reflection coefficient and the scatter spreads both in time and frequency.

The differential Doppler is a function of the relative spatial vectors of the user satellite and synchronous satellite. From the data given in table 4.6-1, the differential doppler is small enough so that most of the multipath energy in the majority of the cases will fall within the receiver

IF bandwidth. In this preliminary analysis, all of the multipath energy is assumed to fall within the IF bandwidth.

Tables 4.6-4 and 4.6-5 summarize the tap energy percent capture for the RHC and LHC polarization cases, respectively. The energy spread is given over 9 taps or an 18 μ sec interval. The energy for most of the cases is spread beyond these 9 taps as is seen from the 10 dB delay spread given in tables 4.6-2 and 4.6-3. However, except for high grazing angles, most of the energy is concentrated about the first few taps. A cumulative plot of the multipath energy capture as a function of time is given in figures 4.6-4 and 4.6-5 for the RHC and LHC cases, respectively. The results are plotted with elevation angle as a parameter. The mean square scatter coefficient is plotted as a function of grazing angle in figure 4.6-3 for several antenna polarization configurations. The scatter coefficient Γ is a measure of the total reflected energy captured in frequency and time and is given in dB below the direct signal.

Table 4.6-7 summarizes some of this data pertinent to the analysis under consideration. The reflection coefficient is shown versus elevation angle for the RHC and LHC antennas. The percent energy captured in 2 μ sec by the tap with the largest energy captured is also shown as a function of elevation angle. For the TDRS application, we are interested in the energy captured within a single tap of its 3 Mcps signal or 0.33 μ sec. For each of the cases, this was determined from figures 4.6-4 and 4.6-5 and is also given in table 4.6-7. Thus, knowing the relative total reflected energy and knowing the percentage of that energy which falls within a single chip time window, we can compute the minimum signal-to-interference level, assuming we refer to the multipath as interference. These parameters are also shown in table 4.6-7.

The significance of the signal-to-multipath interference parameter is shown in figure 4.6-6. This figure illustrates the allowable dynamic range of the received signal level above threshold before the possibility exists of locking onto the multipath signal. There are two underlying assumptions. The first assumption is that there is no differential antenna

K+E 10 X 10 TO 13 INCH 7 X 10 INCHES

KON 10 X 10 TO 14 INCH 7 X 10 INCHES KEUFFEL & ESSER CO MADE IN USA

X

46 1322

Cumulative Percent Energy Capture

Time in µsec

The second secon

The second secon

Multipath Interference Parameters (IP) vs. Elevation Angle (EA) Table 4.6-7

8

In-Plane/Cross-Plane

al II		R	RHC		ЭНТ	to Multipath,	LHC to Multipath, RHC to Satellite	lite
EA	Г (dB)	% Energy in 2 μs Max Tap	% Energy in 0.33 µs Tap	TDRS S/I (dB)	r (dB)	% Energy in 2 μs Max Tap	% Energy in 0.33 µs Tap	TDRS S/I (dB)
02	-14.3	32	7.5	-25.5	-9.1	28	9	-21.3
300	-20.3	14	က	-35.5	-3.7	15	က	-18.9
09	-33	11	8	-50	-3.0	13	7	-20
850	-54	ស	0.833	-76.7	-3.0	14	2.5	-19

*** : .

4-130 -Rayleigh fading (acquisition) 9 (verify With Rayleigh fading (verification mode) -With Rayleigh fading (acquisition mode) -No multipath fading Rayleigh fading 1 RHC to Satellite, LHC to Multipath No fading or multipath Independence between samples, hence, best case. Allowable Dynamic Range of Signal for Various Conditions Versus Elevation Angle (No Differential Antenna Gain Satellite & Multipath Elevation Angle (Degrees) RHC Between Multipath and Direct Signal) Code Maximum Sidelobe "estimated i - 1 Dashed line implies Fading Assumption: 1023 PN Figure 4.6-6 NOTE: Antenna Gain Between Satellite and Multipath) (qB) on Multipath or Sidelobea is Possible (Assumes no Differential Increase in Signal Level Above Threshold for Which Acquisiti

KM 10 X 10 TO 1. INCH 1 X 10 INCHES MELLER & ESSER CO MARKEN UNITED A CONTRACT OF THE CONTRACT

gain between the satellite or direct signal and the multipath signal. The second assumption is that the multipath signal cannot be acquired if its average signal-to-noise ratio is below threshold.

Another factor which impacts this dynamic range analysis relative to the multipath interference is the time spread factor associated with the individual taps. This parameter is denoted by $Q(\tau,\zeta)$ and is given for the various antenna configurations in tables 4.6-4 and 4.6-5. $Q(\tau,\zeta)$ is the time spread for which there is a 0.5 correlation between samples. If we assume a Gaussian shaped Doppler spectra, then the Doppler spread or fading bandwidth associated with a particular individual tap position is given by

$$\sigma (Hz) = \frac{1}{\pi Q(\tau, \xi)}. \qquad (4.6-14)$$

Using this approach, the estimated fading bandwidth is plotted in figure 4.6-7 for the RHC antenna configuration as a function of elevation angle. The fading bandwidth is seen to vary from 100 Hz at low elevation angles to greater than 3 kHz at high elevation angles. The LHC case was not plotted since it follows very closely the RHC case, which is plotted. The significance of the fading bandwidth is that it determines the degree of correlation between samples taken at the output of the envelope detector during acquisition. Clearly, as the fading rate increases, the successive samples are less correlated and hence a larger signal-to-noise ratio is required to achieve a given detection probability.

From a system point of view, the more difficult it is to acquire a multipath signal, the more desirable the situation. Hence, the best case is when the samples are independent and the effect is as though the multipath component is Rayleigh fading. By making the Rayleigh fading assumption, the increase in the allowable dynamic range is approximately that shown by the dashed lines in figure 4.6-6. The results are plotted for both the acquisition and verify modes in accord with the parameters assumed in Section 4.5.

b

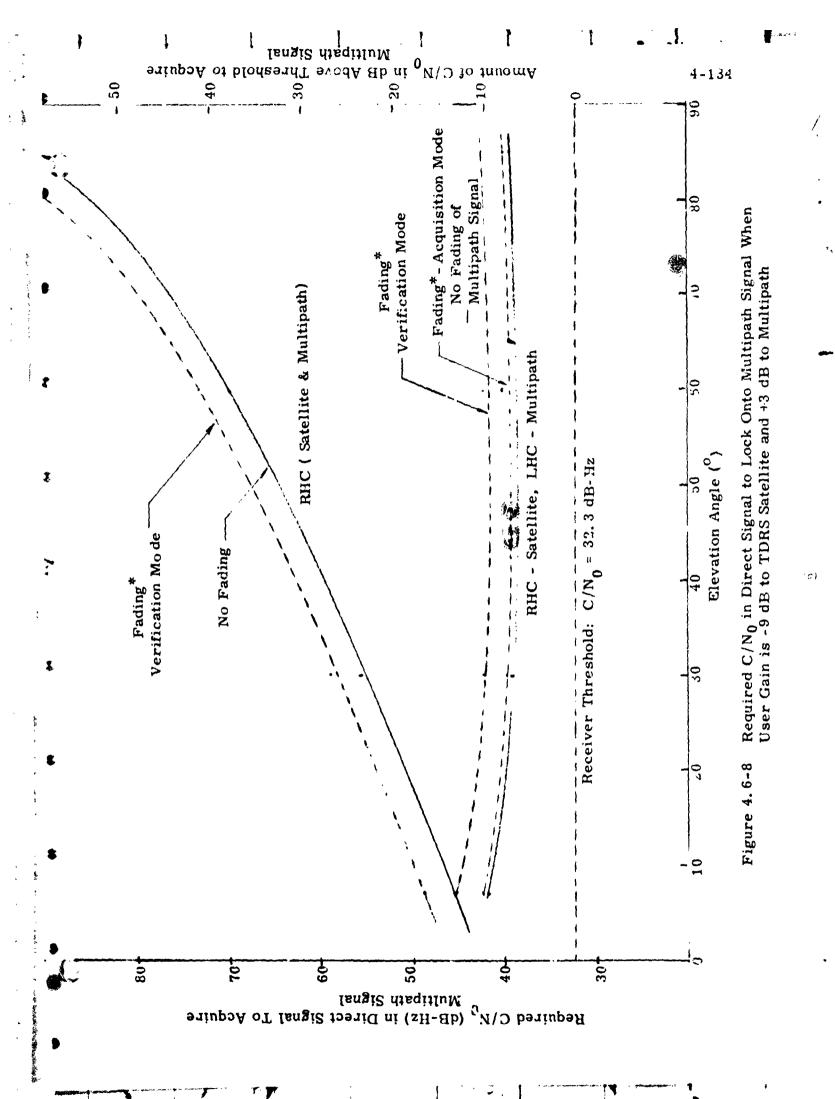
ľ

The dynamic range is least with a minimum value of 18.5 dB when the user receive antenna is RHC toward the multipath.

A specific case of figure 4.6-6 is shown in figure 4.6-8. In this case, a user antenna gain of -9 dB is assumed in the direction of the TDRS satellite and a +3 dB gain is assumed in the direction of the multipath signal. For this case, with the RHC to the satellite and LHC to the multipath, there is slightly more than 6 dB of margin. For the case when the antenna is RHC toward both the satellite and multipath, the margin is much more favorable.

A summary of maximum signal dynamic range against multipath for several elevation angles and antenna configurations is shown in table 4.6-8. The entries in this table assume the worst case condition in that the multipath signal remains constant throughout the duration of the acquisition test.

Į.



Maximum Signal Level Above Threshold to Avoid Multipath Acquisition Versus Elevation Angle for Several Antenna Configurations (assumes no multipath fading) Table 4.6-8

2、 マイン・水水の大きなないはないです。 からからのこと、 からはなるななななななななない。

Maximum Dynamic Range	Omni-Directi	Omni-Directional Antenna*	Maximum Gain of Directional Antenna - Sidelobes Looking at Multipath 10 dB Down	ximum Gain of Directional itenna - Sidelobes Looking at Multipath 10 dB Down	No Differential Antenna Gain Between Direct Signal and Multipath	Antenna Gain rect Signal Itipath
Elevation Angle	RHC: Satellite Multipath	RHC: Satellite LHC: Multipath	RHC: Satellite Multipath	RHC: Satellite LHC: Multipath	RHC: Satellite Multipath	RHC: Satellite LHC: Multipath
70	13.5 dB	9.3 dB	35.5 dB	31.3 dB	25.5 dB	21.3 dB
300	23.5 dB	6.9 dB	45.5 dB	28.9 dB	35.5 dB	18.9 dB
o9	38 dB	8 dB	60 dB	30 dB	50 dB	20 dB
820	64.7 dB	7 dB	86.7 dB	29 dB	76.7 dB	19 dB

*
Omni-Antenna: -9 dB Direct Signal
+3 dB Multipath Signal

1

4.6.8 Direct Signal Verification

There may well be conditions for which the multipath signal level exceeds the threshold, thereby opening the opportunity for the receiver to lock up to the multipath signal. One potential technique for avoiding locking to a multipath signal is to advance the local clock by an amount exceeding the maximum differential path delay after the first indication of acquisition. Search could then be continued perhaps at a slower rate and the loops enabled when the second indication of acquisition occurs. However, for this approach to work, the PN code period must exceed at least twice the maximum multipath delay. This is not the case for the short code as was shown in Section 4.6.7. The long code in quadrature with the short code could potentially be used to resolve the direct signal from the multipath. The difficulty in this case is that the maximum multipath delay is 13 msec for a 2000 km circular user orbit. At a 3 Mcps PN rate, the receiver must search over 39,000 PN chips to resolve the direct signal. At threshold for the long code using a sequential search strategy, it would require 3 minutes to search through this uncertainty region which is an excessive amount of time.

At the conclusion of short code acquisition the code tracking loop is enabled. When PN lock is indicated carrier acquisition is initiated. Normally carrier lock will occur within some prescribed period of time which is short compared to the short code acquisition time. One of the considerations is whether it is possible to code lock and carrier lock onto a multipath signal. Due to the diffuse nature of the multipath signal the cross-correlation function would tend to be smeared thus precluding the locking onto a stable point. Hence, PN code lock would not be achieved and the algorithm would return to the initial acquisition mode. If code lock is attained by the multipath signal, acquisition of the desired signal is precluded. One possible method of eliminating this problem is through the carrier lock loop. We will just briefly consider this possibility. To

achieve carrier lock, a circuit is used to sweep the VCO over the frequency uncertainty range. The bandwidth of the carrier tracking loop is nominally 32 Hz. The primary consideration is whether it is possible to carrier lock onto a multipath signal. The multipath signal as discussed above consists of a large composit of reflected signals phase-shifted and frequency-shifted. The composite waveform is spread in frequency and time.

If we neglect the frequency spreading of the scattered signal, we can write the received multipath signal as

$$r(t) = \sum_{i=1}^{N} a_{i}(t - \tau_{i}) d(t - \tau_{i}) \cos(\omega_{c}t + \theta_{i}) + n(t)$$
 (4.6-15)

where $a_i(t-\tau_i)$ is the amplitude of the i^{th} reflected signal with relative delay τ_i . The amplitude has Rayleigh statistics. The parameter $d(t-\tau_i)$ represents the chip polarity and takes the value of either plus or minus one. The phase angle θ_i is uniformly distributed between 0 and π . The value n(t) is the additive Gaussian noise.

If we assume that the delay lock loop is noncoherently tracking the chip sequence, then the output of the despreader can be written as

$$Z(t) = a_{j}(t) \cos (\omega_{IF}(t) + \theta_{j}) + n(t) + m(t)$$
 (4.6-16)

where the delay lock loop has locked onto the jth reflected multipath signal. Typically, one would anticipate that it would lock onto the largest signal which, for most elevation angles, is the earliest returned signal. The additive noise term m(t) is the cross-correlation of the local PN reference with the N-1 multipath signals that are out of chip synch with the jth signal. Because of the processing gain of the receiver, this term appears as an additional noise factor.

If the carrier loop is to lock cnto the multipath signal, then it must lock to Z(t) above. We will briefly consider the possibility of this occurring. First of all, the amplitude is Rayleigh fading and the phase θ_j which the carrier lock loop must track is uniformly distributed between 0 and 2π . We will consider two effects. The first is the signal-to-noise ratio in the loop bandwidth due to the multipath signal and the other is the fading bandwidth relative to the loop bandwidth.

We will assume that a signal-to-noise ratio of 10 dB is required in the loop bandwidth to give a lock indication. From table 4.6-8, we see that, at an elevation angle of 7°, the average reflected signal is 21 dB below the direct signal in the tap with the largest output. This is then the dynamic range which the direct signal can have so that, under the best conditions, the multipath would be below the carrier loop lock threshold. This dynamic range value changes, of course, as the antenna gain relative to the satellite and multipath varies. The second factor is that the code tracked multipath signal is fluctuating in amplitude and phase. The rate of these fluctuations is a function of the elevation angle (cf. figure 4.6-7). At a 7° elevation angle, this fading bandwidth is approximately 150 Hz which is substantially larger than the 32 Hz loop bandwidth. In addition, as the elevation angle increases the fading bandwidth increases. Hence, coupling these two factors together, that is, the fading bandwidth which exceeds the loop bandwidth and the signal-to-noise ratio in the loop bandwidth, one would conclude that only under very unusual circumstances would the carrier loop be able to track the phase of the multipath signal. Therefore, the second check on having acquired a multipath signal is the subsequent inability to achieve carrier lock. To test for carrier lock the output of the coherent amplitude detector (CAD) can be compared with a threshold. If within a predetermined period of time, the threshold is not exceeded, then either a false acquisition or multipath acquisition of the short code is assumed. The receiver will then automatically unlock the short code loop and a new short code search would be initiated. Another

multipath rejection technique was suggested by Mr. L. Deerkoski. (9)
This technique will probably only work successfully if the long code is
noncoherently detected. Coherent detection was recommended above
for the long code. This was primarily due to the excessive acquisition
time required for noncoherent sequential acquisition of the long code.
However, by the use of multiple filters this time could be reduced considerably as shown in table 4.4-2.

}- --

The proposed technique takes advantage of the time spread of the multipath signal. Based on the Boeing data, the multipath energy is smeared over a number of chips. The extent to which this is true can be seen from figures 4.6-4 and 4.6-5. The rolloff in energy for most elevation angles is quite slow for 5 or more PN chips. This is in contrast to the PN correlation function which approaches zero when the received and reference codes are out of synchronism by one PN chip.

The suggestion is that this multipath time smear be used to discriminate the multipath from the direct signal. The concept could be implemented in the long code detection strategy by adding a multipath detection test subsequent to initial long code acquisition and verification. The multipath detection test could involve offsetting the long code by 2 PN chips relative to the synch position and determining whether correlation is within 10 dB of the initial long code synch correlation. If it is within the 10 dB or some threshold level to be determined, then the time spread of the arriving signal must be present to identify it as the multipath signal. If this is the case, the receiver would then unlock the short code loop and a new short code search would be initiated. If the multipath detection test fails, then time spread is absent and direct signal acquisition is declared.

With this technique, a direct signal verification step would follow the long code verification. The overall acquisition strategy would then take the following form.

Step 1	Short Code Acquisition
Step 2	Short Code Verification
Step 3	PN Code Tracking with Multipath Test
Step 4	Carrier Lock Search with Coherent Am-
	plitude Detector Multipath Test
Step 5	Long Code Acquisition
Step 6	Long Code Verification
Step 7	Direct Signal Verification

To prevent the possibility of multipath capture of the PN tracking receiver, the PN code tracking circuit should be switched to the long code subsequent to direct signal resolution. Since the long code acquisition mode requires searching 128 PN code cells on the average, the addition of another cell for direct signal verification has a very small impact on the long code acquisition time. The entire acquisition process is summarized in the flow chart of figure 4.6-9.

Z.

ź

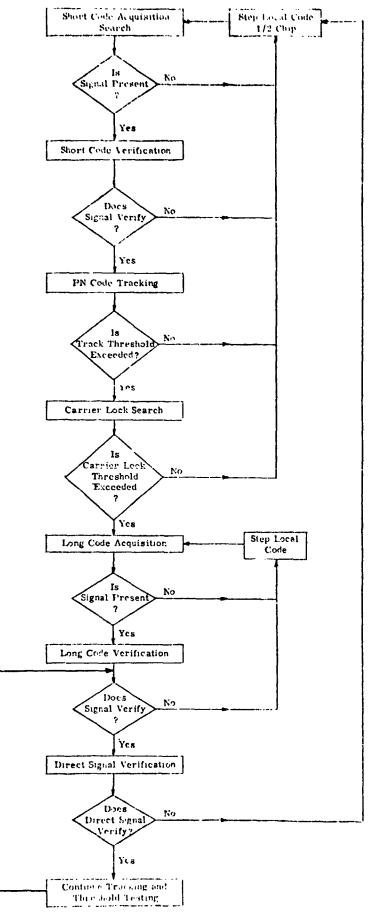


Figure 4.6-9. Summary of Forward Link Acquisition Algorithm

~ ではない

7:7

4.7 References

- 1. R. Dixon, R. Gold, and F. Kaiser, "Interim Report TDRSS Telecommunications System PN Code Analysis," Contract NAS-22546, Robert Gold Associates, April 30, 1976.
- 2. A. Wald and J. Wolfowitz, "Optimum Character of the Sequential Probability Ratio Test," Ann. Math. Stat., 19:326, 1948.
- 3. A. Wald, Sequential Analysis, Wiley, New York, 1947.
- 4. DiFranco and Rubin, Radar Detection, Prentice-Hall, 1968.
- 5. M. B. Marcus and P. Swerling, "Sequential Detection in Radar with Multiple Resolution Circuits," IRE Transactions on Information Theory, IT-8 (3), pp. 237-245, April 1962.
- 6. Allan D. Thompson, "Multipath Characteristics of the Oceanic Tracking and Data Relay Satellite System (TDRSS) Channel," Boeing Commercial Airplane Company, April 15, 1976.
- 7. S. H. Durrani and H. Staras, "Multipath Problems in Communication Between Spacecraft and Stationary Satellite," RCA Review, March 1968.
- 8. A. J. Mallincrodt, "Propagation Error," Unpublished UCLA Short Course notes: Satellite Based Navigation, Traffic Control and Communications to Mobile Terminals, October 1969.
- 9. L. F. Deerkoski, "Direct Signal Resolution for TDRSS Alternate Signal Parameters," Technical Memo, April 16, 1976.

5. 0 CODE GENERATION TECHNIQUES FOR TDRS

5.1 Introduction

The purpose of coding transmissions in the TDRSS is to achieve signals which satisfy flux density restrictions imposed by the International Radio Advisory Committee (IRAC), to facilitate rapid signal acquisition, and to achieve multiplexing capability in the multiple access service categories. These objectives are achieved by means of pseudo random codes which, when used to modulate the system waveforms, result in wideband low power density transmissions. The design of special configurations of PN codes facilitates rapid signal acquisition techniques, and the generation of orthogonal or pseudo orthogonal code structures aids in the achievement of system multiplexing capability.

The main source of the binary sequences which are used as the encoding mechanism to implement the coded signals are the linear (shift register) sequences. This class of sequences is easily generated at the required chipping rate with feedback shift register devices; it is amenable to mathematical analysis and it has been shown to have those characteristics which provide the resultant encoded signals with the desired characteristics outlined in the above paragraph.

Other classes of codes, such as primitive root codes and nonlinear binary sequences, may be used as signal encoding devices but, in general, these classes are more difficult to generate and analyze and do not perform as well as the classes of linear binary sequences.

In this section, we present techniques for the generation of encoding sequences which will achieve the TDRSS signal characteristics stated above and employ these techniques to generate code families having the desired properties.

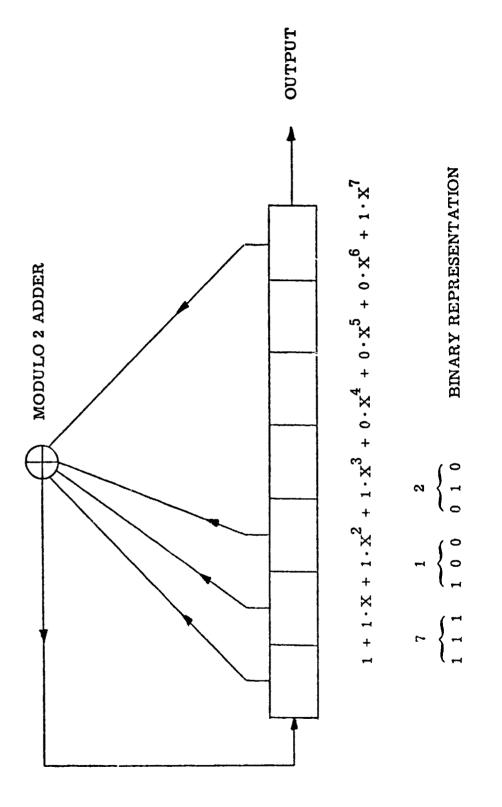
5.2 Some Remarks on Code Tables

A linear shift register code generator is characterized by the number of its shift register stages and its feedback configuration. This information is equivalent to specifying an irreducible polynomial with binary coefficients whose degree is equal to the number of stages in the shift register (Figure 5.2-1). The correspondence between linear feedback shift registers and binary polynomials has been well documented (1,2) and it has been shown that the properties of the sequences generated by the shift register are determined by the algebraic properties of its corresponding binary polynomial.

Many tables of irreducible binary polynomials have been compiled (2-5) and these serve as useful design tools for the configuration of feedback shift registers which will generate linear binary code sequences having specified properties. However useful these tables of irreducible polynomials may be, no one table or even all available tables used together are adequate for the complete design task. In this section, we explain the use of the tables of irreducible polynomials, discuss the advantages and deficiencies of specific tables, and present supplementary techniques which provide the needed information for code generator design which is not available in currently available tables.

The tables by Marsh (3) list all irreducible binary polynomials to degree 19 and the period of the sequences generated by the shift register corresponding to each polynomial. (All phase distinct sequences generated by a linear shift register corresponding to an irreducible polynomial have the same period.) Thus, these tables may be used to generate, for example, maximal linear PN sequences up to period 2¹⁹-1. Since there is no way to determine larger degree irreducible polynomials from those of smaller degree, other tables must be used for PN codes of period exceeding 2¹⁹-1.

A more important deficiency of Marsh's tables concerns the relationship between the different irreducible polynomials of a given degree and hence between the binary coding sequences generated by the corresponding



į .

べんかい はながら 一番 気がないない かかけのないでしょう かいかいかくちょう しんないかん かっかかる からからないない

a min to come out the second s

Figure 5. 2-1. Linear Feedback Shift Register and its Associated Polynomial

いいこうしている 一本のではない いましていませんか こういればいい

OCTAL TABULAR LISTING

shift registers. Taken individually, one maximal linear sequence is indistinguishable from another of the same period with r spect to most of its basic properties and thus there is generally no advantage or disadvantage in choosing one such sequence over any other when such a sequence is used by itself in a particular communication system. However, the relationship between two or more maximal linear sequences of the same period is strongly dependent upon the particular set of sequences chosen and the manner in which such sequences interact (e.g., their cross correlation function) may strongly affect the performance of systems in which such sets of codes are employed.

>.

Marsh's tables provide no means of distinguishing between irreducible polynomials which correspond to linear sequences of the same period. This important defect is supplied in part by the tables of irreducible polynomials published by Peterson. (4) In these tables, each irreducible polynomial and the relationship between the polynomials is characterized by identifying the roots of the polynomials. Thus, in later work, when a particular pair of binary polynomials is specified as corresponding to linear feedback shift registers which generate maximal PN sequences having particularly desirable properties with respect to one another, this polynomial pair is described from the table of irreducible polynomials by specifying the roots of each polynomial as listed in the table. A procedure requiring the selection of particular sets of polynomials of a given degree from the tabular listing will, in general, require a complete listing of the irreducible polynomials of that degree. Peterson's tables provide a complete listing of irreducible polynomials and their roots up to degree 16 and partial listings to degree 34. A complete listing of irreducible polynomials of degree 17 and degree 31 would require 7,710 and 69,273,666 entries, respectively. Thus, for example, a pair of 18th degree binary polynomials which generate optimum codes for the TDRSS multiple access service category are specified by their roots 1 and 1025, as listed in Peterson's tables. The first polynomial

is present but the latter is not included in the incomplete tabular listing of irreducible polynomials.

Gold (2) has compiled a table of maximal polynomials to degree 13. which also identify the roots of the listed polynomials in the same manner as do Peterson's tables. In addition, Gold's tables list the cross correlation function of the maximal PN sequences generated by the listed polynomials. These tables are thus extremely useful in selecting sets of maximal sequences which are most nearly orthogonal. When one maximal polynomial of a given degree is known, then all irreducible polynomials of this degree may be readily computed by a variety of known techniques. (2) i.e., the table of irreducible polynomials may be compiled and their characterizing roots identified. However, there is no known technique for the direct computation of a maximal polynomial of a given degree and, hence, the production of an initial such polynomial must be largely a matter of trial and error. In this connection, Bradford (5) has published tables which list selected maximal polynomials to degree 58. No identification of these polynomials by means of their roots is provided. Watson (6) has published a list consisting of one maximal polynomial of each degree between 2 and 100 which, for most applications, solves the problem of finding an initial maximal polynomial. A summary of available tables discussed herein is provided in Figure 5.2-2.

	IRREDUCIBLE POLYNOMIALS	NUMBER OF MAXIMALS	DEGREE	POLYNOMIAL ROOTS	CORRELATION FUNCTION OF SEQUENCES
MARSH (1957)	YES	ALL	19	ON	ON
PETERSON	OHA	ALL	16	V FS	CX
(1961)	८न्म	PARTUAL	17 - 34		
WATSON (1961)	ON		100	ON	ON
GOLD (1964)	NO	ALL	13	YES	YES
BRADFORD (1965)	NO	PARTIAL	58	ON	ON

Figure 5.2-2. Description of Available 1.. es of Binary Polynomials

5.3 Preferred Pairs of Linear PN Codes

{ _

\$

Gold (2) has shown that the relationship between PN codes corresponding to irreducible polynomials of the same degree is not homogeneous and that, for example, a given set of maximal PN codes may be more nearly orthogonal than another set of such codes of the same period. In (7), Gold introduced the notion of a preferred pair of irreducible polynomials and gave the criteria in terms of their roots for specifying such pairs. A preferred pair of irreducible polynomials is one such that the corresponding linear PN sequences have minimal cross-correlation function. Thus, for example, for degree 12 the maximum value for the cross-correlation function for maximal PN sequences corresponding to the pair of polynomials (10123, 10727) is $\theta = 1407$, while the maximum cross-correlation value corresponding to the preferred pair of polynomials (10123, 14501) is $\theta = 127$, the difference between the two cases being 21 dB. A comparison of the cross-correlation function between the maximal PN sequences generated by a preferred pair and the worst case polynomial pair for polynomials to degree 13 is given in Figure 5.3-1.

A preferred pair of polynomials corresponding to a pair of feedback shift registers which generate binary PN sequences with minimal corretion is determined by specifying the roots of each of the polynomials of the pair. If $\alpha^1 \equiv 1$ is a root of any maximal polynomial of degree n, then the other member of the pair is the polynomial $\alpha^{2^k+1} \equiv 2^k+1$ (any k) for polynomials of odd degree and $\alpha^2^{(n+2)/2}+1 \equiv 2^{(n+2)/2}+1$ for polynomials of even degree. The maximum value of the cross-correlation sidelobes for the sequences corresponding to the preferred pair are then shown to be $2^{(n+1)/2}+1$ for n odd and $2^{(n+2)/2}+1$ for n even.

The TDRSS communication links will use a code pair consisting of two PN codes, one modulating the I channel and one modulating the Q channel of a staggered quadriphase PN modulation technique. In order to achieve maximum isolation between these channels, it is recommended

		EXAMPLE: DEGREE 12	$20 \log \frac{1407}{4095} - 20 \log \frac{127}{4095} = 20.$								
	DIFFERENCE (DB)	1.7	3.7	7.6	9.7	10.7	15.7	12.9	20.9	14.9	
θ SIDE LOBE	PREFERRED PAIR	O	15	1.7	31	33	63	65	127	127	
IS 0	WORST	11	23	41	95	113	383	287	1407	703	
	PERIOD	31	63	127	255	511	1623	2047	4095	8191	
	DEGREE	ın	9	7	ထ	တ	10	11	12	13	

1.

Figure 5.3-1. Performance of Preferred Pairs Compared with Worst Case Polynomial Pairs

that the pairs of maximal PN codes chosen for this purpose in single access forward and return links be preferred pairs, or codes generated using preferred pairs.

To find the preferred pair, we select an arbitrary maximal polynomial having root $\alpha^j \equiv j$ from its listing in the table of irreducible polynomials and then find the polynomial having root $(\alpha^j)^t \equiv j \cdot t$ from the same table, where t is as given above. Clearly, only the tables of Peterson and Gold can be used for this procedure, since only these tables assign roots to each polynomial. For preferred pairs of polynomials to degree 16, computational techniques must be used to obtain the polynomial having the specified roots. A computer program for the generation of preferred pairs has been written (Appendix F.5), and a table of the preferred pairs for code lengths as currently described in the TDRSS User's Guide was generated, and is included in Appendix E.5. The code polynomials are listed in octal notation.

5.4 Generation of TDRS Band Spreading Codes

5.4.1 Introduction

The basic bandspreading codes recommended for use in the TDRSS MA service are balanced Gold codes of the appropriate length. In this section, we describe the method for implementing the shift register configuration and determining the register initial conditions which will generate these codes.

The family of 2ⁿ+1 Gold codes of period 2ⁿ-1 is generated by taking the modulo 2 sum of a preferred pair of maximal PN sequences where each of the 2ⁿ-1 relative phases of the two maximal sequences produces one of the 2ⁿ-1 members of the family. It has been shown (8) that the codes of the family fall into one of three categories according to the relative number of ones and zeroes in the code sequence:

	Number of ones in code sequence	Number of codes of family having this number of ones
(a)	2 ⁿ⁻¹	$2^{n-1} + 1$
(b)	$2^{n-1} + 2^{(n-1)/2}$	$2^{n-2} - 2^{(n-3)/2}$
(c)	$2^{n-1} - 2^{(n-1)/2}$	$2^{n-2} + 2^{(n-3)/2}$

We note that the $2^{n-1} + 1$ codes of category (a) have 2^{n-1} ones and hence (since the code length is $2^n - 1$) $2^{n-1} - 1$ zeroes. The codes of this category are thus balanced in the sense of having only one more one than zeros (this is the best possible balance since the codes have odd period). The codes of categories (b) and (c) have a surplus and deficiency of ones, respectively, and thus have less desirable spectral characteristics. In order to generate balanced code members of the family, we must determine and select the proper relative phases of the two original maximal sequences. In what follows we describe how this is accomplished.

5.4.2 Characteristic Phase of a Maximal PN Sequence

Each maximal PN sequence has a natural "characteristic" phase which is unique to it. (9) The sequence in this phase position has many useful properties. For example, if a maximal PN sequence in its characteristic phase is sampled by every other bit, the result is the same sequence. The required relative phases of the preferred pair of maximal sequences in order to generate balanced members of the code family are described with reference to their characteristic phase and hence it is necessary to show how the characteristic phase and the shift register initial conditions which determine the characteristic phase are determined.

If f(x) is the n^{th} degree binary polynomial corresponding to the maximal PN shift register, than any phase of the maximal sequences generated by the shift register can be represented by the ratio g(x)/f(x), where g(x) is a binary polynomial of degree less than n. Long division of these polynomials results in a formal binary power series whose binary coefficients are the bits of the sequence generated by the shift register. The formula for the polynomial g(x) which results in the characteristic phase for the maximal sequence has been shown $\binom{9}{}$ to be

$$g(x) = \frac{d(x f(x))}{dx}$$
 for $f(x)$ of odd degree

$$g(x) = f(x) + \frac{d(x f(x))}{dx}$$
 for $f(x)$ of even degree

Here differentiation is carried out in the usual way and then the coefficients are interpreted modulo 2.

For example, the characteristic phase for the maximal PN sequence generated by the 3-stage shift register corresponding to the polynomial $f(x) = 1 + x^2 + x^3$ is found as follows:

$$g(x) = \frac{d(x f(x))}{dx} = \frac{d(x + x^3 + x^4)}{dx} = 1 + 3x^2 + 4x^3 = 1 + x^2$$
.

The characteristic phase for maximal sequences is thus represented by the quotient

$$\frac{1+x^2}{1+x^2+x^3} = 1 + 0 \cdot x + 0 \cdot x^2 + \dots$$

and the initial conditions of the 3-stage shift register which will result in the characteristic phase are [100].

5.4.3 Relative Phases Required for Balanced Codes

The relative phases in which the preferred pair of maximal PN sequences must be added in order to result in a balanced member of the family may now be described in terms of the characteristic phases of the preferred pair.

Let a and b be the preferred pair of maximal sequences in their characteristic phase. It is easily seen from the polynomial representation that a characteristic maximal sequence generated by a shift register with an odd number of stages has its initial bit equal to one. Any relative phase shifts of the sequences a and b which are obtained by shifting the sequence b until its initial one corresponds to a zero in the sequence a will result in a balanced Gold code when the two sequences are added together. For example, if the two maximal characteristic sequences a and b are given as:

$$b = 1001011$$

shifting the sequence b cyclically three, five or six positions to the right places the initial one of the characteristic sequence b under a zero of the sequence a. Adding the two sequences in each case produces a balanced code, e.g.,

$$a = 1 1 1 0 1 0 0$$

$$b_3 = 0 1 1 1 0 0 1$$

$$a+b_3 = 1 0 0 1 1 0 1$$

$$a = 1 1 1 0 1 0 0$$

$$b_5 = 0 1 0 1 1 1 0$$

$$a + b_5 = 1 0 1 1 0 1 0$$

$$a = 1 1 1 0 1 0 0$$

$$b_6 = 0 0 1 0 1 1 1$$

$$a + b_6 = 1 1 0 0 0 1 1$$

Shifting the sequence b by any other phase and adding the resultant sequences yields an unbalanced code:

$$a = 1 1 1 0 1 0 0$$

$$b_1 = 1 1 0 0 1 0 1$$

$$a+b_1 = 0 0 1 0 0 0 1$$

5.4.4 Determination of Initial Conditions

The initial conditions for the Gold code generator which will result in balanced codes is now readily determined. The required shift register configuration is shown in Figure 5.4-1.

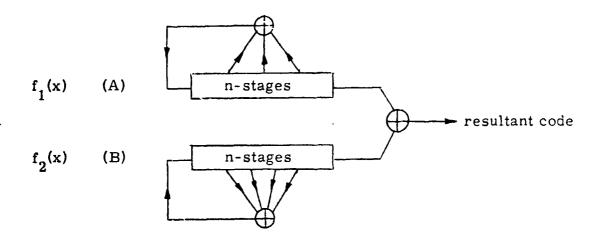


Figure 5.4-1. Code Generator Configuration

1

•

The initial conditions for the shift register (B) corresponding to the polynomial $f_2(x)$ are those initial conditions which determine the characteristic phase of the maximal PN sequence generated by shift register (B). These initial conditions are determined from the representation of the characteristic sequence $\left[d\left(x\,f_2(x)\right)/dx\right]/f_2(x)$ by taking the first n coefficients obtained by performing the indicated long division.

The initial conditions for the shift register (A) corresponding to the polynomial $f_1(x)$ are only subject to the constraint that the first stage contain a zero. This corresponds to a relative phase shift of the characteristic sequences a and b such that sequence a is shifted such that its initial bit corresponds to a zero in the sequence b. We have noted in Section III that the sum of two such relative phase shifts results in a balanced Gold code.

As an example of the above technique, we construct the shift register configuration required to generate balanced Gold codes of period (2¹⁹-1). A preferred pair of 19-stage maximal polynomials is found in the table contained in (10).

(A)
$$2105575 - 1 + x^2 + x^3 + x^4 + x^5 + x^6 + x^8 + x^9 + x^{11} + x^{15} + x^{19}$$

(B)
$$2000605 - 1 + x^2 + x^7 + x^8 + x^{19}$$

The characteristic sequence generated by the shift register corresponding to the polynomial (B) is represented by the ratio

$$\frac{g(x)}{1+x^2+x^7+x^8+x^{19}} \quad \text{where } g(x) = \frac{d}{dx}(x+x^3+x^8+x^9+x^{20}) = 1+x^2+x^8$$

and the initial conditions required for the register (B) are found as the coefficients of the quotient of the two polynomials:

$$\frac{1+x^2+x^8}{1+x^2+x^7+x^8+x^{19}} = 1+x^7+x^9+x^{11}+x^{13}+x^{14}+x^{17}+x^{18}+\dots$$

Initial condition for (B) register = [1 0 0 0 0 0 0 1 0 1 0 1 0 1 1 0 0 1 1].

The only constraint on the initial conditions of the (A) register is that the entry in the first stage be zero. Given that 2^k different codes are required, e.g., 32 codes for the TDRS forward link, then a simple configuration for the initial conditions of the A register is to set stages 1 and k+2 through n to zero while each of the remaining 2^k possible initial conditions for the k stages 2 through k+1 determine 2^k distinct balanced Gold codes. The resultant configuration for the generation of balanced Gold codes of period 2^{19} -1 is shown in Figure 5.4-2.

\$

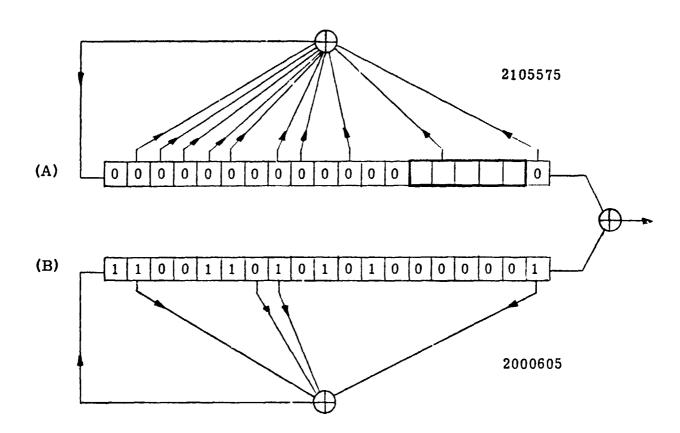


Figure 5.4-2. Generation of Balanced Codes of Period 2¹⁹-1

5.5 The Effect of Clock Error on Acquisition

5.5.1 Introduction

In this section, we consider the effect of clock error on acquisition of a PN signal. We suppose that the chipping rate c of the received signal is in error by one part in n and we compute the acquisition time of the received signal as a function of the error free acquisition time and the ratio r = n/c of clock accuracy to chipping rate. We find that the effect of clock error on the acquisition time increases with increasing error-free acquisition time (no clock error). This is to be expected, since the effect of clock error is to cause the received code to become increasingly decorrelated with time. Specifically, for an error-free acquisition time of not more than 20 seconds, a ratio of clock accuracy to chipping rate of 4×10^2 will add less than 1 second to the acquisition time.

5.5.2 Notation

ŧ.

Let ϵ = clock error in chips/sec. Let ρ = code rate in chips/sec. Then, $(\frac{\epsilon}{\rho}) = \frac{1}{n} = \text{clock accuracy}$ $\Delta = \frac{1}{\rho} = \text{correct chip width}$ $\Delta_{c} = \frac{1}{\rho + \epsilon} = \text{erroleous chip width}$ $\Delta_{c} = \frac{1}{\rho + \epsilon} = \frac{1}{\rho} \left(\frac{1}{1 + \frac{\epsilon}{\rho}}\right) \sim \Delta \left(1 - \frac{\epsilon}{\rho}\right) = \Delta \left(\frac{n-1}{n}\right).$

5.5.3 Analysis

Suppose the received and reference codes are in sychronism and that the clock is in error by $(\frac{\epsilon}{r}) = \frac{1}{n}$. Since the ratio of the correct chip width to the erroneous chip width is $\frac{n-1}{n}$, each successive chip becomes decorrelated by an additional $\frac{1}{n}$ of its width and the codes are completely decorrelated after n chips.

The correlation function between the received and reference codes when the clock is in error by $\frac{1}{n}$ may be written as

$$\mathbf{6} = \left[\mathbf{a}(0) \, \mathbf{a}(0) \, (\frac{\mathbf{n} - \mathbf{1}}{\mathbf{n}}) + \mathbf{a}(0) \, \mathbf{a}(1) \frac{1}{\mathbf{n}} \right] + \left[\mathbf{a}(1) \, \mathbf{a}(1) \, (\frac{\mathbf{n} - 2}{\mathbf{n}}) + \mathbf{a}(1) \, \mathbf{a}(2) \frac{2}{\mathbf{n}} \right]$$

$$+ \cdots \left[\mathbf{a}(i) \, \mathbf{a}(i) \, \frac{\mathbf{n} - (i+1)}{\mathbf{n}} + \mathbf{a}(i) \, \mathbf{a}(i+1) \, (\frac{i+1}{\mathbf{n}}) \right] + \cdots$$

$$\theta = \sum_{i=0}^{n} a(i) a(i) \frac{n - (i+1)}{n} + \sum_{i=0}^{n} a(i) a(i+1) (\frac{i+1}{n})$$
.

Since the out-of-phase terms are uncorrelated, the second sum may be taken as zero, and we have

$$\theta = \frac{1}{n} \sum_{i=1}^{W} (n-i) = w \left[1 - \frac{w+1}{2n} \right] \sim w \left[1 - \frac{w}{2n} \right],$$

where w is the number of chips over which we integrate.

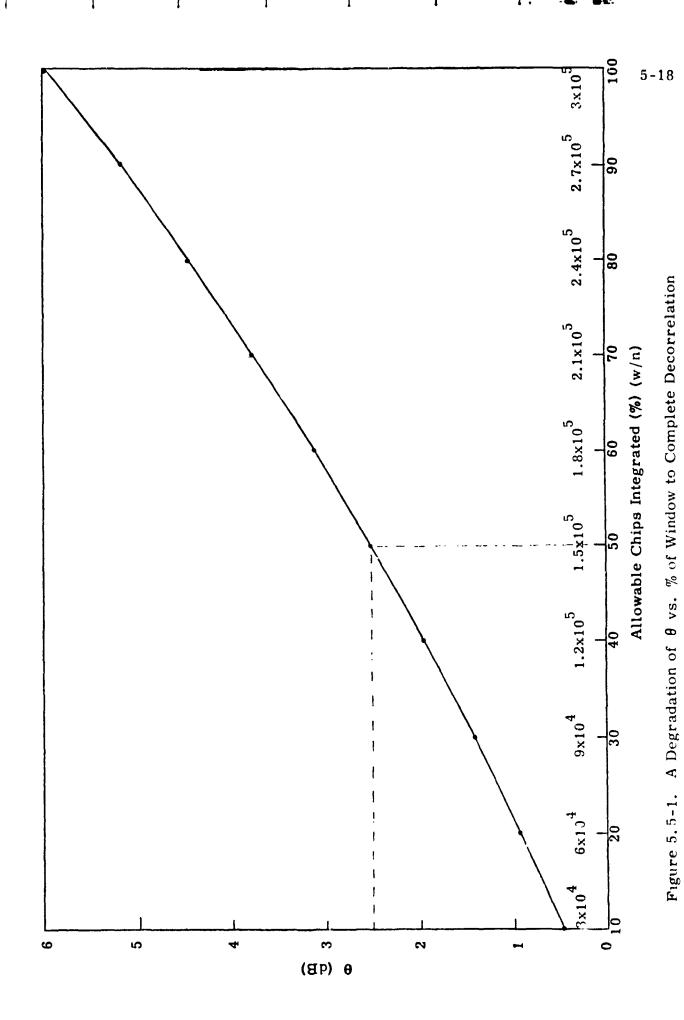
The ratio of the correlation function when the clock is correct to the correlation function when the clock is in error is given by $\left[1 - \frac{w}{2n}\right]$ and the maximum degradation which is achieved for w = n is seen to be 6 dB. A plot of the degradation of θ as a function of the number of chips integrated is given in figure 5.5-1.

For a 6000 Hz doppler on the S-band carrier, the maximum doppler on the PN clock is approximately $\varepsilon = 10$ chips/sec, which results in a clock accuracy of $n = 3 \times 10^5$. The degradation in the correlation function as a function of the integration interval is shown in figure 5.5-1.

5.5.4 Effect of Clock Accuracy on Integration Time

The starting point of this analysis is the following equation which was derived in Section 4.0, where acquisition time $T_{\underline{a}}$ for an accurate clock is given by

$$T_a = \frac{P_i}{\theta^2} \left(\frac{E}{N_0} \right) \left(\frac{N_0}{S} \right) .$$



Using the conclusion of the above section, we have

$$\theta' = \theta(1 - \frac{Tc}{2n})$$

where θ' = degraded correlation function

n = clock accuracy (i.e., 1 part in n)

T = new acquisition time

c = chipping rate.

Ş.

Ţ

Substituting θ' into the equation for T_a , we have

$$T = \frac{P_i\left(\frac{E}{N_0}\right)\left(\frac{N_0}{S}\right)}{\theta^2\left(1 - \frac{Tc}{2n}\right)^2} = \frac{T_a}{\left(1 - \frac{Tc}{2n}\right)^2} = \frac{T_a}{\left(1 - \frac{T}{2r}\right)^2}$$

where r is the ratio of clock accuracy to chipping rate.

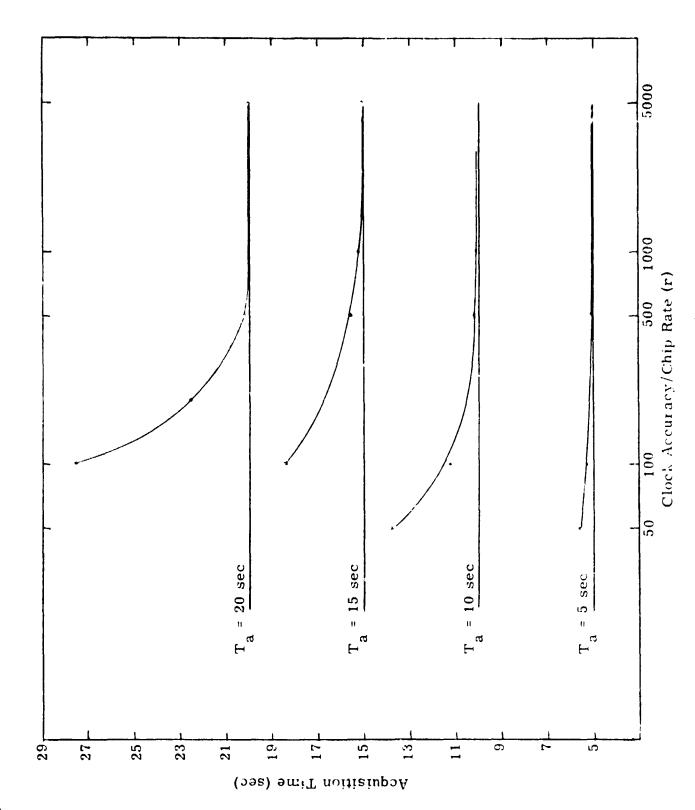
This equation may be used to compute T, the acquisition time with clock error as a function of r, the ratio of clock accuracy to chipping rate with T_a , the acquisition time with an accurate clock as a parameter.

For large r $(\frac{T}{2r} << 1)$, we have

$$T = \frac{T_a}{(1 - \frac{T}{r})}$$

$$T = \frac{r - \sqrt{r^2 - 4r T_a}}{2}.$$

The acquisition times are plotted as a function of r for various error-free acquisition times in Figure 5.5-2.



}

Figure 5, 5-2. Acquisition Time vs. Clock Accuracy/Chip Rate

5.6 Code Libraries for TDRS

5.6.1 Forward Link Multiple Access Library

This code library consists of 100 code pairs. The first member of each pair is a code of period $(2^{10}-1) \cdot (256)$ (long code). The second member of each pair is a code of period $(2^{10}-1)$ (short code). The 100 long and short codes are chosen as balanced members of respective Gold families. In what follows, we describe the technique for generating the required library of code pairs.

5.6.1.1 Forward Link Multiple Access Long Code

The code family from which the long code library is selected may be either a set of maximal PN sequences, each of period 2^{18} -1, or a set of balanced Gold codes generated by a preferred pair of maximal PN sequences. The former approach has the advantage of a simpler implementation (18 shift register stages versus 36 shift register stages) and the code library for this approach consists of the listing of maximal PN codes of period (2^{18} -1) given in Appendix E.5.

In what foliows, we describe the shift register configuration to be used for the generation of 127 balanced Gold codes of period 2^{18} -1.

The preferred pair of maximal PN generators used to generate the desired family is selected from the table of Appendix E.5. The description of one such preferred pair is given in table 5.6-1.

Table 5.6-1. Preferred Pairs for Generation of Code Family of Long Codes

Octal Representations	Polynomial
1000201	$1 + x^7 + x^{18}$
1 3 2 5 4 2 7	$1 + x + x^{2} + x^{4} + x^{8} + x^{9} + x^{11} + x^{13} + x^{15} + x^{16} + x^{18}$

The shift register configuration which will generate the desired code family is illustrated in figure 5.6-1.

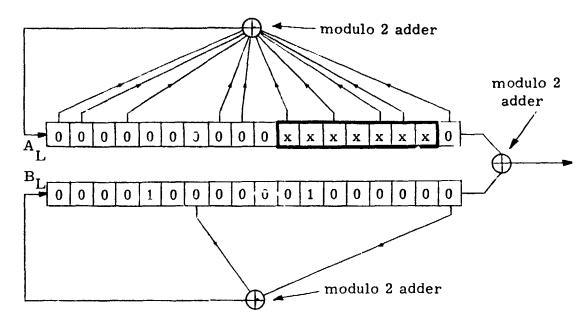


Figure 5.6-1. Long Code Generator Forward Link Multiple Access

In order to generate balanced members of the code family, the relative phases of the two maximal generators must be specified. This is accomplished by requiring that the initial bit of the ${\bf A}_{\bf L}$ register be zero and that the initial conditions of the ${\bf B}_{\bf L}$ register be as given in figure 5.6-1. The 7 unspecified initial conditions of the ${\bf A}_{\bf L}$ register will result in 127 balanced Gold codes whose cross-correlation peaks are -48 dB.

Summary of Parameters for Multiple Access Long Code

- (a) A register feedback 1325427 $1 x + x^2 + x^4 + x^8 + x^9 + x^{11} + x^{13} + x^{15} + x^{16} + x^{18}$
- (b) B_L register feedback 1000201 1 + x^7 + x^{18}
- (c) Initial conditions for A register 0000000000xxxxxxxx0
- (d) Initial conditions for B register 00001000001000000

5.6.1.2 Forward Link Multiple Access Short Code

The code family from which the short code library is selected is generated by the preferred pair of 10-stage maximal generators given in table 5.6-2.

Table 5.6-2. Preferred Pair for Generation of Codes for Forward Link Command Channel

Octal Representation	Polynomial
3515	$1 + x^2 + x^3 + x^6 + x^8 + x^9 + x^{10}$
2011	$1 + x^3 + x^{10}$

The shift register configuration which will generate the desired code family is illustrated in figure 5.6-2.

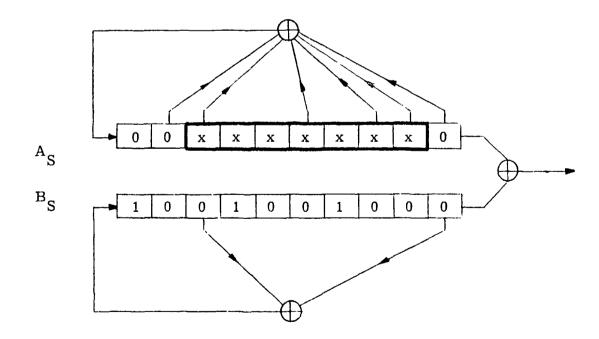


Figure 5.6-2. Short Code Generator Forward Link Multiple Access

As in the case of the generation of the long codes, the relative phases of the two maximal generators must be specified to insure the generation of balanced members of the code family. This is again accomplished by requiring that the initial bit of the A_S register be zero and that the initial conditions of the B_S register be given as in figure 5.6-2. The 7 unspecified initial conditions for the A_S register will result in 127 balanced Gold codes whose cross-correlation peaks are -23.9 dB.

5.6.2 Code Library for Mode 2 Return Link and Its Properties

V.

The code library for the Mode 2 return link consists of 100 code pairs of period (2¹¹-1) selected from the balanced members of a Gold family. The code family from which the code library is selected is generated by the preferred pair of 11-stage maximal generators given in table 5.6-3.

Table 5.6-3. Preferred Pair for Generating Code Library for Mode 2 Return Link

Octal Representation	Polynomial
4445	$1 + x^2 + x^5 + x^8 + x^{11}$
4005	$1 + x^2 + x^{11}$

The shift register configuration which will generate the desired code family is illustrated in figure 5.6-3.

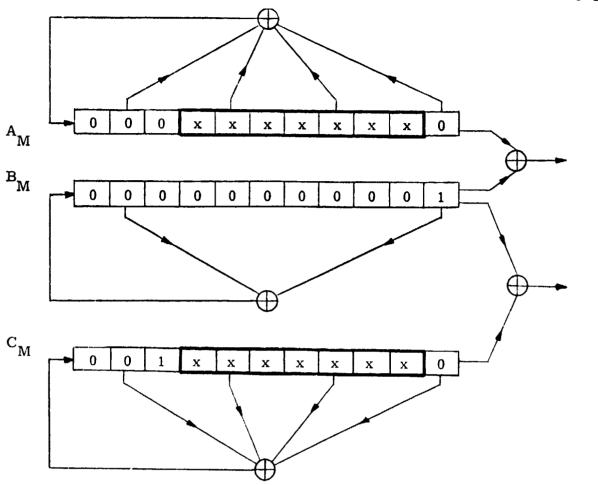


Figure 5.6-3. Generator for Mode 2 Return Link Codes

The requirement that the first bit of the A_M and C_M registers be zero and that the in tial conditions of the B_M register be as indicated in figure 5.6-3 guarantees that the code generator will produce balanced codes. Each subset of initial conditions $[x \ x \ ... \ x]$ of the A_M and C_M registers determines a unique code, while the alternate values of 0 and 1 in the third stage determine the code pair.

Properties of the Code Library for Mod 2 Return Link

The acquisition performance of the Mod 2 return link is dependent upon the distribution of the cross-correlation sidelobes and the RMS value of the cross-correlation function of the code library used for this link. Two algo—thms have been developed which make the determination of this distribution feasible; these procedures are documented in the following sections. In this section, we summarize one of these algorithms

Ţ,

•

and the properties of the recommended Mod 2 return link code family whose implementation was described above.

The cross-correlation sidelobes of any two codes of the recommended family have magnitude 65/2047 or 63/2047, which is approximately 30 dB down from the main correlation peak. The general formula for the number of these sidelobes which occur in the cross-correlation function between two codes a and b of such a family of codes of period 2^n -1 is shown in Appendix A. 5 to be

$$x + y = \frac{\sum_{\theta}^{2} + 2\sum_{\theta} + (2^{n} - 1)}{2^{n+1}}$$

where

$$\sum_{\theta}^{2} = \sum_{\tau=0}^{2^{n}-2} \theta^{2}(a,b)(\tau) = \sum_{\tau=0}^{2^{n}-2} \theta(a,a)(\tau) \theta(b,b)(\tau)$$

$$\sum_{\theta} = \sum_{\tau=0}^{2^{n}-2} \theta(a,b)(\tau) = \theta(a) \cdot \theta(b).$$

The above formula expresses the number of sidelobes in the cross-correlation function of any pair of codes in terms of the parameters of each of the individual codes. Thus, once the required parameters are computed for each member of the family, the number of sidelobes may be determined using the above formula, rather than by the lengthy process of computing the cross-correlation functions. For a family of n codes, the required computation, using this technique, is reduced by a factor of n.

The sidelobe distribution data for the code family of 100 codes described above is given in table 5.6-4. There are (100)(101)/2 = 5050 code pairs and, hence, 5050 cross-correlation functions. The data in the table presents the cumulative frequency function for the number of sidelobes (of magnitude 65 or 63) which occur in each of the 5050 cross-correlation functions. Thus, for example, 104 of the 5050 cross-correlation functions have 1070 sidelobes or more. This cumulative frequency function is plotted in figure 5.6-4.

Table 5.6-4. Probability Distribution of Sidelobes in Mode 2 Codes of Period 2^{11} -1

NO. OF SIDE LOBES	CUM. FREQ.	PROBABILITY DISTRIBUTION
1115 1110	2 3 4	.000 .001
1105		.001
1100	6 7	.001
1095 1090	12	.001 .002
1085	20	.004
1080	39	.008
1075 1070	68 104	.013 .021
1065	166	.033
1060	265	.052
1055 1050	413 594	.082 .118
1045	869	.172
1040	1209	.239
1035 1030	1557 1991	.308 .394
1025	2400	.475
1020	2862	.567
1015 1010	3282 36 7 5	.650 .728
1005	4039	.800
1000	4348	.861
995 990	4564 4755	.904 .942
985	4852	.961
980	4909	.972
975 970	4974 4999	.985 .990
965	5028	.996
960	5034	.997
955 950	5047 5049	.999 1.000
945	5050	1.000

KE 10 X 10 TO THE INCH 46 0782

5.6.3 Dedicated Return Link Mode 1 Code

In this section, we describe a library of code pairs, each consisting of a maximal PN shift register code and a proper phase shift of this code which can be obtained from it via the shift-and-add property discussed in Appendix A.5. The phase difference between the PN codes of each pair is required to be at least 5000 chips. Any prespecified phase shift of a maximal PN code may be generated by taking an appropriate modulo 2 linear combination of the outputs of the taps of the shift register generating the code, as indicated in figure 5.6-5.

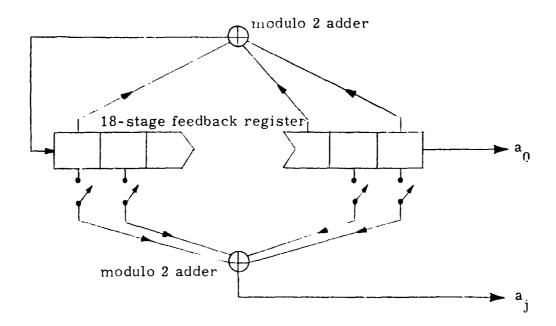


Figure 5.6-5. Generation of Phase Shifts of Maximal PN Sequences

Ξ,

There are 2^{18} -1 settings of the indicated switches, each corresponding to a phase shift a_j ($j=0,1,\ldots,2^{18}$ -1) of the maximal PN sequence a_0 . Thus, any prespecified phase shift a_k may be obtained by the proper switch settings. We may, however, obtain phase shifts in excess of 5000 chips by adding the sequence a_0 to the output sequence obtained from closing one of the switches as indicated in Figure 5.6-6.

This is to be expected, since the probability of a phase shift generated at random being less than 5000 chips is less than 2×10^{-2} . The code library given in Appendix B. 5 lists the phase shift a obtained when the output sequence is added modulo 2 to the output sequence obtained from the kth tap of the shift register. The computer program used for obtaining this data is included in Appendix C. 5.

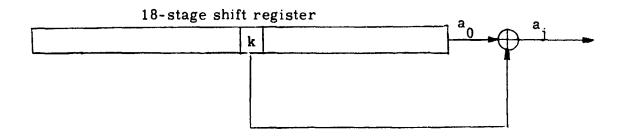


Figure 5.6-6. Generation of Phase-Shifted Version of Maximal PN Code

5.7 Listing of TDRSS User Code Libraries

A listing of the TDRSS user code libraries is contained in table 5.7-1. In what follows, we give a brief description of the contents of this table and reference the appropriate sections of this report for further details.

Column 2 contains the user-unique initial conditions for the seven stages of the 10-stage A register used to generate the 1023 bit code for the forward link command channel, as illustrated in figure 5.6-2. The code generator configuration and the remaining initial conditions for the A and B registers are chosen so that the user-unique initial conditions can consist of the binary representation of the user number.

Column 3 contains the octal representation of the feedback taps for maximal PN generators of period 2¹⁸-1 to be used for the forward link range channel. Each feedback configuration requires no more than six feedback taps.

Column 4 contains the octal representation of the feedback taps for maximal PN generators of period 2^{18} -1 to be used for the Mode 1 return link. These feedback configurations each have the property that, if the output of the first stage is added modulo-2 to the output of the tenth stage, the resultant code differs in phase from the code at the first stage by at least 20,000 chips. The exact phase difference between the two codes is given in Column 5. The numbering of the shift register stages is further described in Appendix B.5. Each feedback configuration of this code library will use no more than eight feedback taps.

Column 6 contains initial conditions for the seven stages of the A and C registers of the configurations generating Mode 2 return link codes, as described in 5.6.2. As in the case of the forward link range channel, these initial conditions may be taken to be the binary representation of the user number.

Column 7 contains the octal representation of the feedback taps for maximal PN generators of period 2¹⁸-1 to be used as Alternate Mode 1 return link codes. No more than six feedback taps are used for any configuration of this library.

Table 5.7-1. Summary of TDRSS Code Litraries

; ,

7	Alternate Mode 1 Return L.nk Feedback Taps	000115	0074	0075	001013	002031	002061		002133	002171	002211	002241	002441	002623	002705	002741	003011		003053	003215	003451	003461	003521	004073	004163	004205
				_			<u>-</u>	- -	<u>-</u>	_		_	~ —	-	_	<u>-</u>	_	<u>-</u>	_		_	_			_	
9	Mode 2 Return Link Initial Conditions Registers A & C	100000	0000	0000	0010000	1010000	0110000	1110000	0001000	1001000	0101000	1101000	001100	1011000	0111000	1111000	0000100	1000100	0100100	1100100	0010100	1010100	0110100	1110100	0001100	1001100
ະກ	Mode 1 Return Link Channel Phase Difference in Chips	94672	5.52	600	37927	20125	127909	124686	48528	122601	130803	42628	121824	81188	61209	36812	66194	53036	74458	104408	102103	17306		32	106369	43037
4	Mode 1 Return Link Feedback Taps	1000047	3150	1263	7 1	S	1101063	1010463	1011267	1010313	1125611	1010211	1011333	1010163	1011533	1010133	1011553	1011347	1116115	1011261	1011571	1012527	254	0770	9	1013525
3	Forward Link Range Channel Feedback Taps	2006601	2 0	2205	2213	2214	2222	223	2.4	2	226	230	2310	3.1	~	c. 23	0.1	2402	2406	2406	243	2510	2514	2602	2604	2606
2	Forward Link Command Channel Initial Conditions Register A		000001		0001	01000	11000	11000	00100	00100	10100	10100	01100	0110	1,100	1110	00010	00010	10010	10010	01010	01010	0 7 0 1 1	11010	20110	001100
1	User Number		٦ ،	4 66	4	. 13	9	. [-	ω		10		175		7	15	91	17	8	61	200	? ?			2 6	25

Table 5.7-1 (continued)

7	Alternate Mode 1 Return Link Feedback Taps		1010051 1010463 1010551
9	Mode 2 Return Link Initial Conditions Registers A & C	101110 011110 0111110 0111110 010001 010001 010001 1110001 100101 100101 100101 111001 111001	0000110 1000110 0100110
ഗ	Mode 1 Return Link Channel Phase Difference in Chips	8 4 6 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	103124 65712 58281
4	Mode 1 Return Link Feedback Taps	0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1	1017511
3	Forward Link Range Channel Feedback Taps		1041011 1041011 1041035
2	Forward Link Command Channel Initial Conditions Register A	0161100 1101100 00111100 10111100 011111.00 1111111.00 1000010 0100010 11110010 11110010 1101010 1101010 1101010 1101010 1101010	0000110 1000110 0100110
1	User Number	22222333333333333333333333333333333333	50 50

Table 5.7-1 (continued)

1 :

. .

7	Alternate Mode 1 Return Link Feedback Taps	1010613	1010615	1010741	1011041	1011245	1310001	1436001	1136001	1561001	1140401	1060401	1360401	1550401	1170401	1104401	1024401	1022401	1446401	1216401	1036401	1101401	1341401	1521401	1305401	1123401
9	Mode 2 Return Link Initial Conditions Registers A & C	1100110	0010110	10:0110	0110110	1110110	0001110	1001110	0101110	1101110	0011110	1011110	0111110	1111110	1000000	1000001	0100001	1100011	0010001	1010001	0110001	1110001	0001001	1001001	0101001	1101001
ક	Mode 1 Return 1. nk Channel Phase Difference in Chips	112199	123092	77447	25412	130143	95337	95661	111502	62504	74581	130032	91020	446	92879	30646	25494	128965	115634	25409	78323	103808	42612	98036	27:78	77632
4	Mode 1 Return Link Feedback Taps	1001625	1017161	1001607	1017071	1001567	1016705	1021473	1021475	1001453	1133015	1001427	1101533	1001361	1402335	1001253	1301323	011	1015631	1001141	1025051	1001023	1021355	1010615	1021363	1000757
3	Forward Link Range Channel Feedback Taps	1041207	4122	4142	1041445	1041451	1041505	1200441	1640441	1320441		1230441		1114441	1422441	£	1046441	N		1111441	1045441	1203441	0	4 0	1460241	1260241
2	Forward Link Command Channel Initial Conditions Register A	1:00110	0 1 1	0 1	-	11011	0001110	1001110	10111	111	01111	01111	1111	11111	000	00000	0000	10000	01000	0100	11000	1 100	0010	0 0	101	101
1	User Number	5.1	22	23	54	55	26	57	28	59	09	61	9	63	9	65	99	67	68	69	70	7.1	72	. r-	7.	75

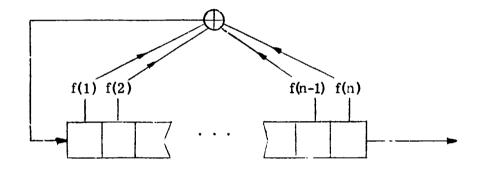
Table 5.7-1 (continued)

7	Alternate Mode 1 Return Link Feedback Taps	1063401	ß	602	702	1204201	0 2 2 2	2 2 2 2	2 2	3220	1446201	1426201	1226201	1116201	1341201		1245201	1215201	3.5	1143201	2320	3		705	
9	Mode 2 Return Link Initial Conditions Registers A & C	0011001	0110	1110	1111001		1001	00	01010	1010101	101	1101		1001101		1101101	0111	1011101	1111	1111101		1000011	0100011	1100011	0010011
2	Mode 1 Return Link Channel Phase Difference in Chips	110203	569	C) (, c) [-) [-] 4	250	179	961	61200	003	651	036	999	583	18	535	106	501	488	45	122484	7 4 8	50633	484
4	Mode 1 Return Link Feedback Taps	6.0	1074	0565	1000143	0062	3052	051	2127	1000407	32424	00035	0207	0034	207	0033	3206	002	724	0117	1726	110	43	000	1016561
3	Forward Link Range Channel Feedback Taps	7	1211241	1031241	P 0	0 9	က	~	1374141	-	141	'n	က	2	003	203	103	413	200	200	100	0 4	240	7 1:0	1462021
2	Forward Link Cor nand Channel Initial Conditions Register A	110	0110	111001	0001	0001	1001	1001	010	0101	1011	1101	0 0 1 1	IIOO	1011	1011	1115	0 1 1 1	1111	11	000	0 0	100	10C	0010011
1	User Number	7.5	77	0 0	80	81	82	83	84		000	2.8	20 G		0.0	 5	7 6	. A	4, 0	93	96	97	86	66	100

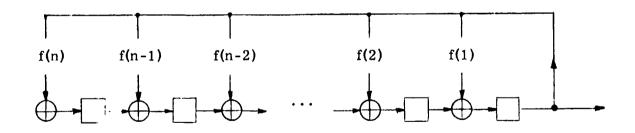
5.8 Modular Implementation of Shift Register Code Generators

()

In this section, we discuss the modular configuration for shift register generators. The output of these shift registers is equivalent to the simple shift registers; however, the modular configuration has some advantages in its hardware implementation. The general n-stage linear shift register and the equivalent n-stage modular register are illustrated below in figure 5.8-1.



(a) n-Stage Simple Feedback Shift Register



(b) n-Stage Modular Shift Register

Figure 5.8-1. Equivalent n-Stage Shift Registers

In figure 5.8-2 below, we illustrate the equivalence between the simple and modular form of the shift register using the ${\bf A}_{\rm S}$ short code generator of figure 5.6-2. The polynomial corresponding to this shift register generator is

1.

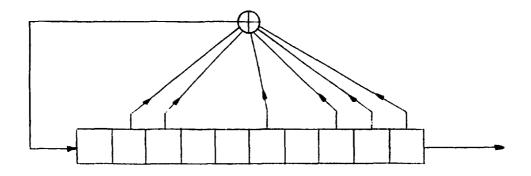
$$f(x) = 1 + x^2 + x^3 + x^6 + x^8 + x^9 + x^{10}$$

and hence

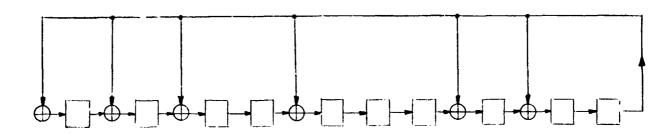
$$f(0) = f(2) = f(3) = f(6) = f(8) = f(9) = f(10) = 1$$

and

$$f(1) = f(4) = f(5) = f(7) = 0$$
.



(a) Simple Feedback Shift Register



(b) Equivalent Modular Shift Register

Figure 5.8-2. Equivalent 10-Stage Simple and Modular Shift Registers

We note that the general rule for constructing the n-stage modular register from the shift register polynomial is that the output of the last stage on the right of the modular register feeds back to the kth stage (counting from left to right) if and only if f(n-k+1) = 1. Thus, in the above example, the output of the tenth stage is fed back to stage k=3 since f(10-3+1) = f(8) = 1.

5.9 References

- 1. N. Zierler, "Linear Recurring Sequences," J. Soc. Indust. Appl. Math., Vol. 7, No. 1, March 1959, 31-48.
- 2. Robert Gold Associates, "Properties of Linear Binary Encoding Sequences," November 1973.
- 3. R. W. Marsh, "Tables of Irreducible Polynomials Over GF(2)
 Through Degree 19," Clearinghouse of Federal Scientific and
 Technical Information, U.S. Department of Commerce, October
 24, 1957.
- 4. W. W. Peterson, Error-Correcting Codes, The MIT Press and John Wiley & Sons, Inc., 1961.
- 5. M. Bradford, "Some Further Generating Polynomials for Binary M-Sequences (U)," DRTE Report No. 1144, Defence Research Telecommunications Establishment, Canada, June 1965.
- 6. E. J. Watson, "Primitive Polynomials (Mod 2)," J. Soc. Indust. Appl. Math., Vol. 10, No. 1, March 1962, 368-369.
- 7. R. Gold, "Optimal Binary Sequences for Spread Spectrum Multiplexing," IEEE Transactions on Information Theory, IT-13, No. 4, October 1967, 619-621.
- 8. R. Gold, "Maximal Recursive Sequences with 3-Valued Recursive Cross-Correlation Functions," IEEE Transactions on Information Theory. Vol. IT-14, No. 1, January, 1968, 154-156.
- 9. R. Gold, "Characteristic Linear Sequences and Their Coset Functions," J. SIAM Appl. Math., Vol. 14, No. 5, September 1966, 980-985.
- 10. W. W. Peterson, Error Correcting Codes, The MIT Press and John Wiley & Sons, Inc., 1961
- 11. Magnavox Co., "TDRSS Telecommunications Study, Phase I Final Report," MRL Report R-4953, September 15, 1974.

APPENDIX A.5

CORRELATION PROPERTIES OF GOLD CODES

A. 5. 1 INTRODUCTION

In this appendix, we give a detailed description and derivation of the two algorithms which may be used to determine the data presented in section 5.6.2.

Let G(a, b) be the family of Gold codes generated by taking all linear combinations of the maximal PN sequences a and b. The cross-correlation function of any two members of the family G(a, b) takes on values which are selected from the values of the cross-correlation function of the maximal sequences a and b. Thus, once a bound on the cross-correlation function of the sequences a and b has been determined, the same bound holds for the correlation function of any two sequences of the family G(a, b).

The distribution of the pross-correlation values and the rms value of the cross-correlation function for any pair of Gold codes are of interest in the calculation of the acquisition performance of these codes. However, although this distribution and rms value have been determined for preferred pairs of maximal sequences and have been used as an approximation to the distribution and rms value for the corresponding family of codes generated by the pair of maximal PN sequences, the precise distribution of correlation values and the rms value for the codes of the family have not been determined. In what follows, we present two algorithms for the determination of the distribution of the cross-correlation values of any pair of Gold codes.

A. 5. 2 RESULTS FOR MAXIMAL PN SEQUENCES

We first note the distribution function of the cross-correlation values of a preferred pair of maximal PN sequences and the rms value of the cross-correlation function of any two maximal PN sequences.

A.5.2.1 Distribution of Correlation Values

The following result holds for the distribution of the 2ⁿ-1 correlation values of a preferred pair of maximal PN sequences of period 2ⁿ-1 (n odd).

$$\frac{\theta(a,b)}{-(2^{(n+1)/2}+1)} = \frac{2^{n-2}-2^{(n-3)/2}}{2^{n-2}+2^{(n-3)/2}}$$

$$\frac{2^{n-2}-2^{(n-3)/2}}{2^{n-2}+2^{(n-3)/2}}$$

$$\frac{2^{n-1}-1}{2^{n-1}-1}$$

We thus note that the cross-correlation sidelobes occur at 2^{n-1} of the 2^n -1 correlation values.

A.5.2.2 RMS Value of Correlation Function of Maximal Sequences

The sum of the squares of the correlation values of any two maximal sequences of period $p=2^n-1$ is given by p^2+p-1 from which the rms value of the distribution of the correlation function is readily computed to be $\sqrt{p+1}-(1/p) \sim \sqrt{p}$ for large periods p. To see this, we use the following relationship between the cross- and autocorrelation function of binary sequences, which is proved in sec. A. 5. 3. 4. 3.

$$\sum_{\tau=0}^{p-1} \theta^{2}(a,b)(\tau) = \sum_{\tau=0}^{p-1} \theta(a,a)(\tau) \theta(b,b)(\tau).$$

Since for maximal linear sequences we have:

$$\theta(a,a)(\tau) = \theta(b,b)(\tau) = p \text{ for } \tau = 0$$

= -1 for $\tau \neq 0$.

$$\sum_{\tau=0}^{p-1} \theta^{2}(a,b)(\tau) = p^{2} + p - 1, \text{ and the result follows.}$$

For p = 15, we have

$$\sum_{\tau=0}^{15} \theta^{2}(a,b)(\tau) = 239.$$

However, we note from Table 2 that, in fact, the sum of the squares of the correlation function for the Gold codes of this example vary from 79 to 623 and, hence, a more precise estimate of their performance than that derived

from the cross-correlation function of the maximal PN sequences which generate the family is desirable. An algorithm to obtain more precise estimates of code performance is discussed in the following section.

A. 5. 3 DERIVATION OF ALGORITHM

In this section, we derive an algorithm for the computation of the precise correlation functions of the Gold codes. The resultant expression will give the cross-correlation values of any two codes of the family in terms of the cross-correlation values and the shift-and-add function of the maximal PN codes which generate the family. In sec. A. 5. 3. 1, we define the shift-and-add function of maximal linear PN sequences and indicate how these functions may be computed efficiently. In sec. A. 5. 3. 2, we describe further properties of Gold codes which are required, and in sec. A. 5. 3. 3, we detail the algorithm for the efficient computation of the cross-correlation function of these codes.

A. 5. 3. 1 Shift-and-Add Function of a Maximal Linear Sequence

Let a₀ be a maximal PN sequence and let a_i denote the sequence obtained from a₀ by cyclically shifting this sequence i positions to the right. Since the modulo-2 sum of a maximal sequence with a proper phase shift of itself is another phase shift of the original sequence (i.e., the shift-and-add property of maximal linear sequences), we have:

$$a_{k} + a_{k+i} = a_{\phi_{a}(i)+k}$$

where ϕ_a is the shift-and-add function of the sequence a. Thus, $\phi_a(i)$ is the shift of the sequence a_k obtained when the sequence a_k is added modulo-2 to an i^{th} cyclic shift of itself. The shift-and-add function of a maximal linear sequence of period 2^n -1 is a permutation of the integers $1, 2, \ldots, 2^n$ -2. This permutation may be determined from a reduced number of values since it is the product of transpositions and, if (i,j) is one of the transpositions, so is (2i,2j).

Thus, for example, for the maximal PN sequence given by a = 1110100:

$$\phi_{\mathbf{a}} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 3 & 6 & 1 & 5 & 4 & 2 \end{pmatrix}$$
$$= (13)(26)(45)$$
$$(2,6) = 2(1,3)$$
$$(4,5) = 2(2,6).$$

Thus, once we have determined that $\phi_a(1) = 3$, the permutation ϕ_a is readily determined.

A. 5. 3. 2 Properties of Gold Family of Codes

The members of the family of codes $G(a_0, b_0)$ consisting of the linear combinations of the maximal PN sequences a_0 and b_0 and all phase shifts of these linear combinations may be represented by all phase shifts of the set of sequences given by

$$g_i = a_0 + b_i$$
 $i = 0, 1, 2, ...$

where b_i denotes the ith cyclic shift of the sequence b_0 . The codes $\{g_i\}_{i=0}^{2^n-2}$ and their proper phase shifts are all distinct, since $(g_i)_{\tau_1} = (g_j)_{\tau_2}$ implies $(a_0 + b_i)_{\tau_1} = (a_0 + b_j)_{\tau_2}$ implies $a_{\tau_1} + b_{i+\tau_1} = a_{\tau_2} + b_{j+\tau_2}$ implies $a_{\tau_1} + a_{\tau_2} + a_{\tau_2} + a_{\tau_3} = a_{\tau_4} + a_{\tau_3} + a_{\tau_4} + a_{\tau_5} = a_{\tau_5} + a_{\tau_5} + a_{\tau_5} = a_{\tau_5} + a_{\tau_5} = a_{\tau_5} + a_{\tau_5} + a_{\tau_5} = a_{\tau_5} = a_{\tau_5} + a_{\tau_5} = a_{\tau_5$

This latter equation implies that phase shifts of two different maximal PN sequences are equal, which is impossible.

We also note that the family of codes G(a,b) is closed with respect to modulo-2 addition, i.e., the modulo-2 sum of any two codes of the family G(a,b) is another member of the family:

$$(g_{i})_{\tau_{1}}^{+} (g_{j})_{\tau_{2}}^{+}$$
 $(a_{0}^{+}b_{i})_{\tau_{1}}^{+} (a_{0}^{+}b_{j})_{\tau_{2}}^{+}$
 $a_{\tau_{1}}^{+} b_{i+\tau_{1}}^{+} a_{\tau_{2}}^{+} b_{j+\tau_{2}}^{+}$

$$a_{1} + \phi_{a}(\tau_{2} - \tau_{1}) + b_{i+\tau_{1}} + \phi_{b}((\tau_{2} - \tau_{1}) + (j-i))$$

$$(a_{0} + b_{k})_{\tau_{3}} = (g_{k})_{\tau_{3}}$$
where
$$k = i + \phi_{b}((\tau_{2} - \tau_{1}) + j - i) - \phi_{a}(\tau_{2} - \tau_{1})$$
and
$$\tau_{3} = \tau_{1} + \phi_{a}(\tau_{2} - \tau_{1}).$$

A.5.3.3 Correlation Function of Gold Codes

To compute the cross-correlation function $\theta(a,b)$ of codes a and b of period 2^n -1, we add the codes in each of their relative phase shifts and count the number of zeroes minus the number of ones in their modulo-2 sum, i.e.,

$$\theta(a,b)(i) = (n_0 - n_1)(a+b_i) = (n_0 - n_1)(g_i)$$
 $i = 0,1,2,...,2^n-2$.

Since the family of codes G(a,b) is closed with respect to modulo-2 addition, the cross-correlation function of any two members g_i, g_j of the family takes correlation values from the set of values $\{\theta(a,b)(i)\}$, i.e.,

$$\theta(g_i, g_j)(t) = (n_0 - n_1)(g_i + g_{j+t}) = (n_0 - n_1)(g_k) = \theta(a, b)(k)$$

for some integer k. Unfortunately, as t varies from 0 to 2^n -2, k does not cover all integers from 0 to 2^n -2 (the mapping from t to k is not one-to-one) and, hence, the distribution of the values of $\theta(g_i,g_j)$ is not the same as the known distribution of the values of $\theta(a,b)$. In what follows, we present an algorithm for the computation of the cross-correlation function $\theta(g_i,g_j)$ of any two members of the family G(a,b) in terms of the cross-correlation function of the maximal PN codes a and b which generate the family.

Theorem: Let
$$g_s$$
 and g_t be any two codes of the family $G(a_0, b_0)$ where $g_s = a_0 + b_s$ and $g_t = a_0 + b_t$. Then,

$$\theta(g_s, g_t)(\tau) = \theta(a, b)(s + \phi_b(t - s + \tau) - \phi_a(\tau)), \qquad \tau \neq 0$$

$$t - s + \tau \neq 0$$

$$= -1, \text{ otherwise.}$$

 ϕ_a and ϕ_b are the shift-and-add functions of the sequences a and b , respectively.

Proof: Case 1 -- $\tau \neq 0$, $t-s+\tau \neq 0$

$$\theta(g_s, g_t)(\tau)$$

$$(n_0 - n_1)(g_s + (g_t)_{\tau})$$
 Number of zeroes - number of ones in $g_s + g_{t+\tau}$

$$(n_0 - n_1)(a_0 + b_s + (a_0 + b_t)_{\tau})$$

$$(n_0 - n_1)((a_0 + a_{\tau}) + (b_s + b_{t+\tau}))$$

$$(n_0 - n_1)(a_{\phi_a(\tau)} + b_{s+\phi_b(t-s+\tau)})$$

$$(n_0 - n_1)(a_0 + b_{s+\phi_b}(t-s+\tau) - \phi_a(\tau))$$

$$\theta (a_{0}^{,b} b_{0})(s + \phi_{b}(t-s+\tau) - \phi_{a}(\tau))$$

Case 2 --
$$\tau = 0$$

$$\theta(g_s, g_t)(0)$$

$$(n_0 - n_1)(g_s + g_t)$$

$$(n_0 - n_1)(a_0 + b_s + a_0 + b_t)$$

 $(n_0 - n_1)(b_s + b_t) = -1$ since b is a maximal linear PN sequence.

The proof for the case $t-s+\tau=0$ is similar.

A. 5. 3. 4 Computational Example of Algorithm

A. 5. 3. 4. 1 G generated by any two maximal PN sequences

In this section, we illustrate the application of the above theorem in an algorithm for the companion of the cross-correlation function of any

two members of the family G(a,b). The required inputs to the algorithm are the cross-correlation function of the maximal sequences a and b and the shift-and-add functions of these sequences. In the following example, we consider the two maximal linear sequences of period 15 and the family $G(a_0,b_0)$ of Gold codes generated therefrom. The shift-and-add functions ϕ_a and ϕ_b and the cross-correlation function of these sequences have been computed and are listed below. The data in Table 1 illustrates the computations required for the determination of the cross-correlation function $\theta(g_2,g_3)$.

Computation of
$$\theta(g_2, g_3)$$

$$\theta(g_s, g_t)(\tau) = \theta(a, b)(s + \phi_b(t - s + \tau) - \phi_a(\tau)) \qquad \tau \neq 0$$

$$t - s + \tau \neq 0$$

= -1, otherwise.

$$\theta(g_2, g_3)(\tau) = \theta(a, b)(2 + \phi_b(1 + \tau) - \phi_a(\tau))$$
 $\tau \neq 0, \tau \neq 14$

= -1, otherwise.

Let
$$\tau' = (2 + \phi_b(1+\tau) - \phi_a(\tau))$$
.

τ	au'	θ (a, b)(τ ¹)	$\theta(g_2,g_3)(\tau)$
			4
0			-1
1	7	-1	-1
2	13	-1	- 1
3	6	3	3
4	11	-1	-1
5	0	-:	- 1
6	2	-5	- 5
7	14	-1	- 1
8	2	-5	- 5
9	0	-1	- 1
10	11	-1	- 1
11	6	3	3
12	13	-1	- 1
13	7	-1	-1
14			

Table 1. Input Data for Algorithm

		0	1	2	3	4	5	6	7	8	9	10	11	12	13	14			
a ₀	=	0	1	1	1	1	0	1	0	1	1	0	0	1	0	0			
^b 0	=	0	0	0	1	0	0	1	1	0	1	0	1	1	1	1			
g ₀	Ξ	0	1	1	0	1	0	0	1	1	0	0	1	0	1	1	θ(g ₀)	= -1	
g ₁	=	1	1	1	i	0	0	1	1	ŭ	ì	1	0	0	1	1	Θ(g ₁)	= -5	
g 2	=	1	0	1	1	1	1	1	0	0	0	ŋ	1	1	1	1	9(g ₂)	= -5	
g ₃	=	1	0	0	1	1	0	0	0	1	0	1	C.	0	0	1	θ(g ₃)	= 3	
$\mathbf{g_4}$	=	1	0	0	0	1	0	1	1	1	1	1	1	1	1	0	θ(g ₄)	= -5	
g ₅	=	0	0	0	0	0	0	1	0	Ú	1	0	1	0	0	1	?(g ₅)	= 7	
g ₆	=	1	1	0	0	0	1	1	0	1	0	0	0	0	1	0	θ(g ₆)	= 3	
g ₇	=	0	0	1	0	0	1	0	O	1	1	1	Э	1	1	1	θ(g ₇)	= -1	
g ₈	=	1	1	0	1	0	1	0	1	1	1	0	1	1	0	1	θ(g ₈)	= -5	
g ₉	-	1	0	1	0	1	1	0	1	0	1	0	0	0	0	0	θ(g ₉)	= 3	
g ₁₀	=	0	0	0	1	0	0	0	1	0	0	0	0	1	1	0	θ(g ₁₀)	= 7	
g ₁₁	=	0	1	0	n	1	1	1	1	0	0	1	0	1	0	1	θ(g ₁₁)	= -1	
٤ ₁₂	=	1	1	1	0	0	0	0	0	0	0	1	1	1	0	0)(g ₁₂)	= 3	
g ₁₃	=	0	0	1	1	0	1	1	1	1	0	1	1	0	0	0	θ(g ₁₃)	= -1	
g ₁₄	=	0	1	0	1	1	1	0	0	0	1	1	1	0	1	0	θ(g ₁₄)	= -1	
				θ (g	;)	= n	um	ber	of	zer	oes	i - 1	num	ber	of	ones	s in g		
		0	1	2	3	4	5	6	7	8	9	10	11	12	13	14			

 ϕ_a - 4 8 14 1 10 13 9 2 7 5 12 11 6 3 ϕ_b - 12 9 4 3 10 8 13 6 2 5 14 1 7 11 $\theta(a,b)$ -1 -5 -5 3 -5 7 3 -1 -5 3 7 -1 3 -1 -1

(_

(F)

As an example of the above computation, we have (see Table 1):

$$\theta(g_2, g_3)(6)$$
 $\theta(a, b)(2 + \phi_b(7) - \phi_a(6))$
 $\theta(a, b)(2 + 13 - 13)$
 $\theta(a, b)(2) = -5$.

A. 5. 3. 4. 2 Case for a and b reverse sequences

\$

The formula for the correlation of members of the code family which was presented in sec. A. 1.4.1 may be simplified in the case where the pair of maximal PN sequences generating the code family consists of sequences which are the reverse of one another. In this case, the formula for the correlation of any pair $g_{\bf g}$, $g_{\bf t}$ of codes of the family becomes

$$\theta(g_s, g_t)(\tau) = \theta(a, b)(s + \phi_b(t - s + \tau) - \phi_b(\tau)) \qquad \tau \neq 0$$

$$\tau + t - s \neq 0$$

$$\tau + t - s \neq 0$$

This simplification follows from the fact that, in this case, we have $\phi_{a}(\tau) = \tau \cdot \phi_{b}(\tau)$ and in any case we have $\phi_{b}(\tau) - \phi_{b}(-\tau) = 0$. Using these two formulas results in the above expression for $\theta(g_{g},g_{t})(\tau)$.

It is also useful to note that, in the present case, the cross-correlation function $\theta(\mathbf{g_s},\mathbf{g_t})$ is symmetric about some value of τ . To see this, we note that $\mathbf{t-s+\tau_0}=-\tau_0$ for τ_0 a solution of the congruence $2\tau = \mathbf{s-t}$ modulo 2^n-1 . Then $\theta(\mathbf{g_s},\mathbf{g_t})$ is symmetric about τ_0 and hence we need only compute the values of $\theta(\mathbf{g_s},\mathbf{g_t})$ at $\tau_0,\tau_0+1,\tau_0+2,\ldots,\tau_0+2^{n-2}-1$. As an example, we again consider the family of Gold codes of period 15 given in sec. A.5.3 4.1. We note from the data of that section.

$$0 \quad 1 \quad 2 \quad ? \quad 4 \quad 5 \quad 6 \quad 7 \quad 8 \quad 9 \quad 10 \quad 11 \quad 12 \quad 13 \quad 14$$

$$\Theta(g_0, g_1) = -1 \quad 7 \quad -1 \quad -5 \quad 3 \quad -1 \quad -1 \quad 3 \quad -1 \quad -1 \quad 3 \quad -5 \quad -1 \quad 7 \quad -1$$

Solving the congruence $2\tau = -1$ modulo 15, we find $\tau_0 = 7$ and note that $\theta(g_0, g_1)$ is in fact symmetric about $\tau_0 = 7$.

A. 5. 3. 4. 3 Proof of basic formulas

In this section, we present the proofs of the basic formulas used in the previous sections.

Theorem: Let a and b be any two binary sequences of period p.

Then:
$$\theta(a,b)(\tau) = \theta(a) \cdot \theta(b)$$
, where

θ(a) = number of zeroes - number of ones in a period of the sequence a

Proof:

C

$$\sum_{\tau=0}^{p-1} \theta(a,b)(\tau)$$

$$\sum_{\tau=0}^{p-1} \sum_{i=0}^{p-1} a(i) b(i-\tau)$$

$$\sum_{i=0}^{p-1} a(i) \sum_{\tau=0}^{p-1} b(i-\tau)$$

$$\left(\sum_{i=0}^{p-1} a(i)\right) \theta(b)$$

$$\theta(a) \theta(b)$$

Theorem: Let a and b be any two binary (+) sequences of period p.

Let
$$\theta(a,b)(\tau) = \sum_{i=0}^{p-1} a(i) b(i-\tau)$$

Then:
$$\sum_{\tau=0}^{p-1} [\theta(a,b)(\tau)]^2 = \sum_{\tau=0}^{p-1} \theta(a,a)(\tau) \theta(b,b)(\tau)$$

Proof: $\sum_{\tau=0}^{p-1} [\theta(a,b)(\tau)]^2$

$$\sum_{\tau=0}^{p-1} \left[\sum_{i=0}^{p-1} a(i) b(i-\tau) \right]^{2}$$

$$\sum_{\tau=0}^{p-1} \sum_{i=0}^{p-1} \sum_{j=0}^{p-1} a(i) a(j) b(i-\tau) b(j-\tau)$$

$$\sum_{i=0}^{p-1} \sum_{j=0}^{p-1} a(i) a(j) \sum_{\tau=0}^{p-1} b(i-\tau) b(j-\tau)$$

$$\sum_{i=0}^{p-1} \sum_{j=0}^{p-1} a(i) a(j) \theta(b,b)(j-i)$$

Letting l = j-i, we have

$$\sum_{\tau=0}^{p-1} \sum_{j=0}^{p-1} a(j) a(j-\ell) \theta(b,b)(\ell)$$

$$\sum_{t=0}^{p-1} \theta(a,a)(\ell) \theta(b,b)(\ell)$$

Theorem: Let F be any family of binary sequences of period p. For any two sequences a, b ϵ F, we have:

$$\sum_{\tau=0}^{p-1} \theta^{2}(a,b)(\tau) \leq \max_{c \in F} \sum_{\tau=0}^{p-1} \theta^{2}(c,c)(\tau)$$

Proof:

0

C

()

$$\sum_{\tau=0}^{p-1} \theta^2(a,b)(\tau)$$

$$\sum_{\tau=0}^{p-1} \theta(a, a)(\tau) \theta(b, b)(\tau)$$
 by previous theorem

$$\leq \int_{\tau=0}^{p-1} \theta^{2}(a,a)(\tau) \int_{\tau=0}^{p-1} \theta^{2}(b,b)(\tau)$$

$$\leq \max_{c \in F} \sum_{\tau=0}^{p-1} \theta^{2}(c, c)(\tau)$$

The following example shows that, in general, this bound cannot be improved. Let $F = \{a, b\}$ where a and b are maximal PN sequences. Then,

$$\sum_{\tau=0}^{p-1} \theta^{2}(a,b)(\tau) = \sum_{\tau=0}^{p-1} \theta(a,a)(\tau) \theta(b,b)(\tau) = p^{2} + p - 1.$$

The significance of this result is that it provides a bound for the rms value of the cross-correlation function of members of a family of sequences F from an examination of the rms values of the autocorrelation function of the members of the family.

Example: Let G be the family of 15 binary PN sequences of the example of sec. A.5.3.4.1 (Table 1). The sum of the squares of the cross-correlation function

$$\sum_{\tau=0}^{p-1} \theta^{2}(g_{i}, g_{j})(\tau)$$

are listed in Table 2. We note that

$$\sum_{\tau=0}^{p-1} \theta^{2}(g_{i}, g_{j})(\tau) \leq \max \sum_{\tau=0}^{p-1} \theta^{2}(g_{i}, g_{j})(\tau) = 623 \text{ for all i, j.}$$

This bound may be reduced to 497 by omitting the sequence g₁ from the family; however, this will not in fact improve the overall cross-correlation bound.

A. 5.4 ALTERNATE TECHNIQUES FOR THE DETERMINATION OF CROSS-CORRELATION FUNCTION OF GOLD CODES

In what follows, we present formulas for the number of times each of the possible three correlation values appears in the cross-correlation function of any two Gold codes. The input data for these formulas depends on the autocorrelation function of the codes being correlated and hence, while some preliminary calculations are required, the determination of

Table 2. Sum of Squares of Cross-Correlation Values of Gold Codes of Period 15

9,1

Ç,

C

. C(_)

C

C

$\theta(g_i, g_j)$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	
0	623	183	183	135	183	255	135	239	183	135	255	239	135	239	239	
1		479	287	239	191	199	271	311	287	79	167	119	143	215	215	
2			479	79	287	167	239	119	191	143	199	215	271	215	311	
3				447	143	151	191	295	271	191	311	231	287	199	199	
4					479	199	79	215	287	271	167	215	239	311	119	
5						463	311	223	167	311	271	159	151	223	159	
6							447	231	143	287	151	199	191	199	295	
7								367	215	199	159	143	199	303	143	
8									479	239	199	311	79	119	215	
9										447	151	295	191	231	199	
10											463	223	311	159	223	
11												367	199	143	303	
12													447	295	231	
13														367	143	
14															367	

000

the distribution function of the sidelobes of the cross-correlation values of a family of Gold codes is reduced by weans of these formulas to a feasible computational problem.

A. 5. 4. 1 Statement of Formulas

Theorem: Let g_1 and g_2 be any two Gold codes of period 2^n -1 (n odd).

The cross-correlation function $\theta(g_1,g_2)$ is known to assume the three values:

$$\theta_1 = -(2^{(n+1)/2} + 1); \ \theta_2 = 2^{(n+1)/2} - 1; \ \theta_3 = -1.$$

The number of times each of these values is assumed is given by

$$N(\theta_1) = \frac{(\sum_{\theta}^2) - (\sum_{\theta})(2^{(n+1)/2} - 2) - (2^n - 1)(2^{(n+1)/2} - 1)}{2^{n+2}}$$

$$N(\theta_2) = \frac{(\sum_{\theta}^2) + (\sum_{\theta})(2^{(n+1)/2} + 2) - (2^n - 1)(2^{(n+1)/2} + 1)}{2^{n+2}}$$

$$N(\theta_3) = \frac{(2^n - 1)(2^{n+1} - 1) - \sum \theta^2 - 2\sum \theta}{2^{n+1}}$$

where

C

C

$$\sum_{\theta} \theta^2 = \sum_{\tau=0}^{2^n-2} \theta^2(g_1, g_2)(\tau) \sum_{\tau=0}^{2^n-1} \theta(g_1, g_2)(\tau)$$

The autocorrelation function of any such Gold code assumes the same three values. The number of times each of these values is assumed in the autocorrelation function is given by

$$N(\theta_1) = \frac{\sum_{\theta}^2 - (\sum_{\theta})(2^{(n+1)/2} - 2) - (2^{2n} - 2^n - 2^{(n+1)/2} + 1)}{2^{n+2}}$$

$$N(\theta_2) = \frac{\sum_{\theta}^2 + (\sum_{\theta})(2^{(n+1)/2} + 2) - (2^{2n} - 2^n + 2^{(n+1)/2} + 1)}{2^{n+2}}$$

$$N(\theta_3) = \frac{(3 \cdot 2^{2n} - 2^{n+2} + 2^n + 1) - \sum_{\theta}^2 - 2\sum_{\theta}}{2^{n+1}}$$

Since
$$\sum_{\tau=0}^{2^{n}-2} \theta^{2}(g_{1},g_{2})(\tau) = \sum_{\tau=0}^{2^{n}-2} \theta(g_{1},g_{1})(\tau) \theta(g_{2},g_{2})(\tau)$$
and
$$\sum_{\tau=0}^{2^{n}-2} \theta(g_{1},g_{2})(\tau) = \theta(g_{1}) \cdot \theta(g_{2}),$$

where $\theta(g_i)$ = number of zeroes - number of ones in the sequence g_i , the number of sidelobes in the cross-correlation function of any two Gold codes may be determined in terms of the parameters of each of the codes itself.

A.5.4.2 Example

Let n=3. We consider the following family of Gold codes:

$$g_0 = 0 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1$$
 $\theta(g_0) = -5$
 $g_1 = 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1$ $\theta(g_1) = 3$
 $g_2 = 0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 0$ $\theta(g_2) = 3$
 $g_3 = 1 \ 0 \ 0 \ 1 \ 1 \ 0 \ 1$ $\theta(g_3) = -1$
 $g_4 = 0 \ 1 \ 0 \ 1 \ 0 \ 0 \ 0$ $\theta(g_4) = 3$
 $g_5 = 1 \ 0 \ 1 \ 1 \ 0 \ 1 \ 0$ $\theta(g_5) = -1$
 $g_6 = 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$ $\theta(g_6) = -1$
 $g_6 = 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$ $\theta(g_6) = -1$
 $g_6 = 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$ $\theta(g_6) = -1$
 $g_6 = 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$ $\theta(g_6) = -1$
 $g_6 = 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$ $\theta(g_6) = -1$
 $g_6 = 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$ $\theta(g_6) = -1$
 $g_6 = 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$ $\theta(g_6) = -1$
 $g_6 = 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$ $\theta(g_6) = -1$
 $g_6 = 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$ $\theta(g_6) = -1$

The product
$$\sum_{\tau=0}^{2^{n}-2} \theta^{2}(g_{i}, g_{j})(\tau) = \sum_{\tau=0}^{2^{n}-2} \theta(g_{i}, g_{i})(\tau) \cdot \theta(g_{j}, g_{j})(\tau)$$
$$= \theta(g_{i}, g_{i}) \cdot \theta(g_{j}, g_{j})$$

is given as follows:

The products $\theta(g_i) \cdot \theta(g_j)$ are given as follows:

	0	1	2	3	4	5	6
0	25	-15	-15	5	-15	5	5
1		9	9	-3	9	-3	-3
2			9	-3	9	-3	-3
3				1	-3	1	1
4					9	-3	-3
5						1	1
6							1

The data in the previous two tables represents the required inputs to the formulas for determining the distribution of sidelobes in the correlation function of any two Gold codes. In this example, the general formulas become:

Cross-Correlation

$$N(\theta_{1}) = \frac{\sum \theta^{2} - 2\sum \theta - 21}{32}$$

$$N(\theta_{2}) = \frac{\sum \theta^{2} + 6\sum \theta + 35}{32}$$

$$N(\theta_{3}) = \frac{105 - 2\sum \theta - \sum \theta^{2}}{16}$$

Autocorrelation

$$N(\theta_{1}) = \frac{\sum_{\theta}^{2} - 2(\sum_{\theta}) - 53}{32}$$

$$N(\theta_{2}) = \frac{\sum_{\theta}^{2} + 6(\sum_{\theta}) - 61}{32}$$

$$N(\theta_{3}) = \frac{153 - 2\sum_{\theta} - \sum_{\theta}^{2}}{16}$$

We note that the distribution of the sidelobes in the case of autocorrelation could be obtained during the computation of

$$\sum_{\tau=0}^{2^{n}-1} \theta(g_{i},g_{i})(\tau);$$

however, the given formulas are useful with respect to unifying the required computer programming.

Using the above formulas, we may compute the following table of sidelobe distributions, $N(\theta_1, \theta_2, \theta_3)$:

A. 5. 4. 3 Proof of Formulas

Let x, y, z be the number of times the values $-(2^{(n+1)/2}+1)$, $(2^{(n+1)/2}-1)$, -1, respectively, occur in the cross-correlation function of two Gold codes, g_1 and g_2 , of period (2^n-1) . We then have the system of equations:

$$x (2^{(n+1)/2} + 1)^{2} + y(2^{(n+1)/2} - 1)^{2} + z = \sum_{\tau=0}^{2^{n} - 2} \theta^{2}(g_{1}, g_{2})(\tau) = \sum \theta^{2}$$

$$x + y + z = 2^{n} - 1$$

$$x - (2^{(n+1)/2} + 1) + y(2^{(n+1)/2} - 1) - z = \sum_{\tau=0}^{2^{n} - 2} \theta(g_{1}, g_{2})(\tau) = \sum \theta$$

Solving this system of equations, we have

$$x = \frac{\sum_{\theta}^{2} - \sum_{\theta} (2^{(n+1)/2} - 2) - (2^{n} - 1) (2^{(n+1)/2} - 1)}{2^{n+2}}$$

$$y = \frac{\sum_{\theta}^{2} + \sum_{\theta} (2^{(n+1)/2} + 2) + (2^{n} - 1) (2^{(n+1)/2} + 1)}{2^{n+2}}$$

$$z = \frac{(2^{n} - 1) (2^{n+1} - 1) - \sum_{\theta}^{2} - 2\sum_{\theta}}{2^{n+1}}$$

The number of sidelobes in the cross-correlation function of two Gold codes, x+y, may be obtained more directly using the following argument.

The possible values for $\theta(a,b)(\tau)$ are $-2^{(n+1)/2}-1$, $2^{(n+1)/2}-1$, -1, and hence the values for $\left[\theta(a,b)(\tau)+1\right]^2$ are 2^{n+1} when there is a sidelobe and 0 when there is no sidelobe. Thus,

$$\sum_{\tau=0}^{n-2} [\theta(a,b)(\tau)+1]^2 = (x+y) \cdot 2^{n+1}$$

or

6

$$(x+y) = \frac{\sum_{\tau=0}^{2^{n}-2} [\theta(a,b)(\tau)+1]^{2}}{2^{n+1}} = \frac{\sum_{\theta}^{2} + 2\sum_{\theta} + (2^{n}-1)}{2^{n+1}}$$

Autocorrelation

In this case, our system of equations is:

$$x (2^{(n-1)^2} + y(2^{(n+1)/2} - 1)^2 + z = \sum_{\tau=0}^{2^n - 2} \theta^2(g,g)(\tau) - (2^n - 1)^2$$

$$x + y + z = 2^n - 2$$

$$x-(2^{(n+1)/2}+1) + y(2^{(n+1)/2}-1) - z = \sum_{\tau=0}^{2^{n}-2} \theta(g,g)(\tau) - (2^{n}-1)$$

Solving this system of equations, we obtain:

$$x = \frac{\sum_{\theta}^{2} - (\sum_{\theta})(2^{(n+1)/2} - 2) - (2^{2n} - 2^{n} - 2^{(n+1)/2} + 1)}{2^{n+2}}$$

$$y = \frac{\sum_{\theta}^{2} + (\sum_{\theta})(2^{(n+1)/2} + 2) - (2^{2n} - 2^{n} + 2^{(n+1)/2} + 1)}{2^{n+2}}$$

$$z = \frac{(3 \cdot 2^{2n} - 2^{n+2} - 2^n + 1) - \sum_{\theta} \theta^2 - 2\sum_{\theta} \theta^2}{2^{n+1}}$$

As in the case of the cross-correlation function, the number of sidelobes in the autocorrelation function of a Gold code, x+y, may be obtained more directly.

The possible values for $\theta(a,b)(\tau)$ are $-2^{(n+1)/2}-1$, $2^{(n+1)/2}-1$, -1, 2^n-1 $(\tau=0)$, and hence the values for $\left[\theta(a,b)(\tau)+1\right]^2$ are 2^{n+1} when there is a sidelobe, 0 when there is no sidelobe, and 2^{2n} (for $\tau=0$). Thus, we have

$$\sum_{\tau=0}^{2^{n}-2} \left[\theta(a,b)(\tau) + 1 \right]^{2} = 2^{2n} + (x+y) 2^{n+1}$$

or

$$(x+y) = \frac{\sum_{\theta}^{2} + 2\sum_{\theta} - (2^{2n} - 2^{n} + 1)}{2^{n+1}}$$

The required computation to obtain the sidelobe distribution in the cross-correlation of Gold codes may be reduced by noting that the sidelobe structure is the same for the pair of codes $\mathbf{g_t}$, $\mathbf{g_s}$ and $\mathbf{g_{2kt}}$, $\mathbf{g_{2ks}}$ for any \mathbf{k} . This follows from the fact that

$$\sum_{\tau=0}^{2^{n}-2} \theta^{2}(g_{t}, g_{s})(\tau) = \sum_{\tau=0}^{2^{n}-2} \theta^{2}(g_{2kt}, g_{2ks})(\tau)$$

and

$$\sum_{\tau=0}^{2^{n}-2} \theta(g_{t}, g_{s})(\tau) = \sum_{\tau=0}^{2^{n}-2} \theta(g_{2kt}, g_{2ks})(\tau)$$

and the number of sidelobes of each kind is seen from the previously derived formulas to depend only upon these quantities. Thus, in the example given for n = 3, the tables of input data may be reduced to:

The table of sidelobe distributions becomes:

G

C

C

A. 5.5 FURTHER PROPERTIES OF GOLD CODES

Result: Let G(a, b) be a family of Gold codes of period 2^n -1 generated by the characteristic maximal linear sequences a_0 , b_0 . Denote $g_i = a_0 + b_i$. Let Ta be the sequence obtained from a by sampling every other term. Then, $T^k(g_i) = g_{i \cdot 2^{n-k}}$.

Proof:
$$T^{k}(g_{i})$$

$$T^{k}(a_{0} + b_{i})$$

$$T^{k}a_{0} + T^{k}b_{i}$$

a + b i. 2m-k by sampling property of characteristic maximal sequences

 $g_{i \cdot 2^{n-k}}$

Example: A Gold family of codes of period $2^4-1 = 15$ is given below.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
g _o	0	1	1	0	1	0	0	1	1	0	0	1	1	0	0
g ₁	1	1	1	0	0	1	1	0	1	1	0	0	1	1	1
g_{2}^{-}	1	1	1	1	1	0	0	0	0	1	1	1	1	1	0
g ₃	1	1	0	0	0	1	0	1	0	0	0	1	1	0	0
g 4	1	0	1	1	1	1	1	1	1	1	•	1	0	0	0
g ₅	0	1	0	0	1	0	1	0	0	1	0	0	0	0	0
g ₆	1	0	1	0	0	0	0	1	0	1	1	0	0	0	1
g ₇	0	1	1	1	0	1	1	1	0	0	1	0	0	1	0
g ₈	1	1	0	1	1	0	1	1	1	0	1	0	1	0	1
g ₉	1	0	0	0	0	. 0	1	0	1	0	1	1	0	1	0
g ₁₀	0	0	1	1	0	0	0	0	1	0	0	0	1	0	0
g ₁₁	0	1	0	1	0	1	0	0	1	1	1	1	0	0	1
g ₁₂	1	0	0	1	1	1	0	0	0	0	0	0	0	1	1
g ₁₃	0	0	0	0	1	1	0	1	1	1	1	0	1	1	0
g ₁₄	0	0	1	C	1	1	1	0	0	0	1	1	1	0	1

We note that

£ ()

$$Tg_1 = T(111001101...) = 11011...$$

$$= g_8 = g_{1 \cdot 2^{4-1}}$$

Result: Let G(a, b) be a family c. Gold codes of period . -1 generated by the characteristic maximal linear sequences a_0 , b_0 . Denote $g_i = a_0 + b_i$. Then,

$$\{\theta(g_s, g_t)(\tau) | \tau = 0, 1, \dots, 2^{n-1}\} = \{\theta(g_{2k_s}, g_{2k_t})(\tau) | \tau = 0, 1, \dots, 2^{n-1}\}$$

for any k.

$$\theta(g_{s}, g_{t})(\tau)$$

$$(n_{0} - n_{1})(g_{s} + (g_{t})_{\tau})$$

$$(n_{0} - n_{1})(a_{0} + b_{s} + a_{\tau} + b_{t+\tau})$$

$$(n_{0} - n_{1}) T^{n-k}(a_{0} + b_{s} + a_{\tau} + b_{t+\tau}) = since n_{0} - n_{1} \text{ in sampled sequence}$$

$$= n_{0} - n_{1} \text{ in original sequence}$$

$$(n_{0} - n_{1})(a_{0} + b_{s} \cdot 2^{k} + a_{\tau} \cdot 2^{k} + b_{t} \cdot 2^{k} + \tau \cdot 2^{k})$$

$$(n_{0} - n_{1})(g_{s} \cdot 2^{k} + (g_{t} \cdot 2^{k})_{\tau} \cdot 2^{k})$$

$$\theta(g_{s} \cdot 2^{k}, g_{t} \cdot 2^{k})(\tau \cdot 2^{k})$$

As τ goes through the numbers $0, 1, \dots, 2^n-1$, so does $\tau \cdot 2^k$, although in a different order. Thus, the result follows.

This latter result shows that the set of correlation values for g_s and g_t is the same as the set of correlation values for g_{2k_S} and g_{2k_t} , and hence the equations:

$$\sum_{\tau=0}^{2^{n}-2} \theta^{2}(g_{s}, g_{t})(\tau) = \sum_{\tau=0}^{2^{n}-2} \theta^{2}(g_{2k_{s}}, g_{2k_{t}})(\tau)$$

and

Ç

10

O

O

$$\sum_{\tau=0}^{2^{n}-2} \theta(g_{s}, g_{t})(\tau) = \sum_{\tau=0}^{2^{n}-2} \theta(g_{2k_{s}}, g_{2k_{t}})(\tau)$$

Using the above results, the data of Table 2 may be reduced to that of the following table.

Table 3. Re	duced Listing	of Cross-	Correlation	Values
-------------	---------------	-----------	-------------	--------

000

(C)

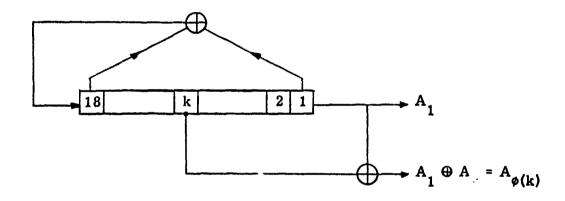
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
0	623	183	183	135	183	255	135	239	183	135	255	239	135	239	239
1		479	287	239	191	199	271	311	287	79	167	119	143	215	215
3				447	143	151	191	295	271	191	311	231	287	199	199
5						463	311	223	167	311	271	159	151	223	159
7								367	215	199	159	143	199	303	143

APPENDIX B. 5

PHASE SHIFT OBTAINED BY ADDITION MODULO 2 OF OUTPUT SEQUENCE AND OUTPUT OF Kth TAP

The following table contains the phase shift obtained when the maximal sequence of period 2¹⁸-1 generated by the shift register corresponding to the listed maximal polynomial is added modulo-2 to the phase-shifted version of the same sequence available at each of the stages of the shift register.

The shift register configuration is illustrated below.



The table lists the phase shift $\phi(k)$ obtained when the sequence A_1 is added to the sequence A_k obtained at the <u>kth</u> stage of the shift register.

For the 100 maximal codes listed, the tap k=10 will yield a maximum phase shift of more than 20,000 chips. The maximum number of feedback taps required for any of the 112 listed generators is 8.

SHIFT	POSITION OF	PHASE SHIFT OF SUM SEQUENCE
REGISTER TAP CONNECTIONS	SECOND TAP	
	K	PHI(K)
1000047	2	125989
1000047 1000047	3	10165
1000047	4 -	112241
1000047	5	20330
1000047	6 7	96872 37661
1000047	8	37007 30947
1000047	9	40660
1000047	10	94672
1000047	11	68399
1000047	12	28005
1000047	13	75322
1000047	14	23897
1000047	15	61894
1000047	16	16045
1000047	17	81320
1000047	18	21624

POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
K	PHI(K)
2	96930
3	68283
4	113163
5	125577
<u>6</u>	116535
7	35817
ğ	116062
	10989
	35529
	29073
	74626 71634
	91302
	30019
	107836
	21978
	45909
	OF SECOND TAP

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
1012622	K	PHI(K)
1012633 1012633	2 3 5 6 7 8 9	43572
	3	87144
1012633	4	127381
1012633	2	87855
1012633	0	45227
1012633	7	7381
1012633	8	13863
1012633		86433
1012633	10	100097
1012633	11	90454
1012633	12	102506
1012633	13	14762
1012633	14	118450
1012633	15	27726
1012633		58664
1012633		89277
1012633	18	31935

TAP	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
	1012715 1012715 1012715 1012715 1012715 1012715 1012715 1012715 1012715 1012715 1012715 1012715 1012715 1012715 1012715	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18	45391 90732 126062 80579 20544 10019 3954 100985 37927 41088 58801 20038 122582 7908 97624 60173 56405

((1)

c

•

O

.

SHIFT OF SUM SEQUENC REGISTER SECOND TAP CONNECTIONS TAP K PHI(K)	
1017551 2 62969 1010551 3 125938 1010551 4 82800 1010551 5 10267 1010551 6 26517 1010551 7 96543	
1010551 8 631 1010551 9 20534 1010551 10 20125	
1010551 11 53034 1010551 12 76220	
1010551 13 69057 1010551 14 127531 1010551 15 1662	
1010551 16 65374 1010551 17 41068 1010551 18 26830	

SHIFT REGISTER	SECOND	PHASE SHIFT OF SUM SEQUENCE
TAP CONNECTIONS	TAP K	PHI(K)
1101063	2	37843
1101063 1101063		75686 98881
1101063	5	110771
1101063	6	130085
1101063	7	64381
1101063	3	47534
1101063	9	40601
1101063		127909
1101063 1101063		197 <u>3</u> 26414
1101063		128762
110106		18943
1101063		95068
110106		109918
1101063		81202
1101063	२ 18	69798

	POSITION	PHASE SHIFT OF
SHIFT	OF	SUM SEQUENCE
REGISTER	SECOND	
TAP CONNECTIONS	TAP	
	K	PHI(K)
1010163	2	20669
1010463	2 3 4	28668
1010463	ភ្	57336
1010463	4	110485
1010463	5 6	114672
1010463	6	104310
1010463	7	23173
1010463	7 8	102626
1010463	9	32799
1010463	10	124686
1010463	11	53523
1010463	12	71542
1010463	13	46346
1010463		115389
1010463		56891
1010463		65488
1010463		65598
1010463	18	115013

T 1 D	SHIFT		PHASE SHIFT OF SUM SEQUENCE
IAP	CONNECTIONS	T A P K	PHI(K)
	1011267	2	65808
	1011267	2 3 4 5 6 7 8 9	130527
	1011267	4	5684
	1011267	5	1089
	1011267	0 7	39749
	1011267 1011267	γ g	11368 52355
	1011267	0	2178
	1011267	10	48528
	1011267	11	79498
	1011267	12	43678
	1011267	13	22736
	1011267	14	44129
	1011267	15	104710
	1011267	16	73446
	1011267	17	4356
	1011267	18	129074

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1010313 1010313 1010313 1010313 1010313 1010313 1010313 1010313 1010313 1010313 1010313 1010313 1010313	17	69277 123589 64382 14965 123891 128764 2663 29930 122601 14361 53592 4615 40054 5326 5594 59860 77369

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
	K	PHI(K)
1125611	2	110099
1125611	3	41945
1125611	4	1533
1125611	5	83890
1125611	6	82283
1125611	7	3066
1125611	2 3 4 5 6 7 8 9	39706
1125611		94363
1125611	10	130803
1125611	11	97577
1125611	12	129371
1125611	13	6132
1125611	14	123547
1125611	15	79412
1125611	16	123310
1125611	17	73417
1125611	18	22468

	HIFT STER	POSITION OF SECOND TAP K	N PHASE SHIFT OF SUM SEQUENCE PHI(K)
	0211	2	127056
	0211 0211	2 3 5 5 7 8 9	8031 52599
	0211	-7 -5	16062
	0211	6	107711
	0211	7	105198
101	0211	8	17771
	0211		32124
	0211	10	42628
	0211	11	46721
	0211	12	47123
	0211	13	51747
	0211	14	98726
	0211	15	35542
	0211	16	121897
	0211	17	64248
101	0211	18	2180

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
THE CONNECTIONS	K	PHI(K)
1011333 1011333	2 3	125793 10557
1011333 1011333 1011333	2 3 4 5 6 7 8 9	108058 21114 2463
1011333 1011333 1011333	7 8 9	46027 81832 42228
1011333 1011333	10 11	121824 49 2 6
1011333 1011333 1011333	13 14	70058 92054 116935
1011333 1011333 1011333	_	98479 38478 84456
1011333	18	103740

فاعتاد الدحظيقون قاجه

č'

e

•

U

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1010163 1010163 1010163 1010163 1010163 1010163 1010163 1010163 1010163 1010163 1010163 1010163	13 14 15 16	108919 44305 71027 88610 15978 120089 63469 84923 81188 31956 6569 21965 70101 126938 24856 92297
1010163	18	71392

REC	SHIFT		PHASE SHIFT OF SUM SEQUENCE
THE COUNTY	2110/42	K	PHI(K)
	011533	2	109089
	011533	23456789	43965 85850
	011533 011533	5	87930
	011533	é	40236
10	011533	7	90443
	011533	8	62483
	011533		86283
	011533 011533		61209 80472
	011533		68904
	011533		81257
	011533	14	36828
	011533	_	124966
	011533		82924
	011533 011533	17 18	89577 116317
1.	U 1 1 7 7 7	(O	110311

TAF	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
		K	PHI(K)
	1010133 1010133	2	104694
	1010133	2 3 4	52755 77029
	1010133		105510
	1010133	5 6	101908
	1010133	7 8	108085
	1010133		108824
	1010133	9	51123
	1010133	10	36812
	1010133 1010133	11	58327
	1010133	12 13	46132
	1010133	14	45973 10648
	1010133	15	44495
	1010133	16	102832
	1010133	17	102246
	1010133	18	11420

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1011553 1011553 1011553 1011553 1011553 1011553 1011553 1011553 1011553 1011553 1011553 1011553 1011553 1011553	11 12 13 14 15	101729 58685 37512 117370 122981 75024 33214 27403 66194 16181 72743 112095 44233 66428 50628 54806 85278

A Secretarian and the second s

C

C

•

	SHIFT REGISTER	POSITION OF SECOND	PHASE SHIFT OF SUM SEQUENCE
TAP	CONNECTIONS	TAP K	PHI(K)
	1011347	2	26633
	1011347	2 3 4 5 6 7 8	53266
	1011347	4	34128
	1011347	5	106532
	1011347	6	90465
	1011347	7	68256
	1011347	8	130139
	1011347	9	49079
	1011347	10	5 3 0 3 6
	1011347	11	81213
	1011347	12	109728
	1011347	13	125631
	1011347	14	103457
	1011347	15	1865
	1011347	16	102654
	1011347	17	98158
	1011347	18	30199

Ü

(c',)

€,

TAP	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
e .	1116115 1116115 1116115 1116115 1116115 1116115 1116115 1116115 1116115 1116115 1116115 1116115 1116115	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18	49146 98292 79151 65559 109802 103841 41796 131025 74458 42539 73403 54461 109218 83592 92552 93

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
	К	PHI(K)
1011261	2	65170
1011261	2 3 4 5 6 7 8	130340
1011261	4	103440
1011261	5	1463
1011261	6	6539
1011261	7	55263
1011261	8	40815
1011261	9	2926
1011261	10	104408
1011261	11	13078
1011261	12	110441
1011261	13	110526
1011261	14	79925
1011261	15	81630
1011261	16	17499
1011261	17	5852
1011261	18	46245

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
THE COMMECTIONS	K	PHI(K)
1011571	2	120780
1011571	2 3 4 5 6 7 8	20583
1011571	4	121799
1011571	5	41166
1011571	6	123121
1011571	7	18545
1011571	8	33727
1011571	9	82332
1011571	10	102103
1011571	11	15901
1011571	12	25502
1011571	13	37090
1011571	74	28367
1011571	15	67454
1011571	16	56481
1011571	17	97479
1011571	18	8166

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
	K	PHI(K)
1012527	2	107643
1012527	2 3 5 6 7 8	46857
1012527	4	112118
1012527	5	93714
1012527	6	85834
1012527	7	37907
1012527	8	62
1012527	9	74715
101 <i>2</i> 527	10	97306
1012527	11	90475
1012527	12	31364
1012527	13	75814
1012527	14	72472
1012527	15	124
1012527	16	122007
1012527	17	112713
1012527	18	46975

TAD	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
171	CONNECTIONS	ĸ	PHI(K)
	1012547	2	3973
	1012547 1012547	2 3 5 6 7 8	7946 80251
	1012547		15892
	1012547	6	25576
	1012547	7	101641
	1012547	8	79868
	1012547	9	31784
	1012547	10	82029
	1012547		51152
	1012547 1012547		94429 58861
	1012547		89109
	1012547		102407
	1012547		128621
	1012547	17	63568
	1012547		9903

A

8

"_

		POSITION	PHASE SHIFT OF
	SHIFT	OF	SUM SEQUENCE
	REGISTER		
TAP CO	ONNECTIONS	TAP	
		K	PHI(K)
	1007705	2	119517
	1007705	3	23109
	1007705	2 3 4	67235
	1007705		46218
	1007705	6	19445
	1007705	5 6 7 8	127673
	1007705	8	62063
	1007705	9	92436
	100 705		88320
	1007705	11	38890
	1007705	12	75428
	1007705		€797
	1007705		8860
	1007705	15	124126
	1007705	16	30767
	1007705	17	77271
	1007705	18	130631

SHIFT REGISTER	POSITION OF SECOND	PHASE SHIFT OF SUM SEQUENCE
TAP CONNECTIONS	TAP K	PHI(K)
1012363	2	79592
1012363 1012363	2 3 4 5 6 7 8 9	102959 116388
1012363	5	56225
1012363	6	39135
1012363 1012363	7	29367 :29619
1012363	9	112450
1012363	10	106369
1012363 1012363	11 12	78270 33952
1012363	13	58734
1012363	14	69808
1012363 1012363	15 16	2905 91035
1012363	17	37243
1012363	18	57988

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
	K	PHI(K)
1013525	2	54440
1013525	2 3 4 5 6	103880
1013525	4	86343
1013525	5	44383
1013525	6	56316
1013525	7 8	89457
1013525	8	98147
1013525	9	88766
1013525	10	43037
1013525		112632
1013525	12	1348
1013525		83229
1013525 1013525		45498
1013525		65849
1013525		68680
1013525		84611
1013723	10	29623

E.

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
	K	PHI(K)
1201011	2	89998
1201011	2	82147
1201011	j ji	19196
1201011	2 3 4 5 6	
1201011	6	97849
1201011	7	75595
1201011	7 8	38392
	0	125173
1201011	9	66445
1201011	10	38185
1201011	11	110953
1201011	12	2333
1201011	13	76784
1201011	14	92305
1201011	15	11797
1201011	16	114324
1201011	17	129253
1201011	18	68333

	POSITION	PHASE SHIFT OF
SHIFT	OF	SUM SEQUENCE
REGISTER		
TAP CONNECTIONS		
THE COMMECTIONS	TAP	
	K	PHI(K)
1007543	2	124152
1007543	- 3	13839
1007543	2 3 4 5 6 7 8 9	101302
1007543	Ē	27678
	2	
1007543	0 ~	16408
1007543	7	59539
1007543	8	28526
1007543		55356
1007543	10	117247
1007543	11	32816
1007543	12	56175
1007543		119078
1007543		16287
1007543		5 7 052
1007543		128516
1007543		110712
1007543	18	34854

SHIF REGISTE TAP CONNECTION	R SECOND	PHASE SHIFT OF SUM SEQUENCE PHI(K)
101362 101362 101362 101362 101362 101362 101362 101362 101362 101362	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	33103 66206 37898 129731 50960 75796 11097 2681 98985 101920 111316 110551 30138
101362 101362 101362 101362	5 15 5 16 5 17	22194 90110 5362 116167

€', }

€,

C

G

C

•

SHIFT REGISTER TAP CONNECTIONS	SECOND TAP	SUM SEQUENCE
	K	PHI(K)
1007501	2	8995
1007501	3	17990
1007501	4	126325
1007501	2 3 4 5 6	35980
1007501	. 6	37480
1007501	7	9493
1007501	8	97298
1007501	9	71960
1007501	10	46045
1007501	11	74960
1007501	12	125775
1007501	1 13	18986
1007501	14	118694
1007501	15	67547
1007501	16	30116
1007501	17	118223
1007501	18	121642

SHIFT REGISTER TAP CONNECTIONS	SECOND	PHASE SHIFT OF SUM SEQUENCE
THE CONNECTIONS	K	PHI(K)
1014555	2	120780
1014555	2 3 4 5 6 7 8 9	20583
1014555	4	99265
1014555 1014555	2	41166
1014555	7	1139 63613
1014555	ģ	26800
1014555	à	82332
1014555		43892
1014555		2278
1014555		120376
1014555	13	127226
1014555	14	9609
1014555		53600
1014555		104233
1014555		97479
1014555	18	95955

SHIFT REGISTER	POSITION OF SECOND	PHASE SHIFT OF SUM SECUENCE
TAP CONNECTIONS	TAP K	PHI(K)
	N.	1112(11)
1007817	2	47663
1007417	3 4	95326
1007417	4	4784
1007417	5 6	71491
1007417	6	116Jó }
1007417	7 8	9568
1007417		44697
1007417	9	119161
1007417	10	91623
1007417	11	30005
1007417	12	95394
1007417	13	19136
1007417	14	111168
1007417	15	89394
1007417	16	47278
1007417	17	23821
1007417	18	18781

ТАР	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
,,,,		K	PHI(K)
	1716201	2	111722
	1716201	3 4 5 6 7 8	38699
	1716201	14	115196
	1716201	5	77398
	1716201	6	122836
	1716201	7	31751
	1716201	8	3357
	1716201	9	107347
	1716201	10	124677
	1716201	11	16471
	1716201	12	82084
	1716201	13	63502
	1716201	14	28953
	1716201	15	6714
	1716201	16	90728
	1716201	17	47449
	1716201	18	76794

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
TRY CONNECTIONS	K	PHI(K)
1007315	2	20641
1007315	3	41282
1007315	4	43663
1007315	5	82564
1007315	6	24679
1007315	7	87326
1007315	2 3 4 5 6 7 8 9	67491
1007315	9	97015
1007315	10	124514
1007315	11	49358
1007315	12	20716
1007315	13	87491
1007315	34	78725
1007315	15	127161
1007315	16	31200
1007315	17	68113
1007315	18	2810

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
TAP CONNECTIONS	K	PHI(K)
1015037	2	123111
1015037	3	15921
1015037	4	29670
1015037	5	31842
1015037	6	61993
1015037	7	59340
1015037	2 3 4 5 6 7 8 9	110272
1015037	9	63684
1015037	10	25407
1015037	11	123986
1015037	12	38778
1015037	13	118680
1015037		23157
1015037		41599
1015037		116340
1015037		127368
1015037		16787

SHIFT	POSITION OF	PHASE SHIFT OF SUM SEQUENCE
REGISTER	SECOND	
TAP CONNECTIONS	TAP	5.1.5 / rs \
	K	PHI(K)
	_	•
1007263	2 3. 4 5 6	49910
1007263	3∙	99820
1007263	Ħ	7 386
1007263	5	62503
1007263	6	128667
1007263	7	14772
1007263	7 8	60767
1007263	9	125006
1007263	10	79938
1007263	11	4809
1007263	12	113194
1007263	13	29544
1007263	14	34789
1007263	1 5	121534
1007263		74419
1007263	17	12131
1007263	18	112531
,00,203	. •	116731

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1230121 1230121 1230121 1230121 1230121 1230121 1230121 1230121 1230121 1230121 1230121 1230121 1230121 1230121	234567890112314561718	55144 110288 111085 41567 99045 39973 67113 83134 53510 64053 107694 79946 6656 127917 84263 95875 58527

i. (_

E

ľ

TAD	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
1.41	COMMECTIONS	K	PHI(K)
	1014365	2	29048
	1014365	2 3 5 6 7 8 9	58096
	1014365	4	17471
	1014365	5	116192
	1014365	6	13645
	1014365	7	34942
	1014365	8	10503
	1014365		29759
	1014365		38428
	1014365	11	27290
	1014365	12	103669
	1014365	13	69884
	1014365	14	24555
	1014365	15	21006
	1014365		15851
	1014365		59518
	1014365		127041

()

SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
	K	PHI(K)
1014475	2	56737
1014475	3	113474
	4	101120
	5	35 195
	6	10464
	7	59903
	8	60239
	9	70390
		33738
		20328
		31333
		119806
		56454
		120478
		85344
		121363
1014475	18	118672
	REGISTER CONNECTIONS 1014475 1014475 1014475 1014475 1014475 1014475 1014475 1014475 1014475 1014475 1014475 1014475	SHIFT OF SECOND TAP K 1014475 2 1014475 3 1014475 4 1014475 5 1014475 6 1014475 7 1014475 7 1014475 10 1014475 10 1014475 11 1014475 12 1014475 13 1014475 14 1014475 15 1014475 16

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
4007465	K	PHI(K)
1007165 1007165	2 3 4 5 6 7 8	18934
1007165	5 h	37868
1007165	4	21299
1007165	5	75736
1007165	7	45044
1007165	ά	42598 7825 <i>5</i>
1007165	9	78255 110671
1007165	10	45941
1007165	11	90088
1007165	12	36499
1007165	13	85196
1007165	14	114847
1007165	15	105633
1007165	16	7680
1007165	17	40801
1007165	18	7949

POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
ĸ	PHI(K)
2	11448
3 11	22896 79557
	45792
6	17201
7	103029
	3143
	91584
	30125 34402
	46846
13	56085
	4865
	6286
	50153 78975
18	122016
	OF SECOND TAP K 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17

c()

POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
K	PHI(K)
2	25635
3	51270
4	127449
5	102540
6	82629
7	7245
8	103140
9	57063
10	57531
11	96885
12	55203
13	14490
14	92893
15	55863
16	19152
17	114126
18	114621
	OF SECOND TAP K 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17

TAP	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
••••	OSMABOTTO 45	K	PHI(K)
	1021553	2	47405
	1021553	2 3 4 5 6 7 8	94810
	1021553	4	22061
	1021553 1021553	5	72523
	1021553	7	43913
	1021553	á	44 122
	1021553	9	6934 117097
	1021553		26391
	1021553		87826
	1021553		103968
	1021553		88244
	1021553	14	32423
	1021553		13868
	1021553		72642
	1021553	17	27949
	1021553	18	85283

(C)

POSITION OF SECOND	PHASE SHIFT OF SUM SEQUENCE
TAP K	PHI(K)
2	32336 64672
j i	83291
5	129344
6	117483
7	95561
8	130516
	3455
	83753
	27177
	49645
	71021
	10146
	1111
	127090
	6910
10	129001
	OF SECOND TAP K 2 3 4 5 6 7 8 9 10 11 12 13

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
TAP CONNECTIONS	K	PHI(K)
1020277	2	46819
1020277	2 3 4 5 6 7 8	93638 1270
1020277 1020277	4 5	74867
1020277	6	80681
1020277	7	2540
1020277	8	124474
1020277	9	112409
1020277	10	22264
1020277		100781
1020277		119810
1020277		5080
1020277		80814
1020277		13195
1020277	16 17	99783 37325
1020277 1020277	18	116410
1020211	10	110410

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1001661	2	36517
1001661	3	73034
1001661	4	74422
1001661 1001661 1001661	2 3 4 5 6 7 8	116075 80742 113299
1001651	8	128084
1001661	9	29993
1001661	10	59945
1001661	11	100659
1001661	12	30346
1001661	13	35545
1001661	14	22633
1001661	15	5975
1001661	16	19777
1001661	17	59986
1001661	18	31680

SHIFT REGISTER		PHASE SHIFT OF SUM SEQUENCE
TAP CONNECTIONS	T A P K	PHI(K)
1017611	2	6338
1017611	2 3 4 5 6 7 8 9	12676
1017611	4	16649
1017611	5	25352
1017611	<u>6</u>	39888
1017611	7	33298
1017611	8	29767
1017611		50704
1017611	10	113772
1017611	11	79776
1017611	12	14667
1017611	13	66596
1017611	14	16536
1017611		59534
1017611		32361
1017611	17	101408
1017611	18	35877

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1001651 1001651 1001651 1001651 1001651 1001651 1001651 1001651 1001651 1001651 1001651 1001651 1001651 1001651	234567891011213145161718	69796 122551 86167 17041 117179 89809 127190 34082 106789 27785 396 82525 34309 7763 107267 68164 55203

SHIFT REGISTER	POSITION OF SECOND	PHASE SHIFT OF SUM SEQUENCE
TAP CONNECTIONS	TAP · K	PHI(K)
1017511	2	11550
1317511	2 3 4	23100
1017511	4	32066
1017511	5	46200
1017511	6	40153
1017511	7 8	78011
1017511	8	119271
1017511	9	92400
1017511	10	103124
1017511	11	80306
1017511	12	67560
1017511	13	106121
1017511	14	66481
1017511	15	23601
1017511	16	107278
4 1017511	17	77343
1017511	18	85645

C

 $\epsilon(\cdot)$

•

TAP	SHIFT REGISTER COMMECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
	1001631 1001631 1001631 1001631 1001631 1001631 1001631 1001631 1001631 1001631 1001631 1001631 9001631 9001631	16	47121 94242 85047 73659 105792 92049 74959 114825 65712 50559 94826 78045 55843 118225 80839 32493 106827

SMIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
₹0\$7311	2	80078
1017311	2 3 4 5 6 7 8	101987
1017311	4	105979
1017311	5	58169 107136
# 017311	7	50185
1017311 1017311	į g	52205
1017311	9	116338
1017311	10	58281
1017311		47871
1017311	12	111209
1017311	13	100370
1017311	14	59368
1017311	15	104410
1017311	16	46116
1017311	17	29467
1017311	18	67189

FOOTITON	PHASE SHIFT OF
OF	SUM SEQUENCE
SECOND	
TAP	
K	PHI(K)
2	16096
3	32192
4	62795
5	64384
6	76569
7	125590
	32458
Ò	128768
10	112199
11	109005
12	71923
	10963
14	90666
15	64916
16	119862
17	4607
18	123
	SECOND TAP K 234567891012131451617

SHIFT REGISTER	POSITICN OF SECOND	PHASE SHIFT OF SUM SEQUENCE
TAP CONNECTIONS	TAP K	PHI(K)
	K	1112(117)
1001607	2	41857
1001607	3	83714
1001607	4	24734
1001607	5	94715
1001607	6	76652
1001607	7	49468
1001607	2 3 4 5 6 7 8	17132
1001607	9	72713
1001607	10	77447
1001607	11	108839
1001607	12	68362
1001607	13	98936
1001607	14	120869
1001607	15	34264
1001607	16	121992
1001607	17	116717
1001607	18	93803

	SHIFT REGISTER	POSITION OF SECOND	PHASE SHIFT OF SUM SEQUENCE
TAP C	ONNECTIONS	TAP K	PHI(K)
	1017071	2	104867
	1017071	3 5 6 7 8 9	52407
	1017071	4	35443
	1017071	5	104318
	1077071	6	121608
	1017071	7	70886
	1017071	8	80471
	1017071		52507
	1017071	10	25412
	1017071	11	18927
	1017071	12	24920
	1017071	13	120371
	1017071	14	15524
	1017071	15	101201
	1017071	16	18779
	1017071	17	105014
	1017071	18	12674

	POS1TION	PHASE TIFT OF
SHIFT	OF	SUM SL ENCE
REGISTER	SECOND	
TAP CONNECTIONS	TAP	
	K	PHI(K)
1001567	2	103393
1001567	2 3	55357
1001567	4	59109
1001567		110714
1001567	6	113709
1001567	5 6 7 8	118218
1001567	8	1800
1001567	9	40715
1001567	10	130143
1001567	11	34725
1001567	12	108128
1001567	13	2570 7
1001567	14	123389
1001567	15	3600
1001567	16	67577
1001567	17	81430
1001567	18	87968

ТДР	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
Int	COMMECTIONS	K	PHI(K)
	1016705	2	65052
	1016705	2 3 4 5 6	130104
	1016705	4	107853
	1016705	5	1935
	1016705	6	111638
	1016705	7 8	46437
	1016705	8	57 146
	1016705	9	3870
	1016705	10	95338
	1016705	11	38867
	1016705	12	96974
	1016705	13	92874
	1016705	14	74671
	1016705	15	114292
	1016705 1016705	16	107239
	1016705	17	7740
	1010105	18	36549

βη ;

SHIN REGISTI TAP CONNECTION	ER SECOND	PHASE SHIFT OF SUM SEQUENCE
301101	K	PHI(K)
10214 ⁻ 10214 ⁻		67392
102147	13 3 73 4	127359 90960
10214	73 5	7425
102147	73 6	18208
102147	73 7	80223
102147 102147	/3 8	83430
102147		14850
102147		95561 36416
102147		13695
102147	73 13	101697
102147	-	42897
102147	•	95283
102147 102147		48768
102147		29700 32705
• • • •		7-107

Т	SHIFT REGISTER AP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
		ĸ	BHI(K)
	1021475	2	56372
	1021475 1021475	3 4 5 6	112744 108654
	1021475	5	36655
	1021475	6	18502
	1021475	7 8	44835
	1021475 1021475	8	68180
	1021475	9 10	73310 111502
	1021475	11	37004
	1021475	12	23028
	1021475	13	89670
	1021475	14	81196
	1021475 1021475	15 16	125783
	1021475	17	112648 115523
	1021475	18	16332

SHIFT REGISTER TAP CONNECTIONS	TAP	SUM SEQUENCE
40041152	K	PHI(K) 25624
1001453	2	51248
1001453	2	
1001453	4	114933
1001453	5	102496
1001453	6	71640
1001453	7	32277
1001453	2 3 4 5 6 7 8	77703
1001453	9	57151
1001453	10	62504
1001453		118863
1001453		87493
1001453		64554
1001453		18903
1001453		106737
1001453		63748
1001453		114302
1001453		83404

))

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
(AP CONNECTIONS	K	PHI(K)
1133015	2	28277
1133015	2 3 4 5 6 7 8 9	56554
1133015	4	67044
1133015	5	113109
1133015	6	56421
1133015	7	128055
1133015	8	74148
1133015	9	35927
1133015	10	74581
1133015	11	112842
1133015	12	112659
1133015	13	6033
1133015	14	12677
1133015		113847
1133015		112120
1133015	17	71854
1133015	18	12630

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
the outdoor to the	ĸ	PHI(K)
1001427	2	52744
1001427	2 3 4	105488
1001427		108582
1001427	5	51167
1001427	5 6 7 8	21126
1001427	7	44979
1001427		53263
1001427	9	102334
1001427	10	130092
1001427	11	79891
1001427	12	54116
1001427	13	89958
1001427	14	41060
1001427	15	106526
1001427	16	69839
1001427	17	57475
1001427	18	34141

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1101533 1101533 1101533 1101533 1101533 1101533 1101533 1101533 1101533 1101533 1101533 1101533 1101533 1101533	12 13 14 15	5685 11370 33792 22740 9596 67584 41333 45480 91020 19192 36154 126975 128420 82666 12424 90950 8268

CUTET OF CUM CECUPACE	
SHIFT OF SUM SEQUENCE	
REGISTER SECOND	
TAP CONNECTIONS TAP	
K PHI(K)	
1001361 2 8790	
1001361 3 17580	
1001361 2 8790 1001361 3 17580 1001361 4 18210	
1001361 5 35160	
1001361 6 18158	
1001361 7 36420	
1001361 8 42786	
1001361 9 70320	
1001361 10 94465	
1001361 11 36316	
1001361 12 48857	
1001361 13 72840	
1001361 14 120952	
1001361 15 85572	
1001361 16 69945	
1001361 17 121503	
1001361 18 8591	

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1402335 1402335 1402335 1402335 1402335 1402335 1402335 1402335 1402335 1402335 1402335 1402335	12 13 14 15 16 17	97889 66365 35344 129413 2884 70688 40059 3317 92879 5768 129880 120767 50377 80118 33787 6634
1402335	18	84390

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1001253 1001253 1001253 1001253 1001253 1001253 1001253 1001253 1001253 1001253 1001253 1001253 1001253 1001253 1001253	11 12 13 14 15 16 17	74810 112523 69711 37097 16611 122721 76258 74194 39646 33222 92197 16701 99034 109627 7262 113755 19513

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
the common tend	K	PHI(K)
1301323	2	43456
1301323	2 3 4 5 6 7 8 9	86912
1301323	4	97346 88319
1301323 1301323	6	128775
1301323	7	67451
1301323	8	17183
1301323		85505
1301323		25494
1301323		4573
1301323		80615 127241
1301323		90867
1301323		34366
1301323 1301323		80014
1301323		91133
1301323	18	72790

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1001165	2	61729
1001165	3	123458
1001165	4	69281
1001165	5	15227
1001165	6	85582
1001165	2 3 4 5 6 7 8 9	123581
1001165	8	73098
1001165		30454
1001165	10	128965
1001165	11	90979
1001165	12	4480
1001165	13	14981
1001165	14	93604
1001165		115947
1001165	16	126834
1001165	17	60908
1001165	18	127726

TAP	CHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
	1015631 1015631 1015631 1015631 1015631 1015631 1015631 1015631 1015631 1015631 1015631 1015631 1015631 1015631 1015631	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18	94174 73795 29044 114553 60382 58088 60036 33037 115634 120764 104679 116176 31417 120072 93673 66074 37258

TAP	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
		K	PHI(K)
	1001141	2	85505
	1001141	2 3 4	91133
	1001141	4	110402
	1001141	5	79877
	1001141	5 6 7	34226
	1001141		41339
	1001141	8	14992
	1001141	9	102389
	1001141	10	25409
	1001141	11	68452
	1001141	12	23309
	1001141	13	82678
	1001141	14	18414
	1001141	15	29984
	1001141	16	30916
	1001141	17	57365
	1001141	18	1695

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1025051 1025051 1025051 1025051 1025051 1025051 1025051 1025051 1025051 1025051 1025051 1025051 1025051 1025051	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16	55834 111668 52553 38807 83433 105106 33388 77614 78323 95277 778 51931 110554 66776
1025051	18	106915 125806

_

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1001023 1001023 1001023 1001023 1001023 1001023 1001023 1001023 1001023 1001023 1001023 1001023 1001023 1001023 1001023	12 13 14 15 16	63208 126416 47311 9311 90307 94622 124474 18622 103808 81529 92537 72899 88243 13195 80481 37244 2954

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
	K	PHI(K)
1021355	2	84968
1021355	2 3 4 5 6 7 8 9	92207
1021355 1021355	4 E	12 1075 77729
1021355	6	126397
1021355	Ž	19993
1021355	8	110171
1021355		106685
1021355	10	42612
1021355		9349
1021355		101246
1021355 1021355		39986 65972
1021355		41801
1021355		15001
1021355	17	48773
1021355	18	65038

SHIFT	POSITION OF	PHASE SHIFT OF SUM SEQUENCE
REGISTER	SECOND	SOLI SEQUENCE
TAP CONNECTIONS	TAP K	DUT/V)
	K	PHI(K)
1010615	2	114760
1010615	3 5 6 7 8 3	32623
1010615	4	43589
1010615	5	65246
1010615	<u>6</u>	97291
1010615	7	87178
1010615	8	73503
1010615		130492
1010615	10	98036
1010615	11	67561
1010615	12	42818
1010615	13	87787
1010615	14	48025
1010615	15	115137
1010615	16	97401
1010615	17	1159
1010615	18	79179

TAP	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
		K	PHI(K)
	1021363	2	116502
	1021363 1021363	2 3 4 5 6 7 8	29139
	1021363	5	53247 58278
	1021363	6	32940
	1021363 1021363	8	106494 21595
	1021363	9	116556
	1021363 1021363	10 11	27778 65880
	1021363	12	73781
	1021363 1021363	13 14	49 155 29 7 95
	1021363	15	43190
	1021363 1021363	16 17	41519
	1021363	18	29031 115446

·D

8

. Let

	POSITION	PHASE SHIFT OF
SHIFT	or	SUM SEQUENCE
REGISTER	SECOND	
TAP CONNECTIONS	TAP	
	ĸ	PHI(K)
1000757	2	3265
1000757	2 3	6530
1000757	4	73075
1000757	5	13060
1000757	6	9785
1000757	7	115993
1000757	8	94193
1000757	9	26120
1000757	10	77032
1000757	11	19570
1000757	12	30886
1000757	13	30157
1000757	14	127370
1000757		73757
1000757	16	89729
1000757	17	52240
1000757	18	98580

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1060065	2	7311
1060065 1060065	2 3 4	14622 46381
1060065	5	29244
1060065	6	80975
1060065	7	92762
1060065	8	41684
1060065	9	58488
1060065	10	110203
1060065	11	100193
1060065	12	112367
1060065	13	76619
1060065	14	29049 83368
1060065 1060065	15 16	121710
1060065	17	116976
1060065	18	30453

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
	K	PHI(K)
1010741	2	127874
1010741	2 3 4 5 6 7	6395
1010741	Ц	63516
1010741	5	12790
1010741	б	52184
1010741	7	127032
1010741	8	78180
1010741	9	25580
1010741	10	75695
\$010741		124368
1010741		39336
1010741		8079
1010741		52160
1010741		105783
10 4 0741		10583
† 01074†	17	51160
1010741	18	111061

SHIFT RÆGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1205651 1205651 1205651 1205651 1205651 1205651 1205651 1205651 1205651 1205651 1205651 1205651 1205651 1205651 1205651	2 3 4 5 6 7 8 9 9 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	84556 93031 \$05166 76081 38963 51811 119487 105981 98275 77926 30692 103622 113547 23169 119270 42181 93526

Ü

١.

()

^

SHIFT REGISTER		PHASE SHIFT OF SUM SEQUENCE
TAP CONNECTIONS	TAP	DUT (4)
	K	PHI(K)
100071/3	2	19416
1000743	วั	38832
1000743	Ú	16811
1000743	2 3 4 5 6 7 8	77664
1000743	6	24907
1000743	7	30622
1000743	8	96058
1000743	9	106815
1000743	10	39070
1000743	11	49814
1000743	12	5717
1000743	13 14	67244
1000743	14	58030
1000743	15	70027
1000743	16	55555
1000743		48513
1000743	18	27895

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
THE GONNEGITONS	K	PH1(K)
1021237	2	32161
1021237	2 3 4 5 6 7 8 9	64322
1021237	ц	106583
1021237	5	128544
1021237	6	21691
1021237	7	48977
1021237	8	107756
1021237		4855
1021237		25929
1021237		43382
1021237		95597
1021237		97954
1021237		79342
1021237		46631
1021237		114995
1021237	17	9710
1021237	18	90728

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1000621	2	70490
1000621	3	121163
1000621	4	88761
1000621 1000621 1000621	2 3 4 5 6 7 8	19817 20329 84621
1000621	8	113728
1000621	9	39634
1000621	10	87745
1000621	11	40658
1000621	12	73074
1000621	13	92901
1000621	14	16357
1000621	15	34587
1000621	16	95029
1000621	17	79268
1000621	18	54287

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT CF SUM SEQUENCE PHI(K)
1530521 1530521 1530521 1530521 1530521 1530521 1530521 1530521 1530521 1530521 1530521 1530521 1530521	14 15	124009 14125 105939 28250 11297 50265 74916 56500 125022 22594 672 100530 23110 112311 103461
1530521 1530521	17 18	113000 19067

Comments of the comments of th

E

•

n

.

TAP	SHIFT HEGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUN SEQUENCE
		K	PHI(K)
	1000517	5	37444
	1000517	3	74888
	1000517	4	42803
	1000517	2 3 4 5 6	112367
	1000517	6	83784
	1000517	7 8	8560 6
	1000517		113742
	10005 17	9	37409
	1000517	10	121793
	1000517	11	94575
	1000517		12538 7
	1000517		90931
	1000517	14	106447
	1000517		34659
	1000517		106396
	1000517		74818
	1000517	18	51470

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1021273 1021273 1021273 1021273 1021273 1021273 1021273 1021273 1021273 1021273 1021273	2 3 4 5 6 7 8 9 10 11 12	110124 41895 60706 83790 6183 121412 37551 94563 69616 12366 100630 19319
1021273 1021273 1021273 1021273 1021273	14 15	57707 75102 2393 73017 46888

•

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1000407 1000407 1000407 1000407 1000407 1000407 1000407 1000407 1000407 1000407 1000407 1000407 1000407 1000407	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18	49350 98700 19403 64743 116090 38806 56729 129486 61200 29963 75745 77612 55780 113458 25159 3171 124381

	SHIFT	POSITION OF	PHASE SHIFT OF SUM SEQUENCE
	REGISTER		50 513.QC2VC
TAP	CONNECTIONS	TAP	
		K	PHI(K)
	1324243	3	98331
	1324243	2 3 4 5 6 7 8 9	65481
	1324243	4	15974
	1324243	5	130962
	1324243	6	119625
	1324243	7	31948
	1324243	8	66716
	1324243		219
	1324243		80039
	1324243		22893
	1324243		7845
	1324243		63896
	1324243		20033
	1324243		128711
	1324243		72882
	1324243		438
	1324243	18	85765

C

8

•

ية يقر

.

	POSITION	PHASE SHIFT OF
SHIFT	OF	SUM SEQUENCE
REGISTER		
TAP CONNECTIONS	TAP	
	K	PHI(K)
	_	
1000355	2	3923
1000355	3	7846
1000355	4	110343
1000355	5	15692
1000355	2 3 4 5 6 7	30094
1000355	7	41457
1000355	8	124439
1000355	9	31384
1000355	10	86513
1000355	11	60188
1000355	12	15525
1000355	13	82914
1000355	14	10309
1000355	15	13265
1000355	16	79337
1000355		62768
1000355		95230

TAP	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
	1020753	2	18925
	1020753	3	37850
	1020753	4	114296
	1020753	5	75700
	1020753	2 3 4 5 6 7 8	129427
	1020753	7	33551
	1020753	8	42170
	1020753	9	110743
	1020753	10	60361
	1020753	11	3289
	1020753	12	50317
	1020753		67102
	1020753	14	10065
	1020753	15	84340
	1020753	16	73295
	1020753	17	40657
	1020753	18	65856

: []

R

	POSITION	PHASE SHIFT OF
SHIFT	OF	SUM SEQUENCE
REGISTER	SECOND	
TAP CONNECTIONS	TAP	
	K	PHI(K)
10002117	2	hahaO
1000347	2 3 4	41418
1000347	3	82836
1000347	4	11047
1000347	5 6	96471
1000347	6	30382
1000347	7	22094
1000347	7 8	73939
1000347	9	69201
1000347	10	56667
1000347	11	60764
1000347	12	105487
1000347	13	44188
1000347	14	8729
1000347	15	114265
1000347	16	378
1000347		123741
1000347	18	80962
1000347	; O	00702

(

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
TRI CONTROLLONS	K	PHI(K)
1020771	2	121382
1020771 1020771	2 3 4 5 6 7 8	19379 56262
1020771	5	38758
1020771	6	116539
1020771	7	112524
1020771 1020771	9	124481 77516
1020771	10	105837
1020771	11	29065
1020771	12	15770
1020771	13	37095
1020771 1020771	14 15	55190 13181
1020771	16	92539
1020771	17	107111
1020771	18	85278

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1000333 1000333 1000333 1000333 1000333 1000333 1000333 1000333 1000333 1000333 1000333 1000333 1000333	12 13 14 15 16	19273 38546 27896 77092 43690 55792 81602 107959 47180 87380 67198 111584 66887 98939 57643 46225
,,,,,,	, 0	48009

TAP	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
	1032067 1032067 1032067 1032067 1032067 1032067 1032067 1032067 1032067 1032067 1032067 1032067 1032067 1032067	2345678901123 11123 11567	109793 42557 6240 85114 16939 12480 90341 91915 25351 33878 10443 24960 122556 81461 14015 78313
	1032067	18	118872

 $\mathfrak{c}()$

C

2

۲,

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1000201 1000201 1000201 1000201 1000201 1000201 1000201 1000201 1000201 1000201 1000201 1000201 1000201 1000201 1000201	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18	52379 104758 126258 52627 114090 9627 11 105254 131066 33963 18 19254 28738 22 103274 51635 50628

	POSITION	PHASE SHIFT OF
SHIFT	OF	SUM SEQUENCE
REGISTER		
TAP CONNECTIONS	TAP	
TAP CONNECTIONS		DUT (V)
	K	PHI(K)
1017243	2	47380
1017243	2 3 4 5 6 7 8 9	94760
1017243	ĬĮ	17348
1017243	5	72623
1017243	,	34675
	7	
1017243	(34696
1017243	8	71413
1017243		116897
1017243	10	55015
1017243	11	69350
1017243		6342
1017243		69392
1017243		115368
1017243		119317
1017243		13875
1017243	17	28349
1017243	18	84744

C

8

n

r r d

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1000173	2 3 4 5 6 7 8 9	111420
1000173	3	39303
1000173	4	23904
1000173	5	78606
1000173	6	23819
1000173	7	47808
1000173	8	59151
1000173	9	104931
1000173		44889
1000173	11	47638
1000173		8630
1000173		95616
1000173		128885
1000173		118302
1000173		89105
1000173		52281
1000173		21461

TAP	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
	1017261	2	57114
	1017261	3	114228
	1017261	4	33002
	1017261	2 3 4 5 6 7 8	3368 7
	1017261	6	7 552 7
	1017261	7	66004
	1017261		101252
	1017261	3	67374
	1017261	10	27451
	1017261	11	111089
	1017261	12	68666
	1017261	13	130135
	1017261	14	124968
	1017261	15	59639
	1017261	16	127054
	1017261	17	127395
	1017261	18	33291

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1011055	2	1956
1011055	3	3912
1011055	2 3 4 5 6	122800
1011055	5	7824
1011055	6	69199
1011055	7	16543
1011055	8	45547
1011055	9	15648
1011055		122484
1011055		123745
1011055	12	38728
1011055	•	33086
1011055		9889
1011055 1011055	-	91094 14283
1011055		31296
1011055	18	27351
1011075	10	21371

1016435 2 53810 1016435 3 107620 1016435 4 69218 1016435 5 46903 1016435 6 114963 1016435 7 123707 1016435 8 10645 1016435 9 93806 1016435 10 111283 1016435 11 32217 1016435 12 66098 1016435 13 14729 1016435 14 24942 1016435 15 21290 1016435 16 35636 1016435 17 74531 1016435 18 61443	SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
the state of the s	1016435 1016435 1016435 1016435 1016435 1016435 1016435 1016435 1016435 1016435	10 11 12 13 14 15	107620 69218 46903 114963 123707 10645 93806 111283 32217 66098 14729 24942 21290 35636

SECOND TAP K	SUM SEQUENCE PHI(K)
234567890112345678	66335 129473 33161 3197 94555 66322 63176 6394 50633 73033 127109 129499 101267 126352 899 12788 104092
	TAP K 23456789011231456

	SHIFT REGISTER	POSITION OF SECOND	PHASE SHIFT OF SUM SEQUENCE
TAP	CONNECTIONS	T A P K	PHI(K)
	1016561	2	99988
	1016561 1016561	2 3 4 5 6	62167 85923
	1016561	5	124334
	1016561	6	21358
	1016561 1016561	7 8	90297 116509
	1016561	9	13475
	1016561	10	74848
	1016561 1016561	11 12	42716 41023
	1016561	13	81549
	1016561	14	61074
	1016561 1016561	15 16	29125 21750
	1016561	17	26950
	1016561	18	59156

C

	POSITION	PHASE SHIFT OF
SHIFT		SUM SEQUENCE
00/// 30/110// 3		PHI(K)
	N.	THECKY
1013227	2	106962
1013227	3	48219
	4	17509
	5	96438
	6	116241
	7	35018
	Ŕ	94698
_	q	69267
-		112817
-		29661
_		38299
		70036
		119902
-		
		72747
_		113296
		123609
1012277	1 12	64876
	1013227 1013227 1013227 1013227 1013227 1013227 1013227 1013227 1013227 1013227 1013227 1013227 1013227 1013227 1013227 1013227	SHIFT OF SECOND CONNECTIONS TAP K 1013227 2 1013227 3 1013227 4 1013227 5 1013227 6 1013227 7 1013227 7 1013227 8

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
THE CONNECTIONS	K	PHI(K)
1013263	2	9315
1013263 1013263	2 3 4 5 6 7 8	18630 56725
1013263	5	37260
1013263	6	120691
1013263	7	113450
1013263	8	89070
1013263	9	74520
1013263 1013263	10 11	114937 20761
1013263	12	92104
1013263	13	35243
1013263	14	76365
1013263	15	84003
1013263		109756
1013263	17	113103
1013263	18	126373

•

T.

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1013323 1013323	2 3 4	122983 16177
1013323	ŭ	80100
1013323		32354
1013323	6	78104
1013323	5 6 7 8	101943
1013323	d 0	62546
1013323	9	64708
1013323 1013323	10	48320
1013323	11 12	105935
1013323	13	72654 58257
1013323	14	99335
1013323		125092
1013323		75458
1013323	17	129416
1013323	18	115767

TAP	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
	1013331 1013331 1013331 1013331 1013331 1013331 1013331 1013331 1013331 1013331 1013331 1013331 1013331 1013331		81802 98539 89998 65065 56632 82147 21153 130130 96803 113264 38646 97849 105292 42306 78633 1883 39511

(0 0

SHIFT REGISTER TO CONNECTIONS	POSTTION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
141 COMMECTIONS	≪	PH1(K)
1013561	2	29481
1013561	2 3 4 5	58962
101356† 1 0 1356†	4 5	170 117924
101356	6	51441
1013561	7	340
10 73561	7 8 9	94438
f013561	9	26295
1013561	10	42598
1013561	11	102882
1013561	12	9562 0
1013561	13	680
1013561	14	65979
1013561	15	73267
1013561 1013561	16	71510
1013561	17 18	52590 118526

Ó

T 4 D	SHIFT REGISTER		PHASE SHIFT OF SUM SEQUENCE
IAP	CONNECTIONS	T A P K	P⊯I(K)
	1013507	2	61117
	1013607 1013607	3 4	122234 87434
	10 1 3607 1013607	2 3 4 5 6	17675 24786
	1013607 1013607	7 8	87275 119135
	1013607	9	35350
	1013607 1013 6 07	4 %	97900 495 7 2
	₩013607 1013607		106740 87593
	10 1 3607 1013607		475 14 23873
	1013607 1013607	,	15003 70700
	1013607	18	40072

O

•

E

•

O

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1015155 1015155 1015155 1015155 1015155 1015155 1015155 1015155 1015155 1015155 1015155	11 12 13 14 15	84157 93829 80057 74485 121733 102029 41730 113173 130006 18677 27877 58085 100083 83460
1015155 1015155 1015155		21301 35797 122794

тар	SHIFT REGISTER CONNECTIONS	POSITION OF SECOND TAP	PHASE SHIFT OF SUM SEQUENCE
INI	COMMECTIONS	K	PHI(K)
	1015253 1015253	2 3 4	130336 1471
	1015253	<u>э</u>	130629
	1015253	5	2942
	1015253	6	5690
	1015253	7 8	885
	1015253	8	1557
	1015253 1015253		5884 93131
	1015253		11380
	1015253		122935
	1015253		1770
	1015253		65 102
	1015253		3114
	1015253		21200 11768
	1015253 1015253		114622
	1017273	, ,	11.022

SHIFT REGISTER TAP CONNECTIONS	POSITION OF SECOND TAP K	PHASE SHIFT OF SUM SEQUENCE PHI(K)
1015271	2	71803
1015271	3	118537
1015271	4	3209
1015271	3 4 5 6	25069
1015271	6	71722
1015271	7 8	6418
1015271		104437
1015271	9	50138
1015271	10	115895
1015271	11	118699
1015271	12	56755
1015271	13	12836
1015271	14	34295
1015271		53269
1015271		35374
1015271		100276
1015271	18	78517

ТАР	SHIFT REGISTER CONNECTIONS		PHASE SHIFT OF SUM SEQUENCE
••••		K	PHI(K)
	1015325	2	60672
	1015325 1015325	2 3 4 5 6 7 8 9	121344 17874
	1015325	5	19455
	1015325	6	5186
	1015325	7	35748
	1015325	8	66361
	1015325		38910
	1015325		63236
	1015325 1015325		10372 68148
	1015325		71496
	1015325		121562
	1015325		129421
	1015325		116454
	1015325	17	77820
	1015325	18	55416

C

APPENDIX C. 5

COMPUTER PROGRAM LISTING FOR GENERATION OF PHASE SHIFTS OF 18-STAGE MAXIMAL CODES

The following is the computer program listing used for the generation of phase shifts of maximal PN sequences of period 2¹⁸-1 as described in Appendix B. 5.

The program sets up an 18-stage register with a specified initial condition vector $\mathbf{a} = [\mathbf{a}_0, \mathbf{a}_1, \dots \mathbf{a}_{17}]$. The shift register is then clocked -k times to obtain the initial condition vector $\mathbf{b} = [\mathbf{b}_0, \mathbf{b}_1, \dots \mathbf{b}_{17}]$ of the sequence obtained at the kth tap of the shift register. The sequence which is generated by the shift register with initial conditions \mathbf{a} is then searched for the state vector A+b. The position of this state vector gives the phase shift obtained when the output sequence of the shift register is added modulo 2 to the sequence obtained at the kth stage of the shift register.

_শ ্বত হল্পুন		٠			,	,	1				* z	70 VA.L.Q			System of a contract of
•			, ,		•										5-121
						And the second s				•		·	, ,		
\$									5 DF *			* NU		CONDITIONS	
\$	·			PRINTING					CGNDITIONS			IST OF	,	INITIAL	
	21.04.05			TS/PAGE		SO STAGES.		.D CGNTAIN*/	OF INITIAL CON	E.20) GD TD 115	IER DATA+1)	D CONTAIN A L		REGISTER FOR I	
**************************************	92/10/20			1 IBRARY7505 TO 2 18 STAGE RESUL	ROBERT GOLD	FEGISTER IS		*7H*IAPE5** SHOULD	ESENTATION ER*/ AY A B*/1	. IORDER.L	STAGES, RE-ENTE	*7H*TAFE5** SHOULD			INTIPLIANHOLSKOLUKUEKOLEON
G	The state of the s	RGA12(IAPE5, TAPE6)		STAGE CODE LIBI TAILGRED TO 2 PAPER 3 SPACES	GREEN AND	OF SHIFT	IFA(21)	*7H*	AL REP REGIS	IURDER, INH . GE.1 . AND.	TO 20 S	()	LLOWED BY TERMINATEL	CONFIGURATION	NH THAT
\$	(VEP. 2.3A)	JCRAM	the state of the s	18 PMAT IGN	AUTHORSIRA GRI	MAXIPUM SIZE	DIMENSION IF	6,10 (/* *	* 0CT/ *SHIFT * FE	ACCEPT(5) IURDE IF (IORDER.GE.1 WPITE(6.112)		11	*FOLLOWED * TERMIN	co	ALL INTIFIE
•	V) BELLEVIO	· . [A A	* * EUL! * * FC	* * AUT.	* * *		105 F	t 315	111 0	112 F	-	2 8	* SET	
•	RUNX CCM		, , , , , , , , , , , , , , , , , , ,				000004	010000	000010	000010	000033	C00034	000034		**************************************

{ **C**

*

C

u - raggeres.	ATT CONTRACTOR OF THE PARTY OF			ļ	1 1		1964) 436 1008000 ATT 101 TO THE
0							5-122
	P6A12		REVERSE		SEQUENCE		
the second per visit of second of second on the second on the second on the second of second on the second on	21.04.05. J CONNECTIONS	SHIFT DF*/ SEQUENCE*/	*/ REGISTER AND ITS	IFA) CUNNECTIONS	LUE TO OBTAIN THE REVERSE		280
	• • •	PHASE SUM SUM	C)*//) OF SHIFT	RDER,	IRST AGE F		II.EQ.IIL) GO TO
	VER.2.3M) IFIRST = ISR CLIL MIRRCRISSP.IEIRSIM.IDRDEP.IE P TO GENERATE LIBRARY OF ACCEPTED	NF 1 25x *PGS1T *SHIFT *REGISTER	* TAP CON * *K* 10X C-01 SICP FOR PIN H	CCNNECT(INF, IPINL, IPINK, ID IS THE NUMBER OF POSSIBLE O I=2, IORDER	REGISTER AND NCE AND ITS REGISTAND ITS REGISTALINES REGIS	ECTION IFIRST IFIRSTM	. ה ה
	9	12: ISR = IFIRST ACCEPT(5) INF WEITE(6,156,1 150 FURMAT(9(7) 2 1 18X *S	TE CINE	CALL CENN 10REER-1 IS DG 300 I=	CLOCK SHIFT TEST SEQUE CALL PULS CALL ADDS		200 CCNTINUE IF (ITT.EQ.ITR II = II + 1
C	CCMP1	000044 1 000053 000057 1 000057	000057	000062	C00070 **	* *	000104 000104 000104 000114

.1.

in the state of th	And the Markey of the			Cathia	The second secon	व्यं कृष्टिक्रा स्थापक्षक पुरस्का अस्तर ।
						5-123
•						
and the second of the second o						
	BGA12	15.8	IONS		v	
; 6		FT REGISTER	CONNECTIONS			
	21.04.05	IGINAL SHIFT	FOR TAP			
	02/10/126	HE OF	ER) DETERMINED			
March of the state			10RD NCE			
ter all marganisms		SHIFTED= TO AN EAR S A MIRROR IMAGE OF SRIITRAIPINRAIDRDES SHIFTED= TO A LATER	CALL PLLSR(ITL, IFINL, GD 1D 200 SE SHIFT OF SUM SECUE CENTINUE WRITE(6,290) INF, I, III FORMAT(16x G7, 16, II			
C	(VER. 2.3M)	R = PIGHT SH BUT IT IS A CALL PULSE L ≡ LEFT SHI	CALL PLLSR(17L, GD 1D 260 SE SHIFT OF SUM WRITE(6,290) IN FORMAT(16x G7, CONTINUE	TG 125		
**************************************	1'. 7	111	CAI 60 60 * PHASE * 260 CEP 250 FOR 300 CEP			
•	RUNX COMPILER	000115	CCC123 ************************************	060141 Culi41	-	

RUNX COMPILER (VER. 2	PILER LVER.2	2.381		07/01/76	21.04.05	5	P6A12			
PROGRAM L	LENGTH	•								
STATEMENT	FUNCT ION	REFERENCES	S		, e	·				,
	LECATION	GEN TAG	SYM TAG	REFERENCES	S					
STATEMENT	STATEMENT NUMBER REFERENCES	EFFRENCES								
	LCCATION	GEN TAG	SYM TAG	REFERENCES NONE	S					
	000216	000053	110	NONE						
	000010	100007	111	0000033						
	000034	100022	115	000027						
	000044	LC0027	125	000140	:				`	
	000104	100057	200	000123						
	000124	120007	280	660113						
	060305	251003	290	000124						
ELDCK NAM	NAMES AND LE	LENGTHS								
VARIABLE	REFERENCES	И								
	LOCATION	GEN TAG	SYM TAG	REFERENCES	5					
	000334	ACCC01	I E A	000035	000042	000130	000076			
	000344	V00005	IFIRST	000000	600000	220000	000100			
	000345	VC0006	1FIRSTM 11	000041	000101	600133				
	000346	VC0007	INI	000000	C00057	000062	000127	۶		
	000342	V00003	INH	000014	000034	000035		00000	02000	,
	000347	VG0010	IPINE	000076	0000116	000121 000120	000136			
	ucu 430	TIMONA	NA TA	Egnnna	E Thirth				, , , , ,	-124
		, ,					7	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		

. . .

The second section of the second

C

and the first productive to the	A Marie and Co							· · · · · · · · · · · · · · · · · · ·	· managenerum e » · o	r 2 May 114 Helde Thatfall	· 有效性 4000年间	4 .		
												ı	5	125
Ð														
	1													
	W.	000072												
		00	,											
		2					3							
C	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	29000					CDNNECT					ŧ		kgr
*	4	0					3					. /		
Dollard State Control	· · · · · ·	045					م					,		The state of the s
) to	LA 29	000045					STOP							
· ·	, , , , ¹	000040	000120				MIRROR							
	1	33	88				W]							
C	7 0	37	240				11							
; ;	7 7	000037	000110				IAIIAI					,		
•	92											,		·
. -	2710720	000034	000101 000102 0000075				CUTPIC							, ,
; ·	600	000	888				נחם							5-
	in the same						u	00						
	10 Acc	15R 11	17L				INPUTE	040100						
Same Same	194 h	151	нын				H					•		
* *	hin .	400	15				N W	<u>.</u>				, ,		
		VCC004 VCC013	V00015 V00016 V00014	,	8		REWINM ACOSR	USED						7, 47
4	A S N		E.M.	NTS	AR IE	c T S	NC ES	o						1 4 h
C		000343	000354 000355 000353	CONSTANTS	TEMPORAR IES	INDIRECTS	REFERENCES QANIRY PULSR	SPACE OC7700						
0		000	0000					4						
				1 0F	START OF	17 CF	EXTERNAL							,7
6	CHANY COMPTLED (VEP. 2.3M)			START COC143	START	START	EXTE	COMPIL						·
ļ	177		1 · · · · · 1	ı	1		1	'	1	•	7	•	•	, ,

The state of the s	the state of the same	~ n zn		اند و ساچدود	٠, .	· -		ė.	art Ant	era e	S.	A S	To all the last the l		
													5	-126	
			,									,			
	, , ,														
•			REVERSE		RIGHT									ar A	
A contract of circumstance of	.	1E A)	115	THE LEFT	TO THE							,		-	
The state of the s	6 21 64 0	INP.IGRDER. 1EA)	FT REGISTER AND	LOCKED TO	H IS CLOCKED		-1))								
C	7/10/70			WHICH IS C	REGISTER WHICH	JRDER+1)	ACIORDER+2-							,	
C		SUBROULINE CONNECTITME. IPINI. TP	PIN HOOKUP OF		REVERSED REGI	SION IFA(1) BINCCEF(INF, IFA, IORDER+1) = IPIN = G	1, 10RDER (1,1,1,1PINL,1FA(10RDER+2								
c ,	2.3M	ROUTINE CO	UP MASKS FOR	IS NORMAL REGISTER A LATER TIME	IS THE REV	DIMENSION IFA CALL BINCCEF IPINR = IPIN	50 Im SBYT	INUE							
e ()	ORPITER (VER	BILLS	* SET UP	* IPINL * OR A	* IPINR * OR A	DIMEN CALL IPINR	DG 1 CALL CALL	150 CC TIN RETURN ENC							
•	RUNX CCRP					600010 600010 600014	000021 C00022 D0C030	950000 950000 050000							

and the last of the state of th

م بهدر دده	ndic , de president automobile de				.	ng person yan	- verment superior of the second superior of	5-127
		,*,						
•				g				
G				E+0003				
₹,	CONNEC			560003				
*				660003				
median and an area of the second	21.04.0			5200054				
	02101126		REFERENCES REFERENCES	REFERENCES GGGG21				
hande out outer state			TAG TAG	SYM TAG F		g	037400	
		ERENCES		7 A G		G N H	- a	
wine is therefore described with the second	EP (VEP.2.3M)	LENGTH FUNCTION REFERENCES	TON GENTEER	ID LENGTH	CONSTANTS TEMPORARIES	INDIRECTS REFERENCES BINCOEF SBYT	i I I I	
r. ()	T CND	GRAM	STATEMENT NUMBER REFERENCES LGCATION GEN TAG	ELFCK NAMES AND LENGTHS VAFIABLE REFERENCES LOCATION GEN OCOOSS VOCO	±	i	1 1	5
	O XMNA	SUBPROGRAF GOCOSZ STATEFENT	SIAIER	BLF.CK VAE LAF	514KT 000050 START COGO52	START OF ODCOSS EXTERNAL	COMPILER UNUSED -	

.5

TWIN CONDICE (WER 2 SM) SUBSCUTINE INITIALISMA, SEA TOWN TOWN TOWN TOWN TOWN TOWN TOWN TOWN		1 1				1 1	,	r u Britania parci -	Marinda Alleria dell'Alleria L	egent≪s A.t	anders and spread the Control of the control
E-INJIPI(INM-ISE-IDEDER-JEA) ONFIGURATION IN SHIFT REGISTER FOR INITIAL CONDITIONS ONFIGURATION IN SHIFT REGISTER FOR INITIAL CONDITIONS ER IS REPRESENTED WITH THE COEFFICIENT OF THE LEAD, THE FIGHT ON IN SHIP OF THE FIGHT ON SHIP OF THE FIGHT ON IN SHIP OF THE FI											5-128
E-INJIPI(INM-ISE-IDEDER-JEA) ONFIGURATION IN SHIFT REGISTER FOR INITIAL CONDITIONS ONFIGURATION IN SHIFT REGISTER FOR INITIAL CONDITIONS ER IS REPRESENTED WITH THE COEFFICIENT OF THE LEAD, THE FIGHT ON IN SHIP OF THE FIGHT ON SHIP OF THE FIGHT ON IN SHIP OF THE FI											
EN IS REPRESENTED WITH THE COEFFICIENT OF THE GRA. ON THE FIGHT OR IN BIT O 15 ACT) OFFICIAL SEPRESENTED WITH THE COEFFICIENT OF THE 15 ACT) OFFICIAL SEAL STANDER 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	*	-									
E INITRIGINALISE, IDROCE, IEAL ONFIGURATION IN SHIFT REGISTER FOR INITIAL ER IS REPRESENTED WITH THE CUEFFICIENT OF THE RECHT OR IN BIT O IFA(1) DEFLINALIEALIORDER) = 1010ROFR (1,1)1SR_IFA(1))	U										, n
E INITRIGINALISE, IDROCE, IEAL ONFIGURATION IN SHIFT REGISTER FOR INITIAL ER IS REPRESENTED WITH THE CUEFFICIENT OF THE RECHT OR IN BIT O IFA(1) DEFLINALIEALIORDER) = 1010ROFR (1,1)1SR_IFA(1))											
E INITRIGINALISE, IDROCE, IEAL ONFIGURATION IN SHIFT REGISTER FOR INITIAL ER IS REPRESENTED WITH THE CUEFFICIENT OF THE RECHT OR IN BIT O IFA(1) DEFLINALIEALIORDER) = 1010ROFR (1,1)1SR_IFA(1))											
E INITRIGINALISE, IDROCE, IEAL ONFIGURATION IN SHIFT REGISTER FOR INITIAL ER IS REPRESENTED WITH THE CUEFFICIENT OF THE RECHT OR IN BIT O IFA(1) DEFLINALIEALIORDER) = 1010ROFR (1,1)1SR_IFA(1))											
E INITRIGINALISE, IDROCE, IEAL ONFIGURATION IN SHIFT REGISTER FOR INITIAL ER IS REPRESENTED WITH THE CUEFFICIENT OF THE RECHT OR IN BIT O IFA(1) DEFLINALIEALIORDER) = 1010ROFR (1,1)1SR_IFA(1))	(6		,								
E INITRIGINALISE, IDROCE, IEAL ONFIGURATION IN SHIFT REGISTER FOR INITIAL ER IS REPRESENTED WITH THE CUEFFICIENT OF THE RECHT OR IN BIT O IFA(1) DEFLINALIEALIORDER) = 1010ROFR (1,1)1SR_IFA(1))			S								
E INITRIGINALISE, IDROCE, IEAL ONFIGURATION IN SHIFT REGISTER FOR INITIAL ER IS REPRESENTED WITH THE CUEFFICIENT OF THE RECHT OR IN BIT O IFA(1) DEFLINALIEALIORDER) = 1010ROFR (1,1)1SR_IFA(1))	dic.		ION							, ,	
E INITRIGINALISE, IDROCE, IEAL ONFIGURATION IN SHIFT REGISTER FOR INITIAL ER IS REPRESENTED WITH THE CUEFFICIENT OF THE RECHT OR IN BIT O IFA(1) DEFLINALIEALIORDER) = 1010ROFR (1,1)1SR_IFA(1))	C		LI QA								'
E INITPI(INM,ISP,IOROER,IEA) ONFIGURATION IN SHIFT REGISTER FOR INITIAL ONFIGURATION IN SHIFT REGISTER FOR INITIAL ER IS REPRESENTED WITH THE CUEFFICIENT OF ERROR ON THE EIGHT OR IN BIT O JFA(1) OEELINH,JEA,JORDER) * 1,IORDER (1,1),ISR,JEA(1))	Gertal Christian		co	표							
E INITRICIANA, ISR, IORDER, JEAJ ONFIGURATION IN SHIFT REGISTER FOR ER IS REPRESENTED WITH THE CUEFFICE ERP ON THE FIGHT OR IN BIT ON JEACL) OEELINH, JEA, JORDER) = 1, JGR DER LIJLISR, JEALLI)		rat	IAL	1							
E INITRICIANA, ISR, IORDER, JEAJ ONFIGURATION IN SHIFT REGISTER FOR ER IS REPRESENTED WITH THE CUEFFICE ERP ON THE FIGHT OR IN BIT ON JEACL) OEELINH, JEA, JORDER) = 1, JGR DER LIJLISR, JEALLI)	c		HIN	l 1							,
E INITPI(INH, ISR, IDEDER, IEA ONFIGURATION IN SHIFT REGIS ER IS REPRESENTED WITH THE ER DA THE EIGHT OR IN BIT IFA(1) OEE(IMH, IEA, IORDER) * 1, IGR DER (1,1,1,1) SR, IEA(1))	A same	5	- X	IC IE							
E INITPI(INH, ISR, IDEDER, IEA ONFIGURATION IN SHIFT REGIS ER IS REPRESENTED WITH THE ER DA THE EIGHT OR IN BIT IFA(1) OEE(IMH, IEA, IORDER) * 1, IGR DER (1,1,1,1) SR, IEA(1))	!	3		FF.1						,	,
E INITPICINH, ISR, IORDE ONFIGURATION IN SHIFT ER IS REPRESENTED WITH ER ON THE RIGHT OR IN JFA(1) OFF(INH, IFA, IORDER) - 1, ICRCER (1,1,1)SR, JFA(1))			A A A S T E I	1							
E INITPICINH, ISR, IORDE ONFIGURATION IN SHIFT ER IS REPRESENTED WITH ER ON THE RIGHT OR IN JFA(1) OFF(INH, IFA, IORDER) - 1, ICRCER (1,1,1)SR, JFA(1))	.	9	1 E G I	1 HE B 1.1							
SUBPCJINE INITRICIAND CTAC SUBPCJINE INITRICIAND CTAC * SET UP RIT CONFIGURATION IN SHIF * SHIFT REGISTER IS REPRESENTED WI COCOOT CALL BINCDEFLIND IFALL COCOOT CALL SEXTILLISE IFALL COCOOT CALL SEXTILLISE IFALL COCOOT COCOOT CALL SEXTILLISE IFALL COCOOT C	` •		8 I.	EA							, ,
FUNX COMPILER (WER. 2.2M) FUNX COMPILER (WER. 2.2M) SUBFCUTINE INITPITINH, ISR. * SET UP BIT CONFIGURATION IN * SHIFT RECISTER IS REPRESENTER * CONSTANT TERE ON THE RIGHT * OUTEN IN THE RECHT * OUTEN IN THE RECHT * OUTEN IN THE RECHT * OUT OF THE STATE OF THE RIGHT * OUT OF THE STATE OF THE STAT	ι,	7770	SHIF	7 A B	3						
PUNX COMPILER (WER.23M) SUBRCJINE INIPL(INH. SET UP BUT CONFIGURATION SHIFT REGISTER IS REPRESE CONSIDER SION IFALD COCODS COLL BINCOEFLINH, IFALD COCODS COCODS COLL SAVILLALISE, IFAL COCODS COCODS COCODS RETURN COCOCS COCODS COCODS RETURN COCOCS COCODS COCOCS COCODS COCOCS COCOCOCO			IN IS	NTEI GHT	ORDI						
FUNX COMPILER (VER.2.3M) FUNX COMPILER (VER.2.3M) * SET UP BIT CONFIGURATI * SHIFT REGISTER IS REPR * COMMITTER ON THE COMPILED ON THE COM		, , , , , , , , , , , , , , , , , , ,	¥ 8	ESE	A I						
# SET UP BLT CONFIGUR * SET UP BLT CONFIGUR * SHIFT REGISTER IS R * CONOST * CONSTANT TERE ON * CONSTANT TERE ON * CONOST * SHIFT REGISTER IS R * CONOST * CO	1_1	147	1141	EPR	DER						
# SET UP BIT CONFI * SET UP BIT CONFI * SHIFT REGISTER I * SHIFT REGISTER I * SHIFT REGISTER I * SHIFT REGISTER I * COODD CCOODD CCOOD	٠	of the	11.00 F	2 4	ICE ICE						
# SET UP RIT COCOOT C	4.	A.	A I	는 4 2 (점 13	15. GEE.						
# SET UP BE COODS OF COULTS OF COODS OF			¥ Ö H ⊢	IST	I DNC	m .					,
COCOOD CO	ŧ.	47	72	REG TAN	~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~	H (K					
COOOD CCOOD SEI		// 3	an do	1.FT	CAL	RET END					
000000 0000000 00000000000000000000000	C		SET	SHI		0					
000007 C000007 C000015 C000015 C000030 C000030 C000030 C000030	10	1	* * *	* * *	+	15(
0 00000 000000 000000 000000 000000 000000		3			r n o m a	w 0 0				٠,	
3333333	lo	X			0000	0002 0003 1003					
		1 4	1. 1		2223	328					

1.1:

1

ı

11. TE 15 17 17

?

, •

C	
PUNX COMPILER (VER. 2.3M) 07/01/76, 21.04.05. [MITE]	
SUBPREGRAM LENGTH	
STATEMENT FUNCTION REFERENCES	•
LOCATION GEN TAG SYM TAG REFERENCES STATEMENT NUMBER REFERENCES	
LOCATION GEN TAG SYM TAG REFERENCES	
BLUCK NAMES AND LENGTHS	
VARIABLE REFERENCES	
LGCATION GEN TAG SYM TAG REFERENCES OCCO37 VOGGOS I DOGG14 GGGG15	
Slart of constants codo22	
START OF TEMPORARIES GOGG34	
START CF INDIRECTS GGG036	٠
EXTERNAL REFERENCES BINCOEF SRYT END	
CDRPILER SPACE UNUSED - C105CO USED - C27300	THE PARTY OF
	S. S
	5
	-129

· .

ن ر

			1	ı
F	· .			1.
RUNT COMPLLER EVER. 2.3M) 07/01/76	21.04.85.	HIRRER	•	i
SUBPRUCRAM LENGTH .)	; #
STATEMENT FUNCTION REFERENCES	•			∮ . n
LOCATION GEN TAG SYM TAG REFERENCES	S			
STATEMENT MURBER REFERENCES		3		1
LGCATION GEN TAG SYM TAG PEFERENCES	Ón			
BLCCK NAMES AND LENGTHS				
VARIABLE REFERENCES				ļ
LOCATION GEN TAG SYM TAG REFERENCES GOOD37 VOGOD5 I COCOI4 OCOG46	\$ 000646 CGCG25			
STAR; CF CONSTANTS GOODS	•		•	ļ
START OF TEMPORAPIES				
START OF INDIRECTS		•		
EXTERNAL REFERENCES BINCHEE SRYT END				
COMPILER SOACE Unuser - C10500 USER - v37200				\$50 × 4
				n
				0.
			5-	, r-s
			·131	,
				i.

B

C

C

PINX COMPTICE (VEC.2.3M)	07/01/76. 21.04.05.	BINCHEE	
SUBPREGRAM LENGTH	•		, t
STATEMENT FUNCTION REFERENCES			
LUCATION GEN TAG SYM TIG	REFERENCES		
STATEMENT NUMBER REFERENCES			
LOCATION GEN TAG SYM TAG	PEFERENCES		
BLECK NAMES AND LENGTHS			
VARIABLE REFERENCES			
LOCATION GENTAG SYNTAG	REFERENCES OCCO.5		
100004 V00006		:0 000022	
START DF CONSTANTS COCO30			
START CF TEMPOPAPJES COCO31			
START OF INDIRECTS CCC033			
EXTERNAL REFERENCES END			u sygar ha i ra
COMPILER SPACE UNUSED - 010500 USED - 037300			and the second
			-133
			Mar will be

\$*****

*****;

Marie - Talan	erical and the second second		m,				. 😘	N	· ng ng pigasik-ril , ar y	en egen fræs	is 		
•	BAGE										5	-134	
C	90		,							,			1
•	21.04.06												
	07/01/76											,	
	0770											, ,	
8												7. 77.	
	VER												
ŧ.	COMPASS												
	WO3	ARDS											
: 1-1		٩											1
		COLIB	PULSR									,	
c		BINARY COLIROL	IDENT	3	н								
		a	H	ENIEZ PEINIS.	J								
i:				KBIVE	PULSR								
	,	LENGIH	٥										
ε			,	·									
2	PULSP	ADDRESS	0 9										
		ALLO											
•	PULSE	UKAGE									. .		

PULSE				COMPASS - VER 2. 07/01/75. 21:04:05. PAGE	
		IDENI	asina		İ
		ENTRY	PULSR		
	* * * *				
	* CALL	PULSR (ISR	SR, IPINS, IOPOER)	DPDER)	•
	* ISB	* COND	ITTON OF SH	ISR * CONDITION OF SHIET RECISIER	
	# IFINS	NS = MASK		DF PIN CCNNECTIONS	
	* ICKDER	N	DRDER OF NUI	OF NUMBER OF FITS IN SHIFT REGISTER	
	*				
0 2025142322000000000		VFD	42/CLPULSP, 18/2	SP, 18/2	
1 56110	PULSR	85S 541	1 81	ENTRY/EXIT LINE FFICH CONDITION DE SHIET REGISTER	
1		SAZ	82	FEICH PIN CONNFCTIONS	
56530		SA5	83	FETCH DROER	
3 625577776		\$25	x 2-1	AS IN SHIET IN PICH ONE TO SO	
11312		ო ა ჯე	// * * * * * * * * * * * * * * * * * *	TRANSMIT PIN CONNECTIONS IG X3	
4 43073		EXD FXD	٠, ١	8 X X0D 2	
		ex4	7×+0×-	IN X4	
22454		1×4	85,×4	LEFT SHIFT TO HIGH DRDEP SHIFT DECISIED DIGHT SHIFTED END DEF	
5 12614		9X 8	X1+X4	DE IN NEW HIGH DROWN BIT	
		SA6	81	STORE NEW CONDITION	_
6		END	P ULSR	RETURN	
4276G STORAGE USFD		29 STATEME	MENIS	1 SYMBELS	ļ

The second of th

the second of th

:

z

おおとかいれていたできたからとうとうなど、おといれてきていているというかい、これに対対なるないないないできませんない

	y adjy	41 57 S	οφο. 	1		ر، _{يو} سد	ar .				#0.20ths - **	 	1	tom state or the		prigo-stre (appendicture)	A THE THE SECOND	-
	•		-	PAGE	•											5	5-136	
	1	/ 1 ~	- 	9														_
	•	J		21.04			1		,						,			
				07/01/76														
	8			0720	•													
Handle Committee	C		,	2														
2				a zv -	•													
			<i>i</i> .	COMPASS														
:	;			3	•	28	,											
		-				77						j						-
			ų			2/15 1												
			,							1								
						1709												
		:				* 8												
\$	£,				TABLE.	PROGRAM	,										. 1	
		,	y '		ENCE	7												
ir e sai automi (diase a	•) #		SYMBOLIC REFERENCE TABLE.													
a idai, describinada			; ;	SP	ABOL IC	asina										1		
	•			Tin d	SYI	14	•											

v 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Marin Land							ghega:		· ·	ender - Tunzana	, ny m- n, n p-1
	21.04.C6. PAGE			GR					•		5	-138
3 3 3	CCMPASS - VER 2, C7/01/76		3RS)	BIT ADDITION OR EXCLUSIVE	/CLADESP,18/3	CH SHIFT R CH SHIFT R 2 SR ADDI	PE SUM	1 SYMPOLS				
*		IDENT ADDSR ENTRY ADDSR	1 10	WHERE ISES = ISEA (+) ISRB AND (+) MEANS MOD 2 BIT BY	VFD 42	SA1 SA2 Bx6		19 STATEMENTS				
*		**	* * *	* * * *	C10404232200000003 ***	56110 56220 13612	5663C C40CU00UC1+	41161 STORAGE USED				

こうこう こうしょう 一日の こうない かんしょうかいろうしし はなないない

		200	*** _ •								f	1				i a lig	,		
5		ð	,	PAGE													5	-139	
÷	を表現している	AT.		1									•						
· ·		1		21,54,06												,			
· · · · · · · · · · · · · · · · · · ·				1														,	
))	000	\$		07/03/76												ŧ		,	
.	fe dera ffschestliche bestehen	*		2															
	Company of the second	8		VER															
:	ŗ			COMPASS -															
	•		-	¥00															
		: -	1 1			2/18													1
	, <u>s</u>					13													
	* 41. 34. Jan 11	t,				2/13													
· .	gjeringsk-varderskar av		<i>;</i>			53/1													
Saleton K.	A Servetaria Vilaneta - 6		,																
* * * * * * * * * * * * * * * * * * *	is the second of the second of the second	*			E	GRAME													
-	ž		d .		CE TAB	TO BEIGRAM											:		
· ;	900 × 1 31 Chan 3	· (1-	-		FEREN														
*	を持たます。それになって、イイン・ハスのまでは、気を変しませる。	\ \$~	∱. 		SYMBULIC REFERENCE TABLE.	a													
3		•		ADDSR	SYMBG	ASOGA													
	ļ	i	ļ	1			1	1	1	1	1	l	1	i	i	1	I	ţ	1

APPENDIX D. 5

COMPUTER PROGRAM LISTING FOR DETERMINATION OF SIDELOBE DISTRIBUTION OF GOLD CODES

The following listing is the computer program used for the generation of the sidelobe distribution of Gold codes of period 2^{11} -1. The program computes the number of sidelobes in the cross-correlation function θ of any Gold codes of period 2^{n} -1 by making use of the formula for the number S of cross-correlation sidelobes given in A.5.4, i.e.,

$$S = \frac{\sum_{\theta}^{2} + 2\sum_{\theta} + 2^{n} - 1}{2^{n+1}}.$$

For each code, the program first computes its unbalance and its autocorrelation function. For each pair of codes to be correlated, the program then computes the product of the unbalances which yields the quantity Σ_{θ} and the dot product of the autocorrelation function, which yields the quantity Σ_{θ}^2 . The above formula then is used to compute the number of sidelobes for given cross-correlation and the distribution of code pairs with a given number of sidelobes.

												The Money	ale and well and a service	44.	Kagana ya w		5-141	91.
Nagar Se																		
			cabes7565		S H			2047),				10.55	CF#		į			
}	. 20.59.06.		STRIBLTION OF GOLD CO		FCP SHIFT RECISTERS CHESS CORRECATION		ic E					NB, IPE PICO, JTHE TAI, NCCOES	R EXCEEDS PAXIFUR			11		
	07/06/76.	6, TAFE7)	E DI	D REBERT GELD	RGAIC CN *IAPE7* 10 CENERATES SCHE	USEC.	E ITH CORPELATION SECUENCE OTH CORRELATION SEQUENCE CORRELATION CONT	7),ITHETAJ(2047) E(4)	N CECKI MATRIX			7 THADIF LONADICCOELDIF BONBOI	IC SHIFT REG			1)		
	ER (VER.2.3M)	PRJFPAM PGAIS(TAFEC, TAFET)	CROSSCOPRELATION FOR	FUTHURY IFA GREEN AND RUBERT	ACCEPTS JUTPUT FREM REALC EN #1 UP TO 11 STAGES AND CENERATES DISTRIBUTIONS.	Cica = CZICO IS NET USEE.	THETAL IS THE ITH CORRELATION THETAL IS THE CORRELATION NIMETA IS THE CORRELATION COUN	COMMON TRETA!(2047)	JUTTIALIZE CORRECATION	HFTAZ = 0	DT 101 T = 1,2647 NTHFTA(1) = 0 101 CONTINUF	WIND A	TF (PA:[=.11] GC TC WPITE(6.165) NA 105 FPPAT(7/ 15 * STAGE	1 + 11 STAGES#71	UE	ISTACT = 24+(NA+1) FOUF = MCEDES + (V		
	RLNX COPPILER		* * *	* *	* * * 1	F W 4		* 500000 500000	# 4	500000		666012 666614 660616		CCCC53	2 0	6,5000 6,50000 6,60000		

07/06/76, 2C.59.06. RGA13		DE UCCURANCES FUR CURRELATION -1 FGR THE AN EXPRESSION	CT - ISCRIZ - Z*JTHETAI*JTHETAJ) / IZFACI ATIJN GP CFF GIAGGNAL TEPM	= NTHETA(Nr15GK) + 1	CCCPRELATION OF LAST DIAGONAL TEFM	1) = VTHETA(NPICER) + 1	TATISTICS FOR ALL I AND J ON ANT AROVE THE* NAL*// R OF TIMES CORRELATION (THETA) OF -1 OCCURS*	ACH ELLFRENIAL R GF ELEPENIS IN WHICH THE FRECUINCY CCCUFS*//)	.01 WFITE (6,620) ISNIHETAL RICO RE-31 AFITE (6,620) ISNIHETA(I)	UF CLM. PRCBABILITY*/ . LCBES FREG. DISTRIBUTION*//)	SECUENCY DISTRIBUTION
RLNX CCMFILER (VER.2.3M) 07/06/76	CC0247 200 CONTINUE	FCR	1 0	NTHETA(NYICER) = 30C CONTINUE	SCA CPRITATIVE And Pryzining Aliccprelatich CR	F(1) R) = VTHETA(NPICCR)	MRITETANCO 6CC FFOMET(///* STATISTICS FEF ALI 1 * DIAGONAL*// 2 * NUMBER OF TIMES CORRECT	ELEPENIAL ELEPENIS IN	1F (**THFTAZ*NE.3) WFITE(6,023) 620 FOR*AT(115,17) 00 630 I=1,1PERICO 1F (**THFTA(1)*RE.3) AFITE(6,620	0 ::	* CALCULATE CUMPLIA": FECTENCY D

)		!	}		1	J	mar and the contract of the	A LAND OF STREET	ť
radion in the sales								5-144	İ
		:							
	,								
	RGA13								
	. 2		1,355			1			
			1 1						
			F \$10:						
	20.59.06.		וא בי		פר וו				1
1	- 1		FUR NUMBER		-				
	/76.	7	+ C K		ILFRET ST				
	730/23	+ 1 THETAZ + KIRETAT	165			u)			
		Z Z + +	CF S CF S		A(1) U .CK. IFPEC.EU.1 /F'UM NLEBES+1FREG+FOIS	TC 645			
		(1)	FP 5.	NLESES 10 653	Ж. Ж. П. S. й.				
,		NTHETA(1) [PERICO NTHETA(1)	LIIP	EQ	A(1)	11. 15. 10.			
		2 1 1	MUCATIVE FF A FULTIPLE (TPEKICO/5)	IFREG 100 - R 100 - C 100 - C	TF 660 EC = WIHETA(1) TIMUF TIPPET-EC-0 -CK- CT = 1FREC/FCM TF(6.710) NLEBES	#41(116)15; 1 4rs = NLGBES (rlgbes.66.C)			
;	34)	1(1) ((1) (((1) ((()	A O F	0 F . 2	7667 NUF PULF H I	. S = 10.0			
	(VE 6.2.3M)	NTHETA(1) = NTHETA(1) NO 640, I=2, IPEPICO NTHETA(1) = NTHETA(1) CONTINUE	PTCK THI CUMMULATIVE FF WHICH ARE A MULTIPLE WHIREK & (IPEKIOUTS)		GN TP 66 FOSC = CONTINUE CONTINUE TO TECT = LO TECT =	ENDERT([]CJIS, [1.3] **LORES = NLGBES = 5 IF (**LOBES.66.6.) 56 **TPE TNO			
	1	1	HM						
3 ()-	COMPILER	940		645	950	750			
• •	0.0	CC0277 CC0301 C00302 C00304		000300 000311 000313 000314 000316	CCC321 CC0321 CCC323 CCC323 CCC332	200347 000347 000347 000347			
	0	1 ~ ~ ~ ~	i r	944FC	10 10 10 10 10 11	5 0 0 0 0	1 1	. 1 1	

l

•	6	t.	¥		.	#	•	C	,	A LEGISTER
<i>,</i>			,		•		,	;		
RLNX COMFILER IVER	R.2.3M)		07/01/76.	5. 20.59.06.	• (RGA13				٠, ۲
PRUGRAM LENGTH CC0501	•									
STATEMENT FLUCTION	N PEFFFENCES	S								
COCATION	CEN TAG	SYM TAG	PEFERENCES	5.3						•
STATEMENT NIMPED O	DEFFORMCES									
LOCATION	GEN TAG	SYK TAG	PEFEPENCE CCJC45	S						•
2000	1 45076	110	50000	300343						•
690163	190001	120	Cu:107							
[0/40]	620000	(35	C00273							
C2C313	CCOISO	242	256363							
000331	100126	ງ ເ ນ 4 ລ ດ								1
5 350		22.	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2							1
8 4 6 00 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	100347	250	000331							•
_	EWETHS									
FICBUFS- GC2057	i	- 014660								•
VARIABLE REFESENT										
LOCATION		SYN TAG	C	ËS					•	
295727	VCOUZS	F SUM	500000	JCC332 JCC127	66(133)	843000	0.0301	000316		-
			606321							
C.C.4 + 2	Exillent	ICCOLI	025350	266143						•
000472	VOORS	ICEDEJ	000213	7:2000						
. 1	.	IFA	220000	351326	102113					•
664200	Veoc14		260200	066150	CC(215		,			
94,4000	LEJUON	1FRED	000312	000313	000352	000323	20C34C			
255200	310000	IHA	05030	051030	502 JJ	145000				
# # # # # # # # # # # # # # # # # # #	45000A	1182	cc1103	0,0265	200	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7			5,	
									-145	
				-						

		e in k assissant and	~	1		1			
0			06230		02(7)30				5-146
			000221		000263			ENO	
to manager of annual adoptions.	Kra13		000163		222000 222000	000345		KTHETA	
	96.		000154	262000	CCC50 CCC217 CCC160	221300		IEAIEX	
ne indressite company section is a	76. 20.59.06.	36.C262	000325 000112 000304	360251 660255 000156	000043 000043 000211 000152	020314		ster	, , , ,
	07/06/7	0002C2 0002C1	000034	000163 000230 000230 000071 0000076	0000126 000126 0000144 0000046	000311 000115 000115 000277 000004		CUTPTC	
	10 m	IJ IJM1	ILFREG IPERIOD	ITHETAI ITHETAI ITHETAJ IZFACT JTHETAI	NA NACOES	NLCBES NMICGR NKECBCK NIHETA NTHETAZ POIST		INPUTE	,
O :	.2.3#1	V00032 V00031	V00040 V00016	1 1	V00027 V00015 V00015 V00026	r r	S III	ES REWINN	
o Ox	COMPILER (VE	000470	000455	000000002 003777092 000460 60C461 006456	000466 000466 000467 000457	00C475 CUC467 0CC467 00C465 00777702 00777602	1 1	F INDIDECTS L REFERENCES CENTRY	1/
0	Y ×				,			COUG42	

		Section 300 and all the months		and the second s	Annual Control of the	TO THE PERSON NAMED IN COLUMN	și.
C						5-147	
	RCA13						india de demonstrata de destrata de de
The second secon	76. 20.59.06.						the territory of the second se
C	07/08/76						ender in der der der der der der der der der der
0 0	OC7300 USED				9 7		
o	RUNX COM						

· 東京 は、、 アイル 1000 で、 中の 1000 で、 1000 では、1000 で、 1000 では、1000 である。 1000 で、 10

The second of

	meringan e reger a primario e e constitución e mante estados.	AND AND AND AND AND AND AND AND AND AND	the state of the second	menter of the second se	Months of the control	A CANADA	Management and and and			
	Ĵ	T)	J	۰ لر	j.	Ď.	c		•	
RUNX COMPILER (VER. 2.3")	An i	.0	7.0877	20.59					4.14	
SUBPREGRAM LENGTH										
2	FFERENCE		,		, t , t , t , t , t , t , t , t , t , t				grade to the agency	
LECATION	GEN TAG	SYM TAG	REFERENCES	ES					ur kungu giri.g	
STATEMENT NUMBER REFE	REFFRENCES								\$1,4°,4°,4°,4°,4°,4°,4°,4°,4°,4°,4°,4°,4°,	
LOCATION GE 600007 LC	GEN TAG 100007	SYK TAG 125	REFERENCES 000034	\$ 2					A glader serve	
	L00017	135	010000	\$10000·						
BLCCK NAMES AND LENGTHS	THS									
VARIABLE REFERENCES									e arrive a regi	
אָט	GEN TAG VOSONG	SYM TAG	REFERENCES None	t S					9 40	
000045 VO	V00005 V00005 V00004	ILEFT IM1 IM2	600012 600012 600006	3cce37 3c3322 00c010	CC0037					No.
START CF CCRSTANTS 000040								٠	againtafairain poserir ten neemingund	
START OF TEMPORARIES CCOC42									Copyright of Copyright (1995)	
START DF INDIPECTS GCOG45									***************************************	
EXTERNAL REFERENCES	END									is
COMPILER SPACE LNUSED - 010500	USED -	037300								, .
	,						. 17.3.		5-149	

BE DISTRIBUTION DF GOLD CODES—7505 BE DISTRIBUTION DF GOLD CODES—7505 BIT GOLD II BE THE SAME SIZE AND II SERVERATED BY CORRELATING THE SHIFTING. IS GENERATED BY CORRELATING THE SHIFTING. II STALLS. II STAL	
* AUTCCGRELATION FOR SIDE LOBE DISTRIBU* * AUTCCGRELATION FOR SIDE LOBE DISTRIBU* * AUTHORS——IRA GREEN AND ROBERT GOLD * AUTHORS——IRA GREEN AND ROBERT GOLD * THEIR MAXIMUM IS 15. * HIS INITIAL CONDITION SHIET REGIST * GIS INITIAL CONDITION POLYNOMIAL * GIS INITIAL CONDITION POLYNOMIAL * GIS INITIAL CONDITION SHIET REGIST * DUTFUTS ON A SEPAFATE FILE *TAPE7* IN * CCAFIGURATION OF THE AND B REGIST * THE SECUENCE OF ALL THETAS IS GENERAL * THE SECUENCE OF ALL THE AND SHIFTING * THAP IFA, AND IFB ARE TO BE INPUT IN * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * THE SECUENCE OF ALL THE PECISIER E IN DIT * TH	ER CONFIGURATION BINARY THE INITIAL ERS, THE PERIOD, N(C) OFS IN THIS RUN. FOR SY CORRELATING THE BINB, IPERIOD, ICGR GCTAL AND THEREFORE CIAL AND MUST BE

The second second second

	AND THE COMMENT OF THE PROPERTY OF THE PROPERT
•	
の から かっかい	
PUNX COMPILER	PILER (VER.2.3M) 07/01/76. 20.57.03. RGA10
	* FOLLOWED BY A B ON INPUT.
	* NA AND NB ARE THE DEDERS OF THE A AND B SHIFT REGISTERS.
	* IPERIOD IS THE PERIOD OF THE A AND B SHIET REGISTERS.
	* *
900000	ŀ
000010	REWIND 7
000015	_
	* CALCULATE NUMBER OF TERMS FROM THE ORUER
000021	NI = NA + 1 N2 = NB + 1
	* CALCILATE NUMBER OF TERMS IN THE CORRELATION PRODUCT POLYMOMIAL
٥٥٥ ، ١٠	NTCGR # NA*2 + 1
	* CALCULATE THE POSSIBLE VALUES OF THE AUTOCORRELATION FUNCTION.
666625	TCGF(1) = -1 ICGF(2) = - (2 ** ((EA+1)/2) + 1)
000035	(3) = 2 ++ ((NA+1)/2) (4) = IPERICD
	ZE
000050	WRITE(6,19C) NA, IFA, IHA, NB, IFB, IPERICO, ICOR 180 FCRMAT(1//* A REGISTER* I3 * STAGES*/
COC072 COC072	## B RE
778888	

the second of th

		Magaginating Association (1997) by the	State agamentage of a	Secretary or other services and services are services and services and services and services and services and services and services and services and services are services and services and services and services are services and services and services are services and services and services are services and services and services are services and services are services and services are services and services are services and services are services and services are services and services are services and services are services and services are services and services are services and services are services and services are services and services are services and services are services and services are services are services and services are services and services are services are services and services are services are	um ya mara tarkenda sepera			5-152
C								,
Recolated values of the part o	RGALO	LENGTH*)	EY CCEFFICIENT TERM.				ITIAL CENDITIENS ASSECTATED	
	07/01/76, 20,57,03, N NCC1-N(1)* 4110//1	TEPS MUST BE	CONVERTER TO A BINAEY F BEING THE CONSTANT T ATION BINARY CREFICIENTS	IF12	2	ONE MCRD	IS CATAINED FROM INIT EN MULTIPLIED BY THE MODES NET CHANGE.	
The second secon	CONDITTO	SHERT SHIFT REGISTERS	AEPRESENTATION IS CONV. I THE FIRST ELEMENT BEING ECTAL REPRESENTATION EUITPUT TABLE OF BINA. NUMBER OF TERMS	BINCUEF(IFA, IHI, NI) BINCUEF(IFA, IFI, NI) BINCUEF(IFB, IF2, NZ) PEPY(IFI, IFZ, IFIZ, NI) M ADDEC AI THE END OF	UMBER OF TERMS A CONSTANT TER	FULYNCMIAL INTO (IF12, IFF, NTCOR) A CENSIANI IEPE	CONDITION FOLYNCPIAL IS IFT RECISTER A AND THEN MIAL F.E.E.E. THIS TERM INITIAL(IGI, IFI, IHI, NI)	PMPY(1G1,1E2,1TP1,N2) 1H8(1) 1H8(2) 1H8(3)
	# *	IE (NA EG PRINT 190 FORMAT(* SIDP 1	# TAELE WITH 18 151 ARG = 2ND ARG = 4	CALL EINCE CALL BINCE CALL BINCE CALL PEPY(- 1	* COMPACT IF12 CALL CPACT * IFF = F1 * *	+ INITIAL CONDITION + FCK SHIFT REGIS + POLYNCMIAL ECK + CALL INITIAL(I	CALL PRPY(I M1 = 1HB(1) M2 = 1HB(2) M3 = 1HB(3)
•	FUNX CCPP			COC102 COO105 OOO110 OOO113		CG0116	600121	000124 000127 000130 000132

•	S S S S S S S S S S S S S S S S S S S		
BUNX CD	PILER (VER-		og springer, skiler z
CCC136 CCC136 COO141 COO147	ITEMP = K2 - M1 + 1 NCODES = ITEMP/M3 .NE. 0) NCODES=NCODES+1 OG 610 ICODE=M1,M2,M3		
000151	CALL BI VITIAL CO OF SHIET		. 12/2011
000153 000156 000161	<pre>call initial(iG2,iF2,fH2,N2)</pre>		
	IN THE BASI		
C00164 C00167 C00173	* CALL CPACILITAIGGANICDR) CALL CORLIGGAIFFEIPERICDAIRHDACA JIHETA = IPERICD - 2*IRHO *		-
000176	CUIPUI GN *IAPE7* EGR		entre les
COC230 COC230 COC230	- (
C00234 C00236 C00237	ITS(NICOR+1) = 0 ILEFT = IPERICD		a same and a same
000241	1111		area antoniconda
CO0246 CO0247 CO0247	2 = 1LEFT + 5C0 500 I=1,1M2 11 PADD(II,1IS,1G	5-15	,
		3	
			esp4

	The state of the s	3° tavo v 4. 18. 1.						
								5-154
Continue of the continue of th	96.410	OR N(1) IN THE			ALIG ANALYTIC PESULT*1			
	07/101/76	* (IG1*IE2+IG2*IE1) + (IG1*IE2+IG2*IE1)SHIETED LCULATE IRHD * THE NUMBER OF DISAGREEMENTS OR N(1 CCRRELATION PRODUCT POLYNOMIAL CALL CPACT(IG,1GG,NTCOR)	COR(IGG, IFF, IPERIOD, IRMO, C) N(C) - N(I)	ETA(I) = IFERIOD - 2*IPHO INE THE1& DISTRIBUTION 490 II=1,4 (ITHETA(I),E&,ICGR(II)) GO IN 455) ITHETA =* 110, 10X *15 NET A VANCOR(II) + 1	FIZ. FICUR)	ICODE, JIHETA, NCOR 5, 5110)	
e O-		# 1G = (1G1#1F2+1G2*1F1) # CALCULATE 1RHD = THE N # CERELATION PRODUCT * CALL CPACT(1G,1GG,N		CC IF R.	490 CONTINUE WFITE(6,492) I 492 FCRMAI(7/ * TH STGP 2 495 NCOR(II) * NCG *	1 XSHI 11 XSHI 11 XSHI 11 XSHI 11 XSHI 11 XSHI	600 CCNTINUE MP11E(7) NCDR,ICCR MP11E(6,65) ICDDE 605 FURMAT(13X U5, 511 610 CCNTINUE * STOP END	
	WOO XVIDE	000254	C0C257	000263	000273 UUC275 C00302 C00302 C00304	C00307 C00311 000314 000326	CC0327 COC336 C00350 C00350 C00353	

			And the state of t	TO CANTENIES TO A	Mir old - Th- _a nki i Sandaransinspo	prompte are acceptanted to	Greek State of the second space of States	Markon and Sulfa Surveying		·	oers at Money M			A C	iks.		
•										•						5	-155
.0					,						000311						
C							-				C00277				•		. 25-4
C	86410										292300	000466	000364	186	00000	C0C257	
Commenter of the second of the	23										000263	000341	000202	400257	171000 000307	606254	,
	76. 20.57.) E S							000200	000100	291933	000116	CC0254 C00167	
G	0710720			REFERENCE	REFERENCES 000050	000073	000243	000245			CC0231	606026	600005	000116	C00114	000251	
C			ES	SYP TAG	SYM TAG	190 200	760	600 605	- 001434	2	1	ICODE ICOR	IFA	15 5	1F12 1E2	16 166	·
C O	3.8		REFERENCES	GEN TAG	GEN TAG	C00063 L00044	100133	100170	LENGTHS	S	10004	V00040			A00007		1 1
e O	BILER (VER	LENGTH	IT FUNCTION	LOCATION GEN TAG	LOCATION	000474	000247	000327	NAMES AND LE S- 003074	REFERENCES	COC572	000566	000550	000.560	00014000	00040000	
•	PUNX COMPILER	FREGRAM	STATEMENT	3					ELOCK NA FIOBUFS-	VAPIABLE					• •		

ð			ev =		॰ इन्द्री ^व			cr a. n.ggg,		nice for			•			~~ •																/		5	5 - 1	156
0					•				000214		,											\$02030		•		262000	500157									
The second secon									000173													60(072	004000			001233	000122	000154								
Ů	,	RGA10		135000				666030	020170	804000 000408	000264											000003	C00212			201165	411000	000151								. 4
		1		המבלכם					0000065	000264	000260	006250					000306	000343	COC147	000251	03830	000034	0000	000220	000346	000162	000176	000125								
		20.57.03	000156	231333	000372	000154	000000	000241	000043	00000	6000173	000164	GC0141		000161	000161	000251	000216	CCC133	000133	000136	CC0021	CCOC61	CC0145	665.332	7 11000 7 11000	, o c o o o	000111								
O	r a ri	02/10/20	000153	750000	000127	000151	000267	000237			000170	000162	m	ACM	000125	C00157	000235	00C175	000130	000132	C00134	000015	CC0022			0000000	00000 00000	000054			,					
a			162	V H	S H	142	11	ILEFT	1PFR 10D	:	IRHD	11	ITEMP	ITHE 1A	IIPI	1122	115	JTHETA	T.	22	w.	۷ ۷	60 ·	NCOCES . ODE	I. L. P. R.	430	2	22								
8	A STATE OF THE STA	2.381	A00005	VC0021	A00020 A00001		10000	V00045	VG0026		VCOC42	ACCC10		ACCC15	A00012		1	V00C43	100033	700034	V00C35	VC0023	V00025		7	160004	VC0027	V00030			, *	ES				-
o		CCMPILER LVEF.2.	00010000	0000	0000000000	000000000	000575	000573	000554		025000	200050000	500564	222246000	CCC300CC2	00034000	00024000	000571	000561	000562	000563	000551	000553	000565	7736530	2 66000	000.555	000556	STARTSACT	l		TEMPOKAPIES		STABL OF INDIRECTS	- Tarana	
•		RUNX CCK																											STABT CE	- ا	•	START OF	225022	STADT OF	-	

(0 0.

		1	i				, 17:34/93 ⁶	· · · · · · · · · · · · · · · · · · ·		enere es especial de la cons erva-	, , , , , , , , , , , , , , , , , , , 				- Alfastinista
													5	-157	
		ľ													
	5		.						•	!				٠.]
6	-	1										,		1 .	
	3. 5.) ' '													
	u_{i}	Ì	.]					}				,		,	
			1												
	,		<u>u</u>												
			EINCOEF END	İ											
		Ì				Ì									
	3														
	1 " " " " " " " " " " " " " " " " " " "	1	H											,	
	01792	1	STOP XSh1E1												
	32		S S												
The state of the s															
			ည္												
•			OUTPIC CUTPIB												
BBQ(38 ubloom)	1		5 ಕ												
ا الماريخ الماريخ	3				1										
1	-		Z								<u>}</u>				
	20.57	1	COR											·	
		1	00												
	777]													
	19	j	IBAIEX PADD												:
•	0770	ł	4 8 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5									,	ı		
								,							
		İ	~ d	g											i i
e		1	57	201183				, i		 					
	\mathcal{L}_{i}		INPUTN	3											
				•											
			×							} 					1
•		1.	REWINA	LSED						i I					ļ
	/ER-2-3M	1	<u> </u>	4											
	3	189										-		,	
	3	A P	≿	SPACE COSZOO							<u> </u>			,	
•	# a	1 1 1 1	Z	AC.											
O	400 11 a		OBNTRY R												
	3			3											
	XNA	541 FR		PII										,	
•	PUNK COMPILER (VER.2.3M)	COOS41 EXTERNAL		COMPILER UNUSEC -									!		
	, 7	- -	i	- 7	1	1	ı	I	i	Ī	1	j	l	l	i

 L_i

۳,

SUBPROGRAM LENGTH SUBPROGRAM LENGTH OOGGOSS STATEMENT FUNCTION REFERENCES LOCATION GEN TAG REFERENCES STATEMENT NUMBER REFERENCES	
ES SYM TAG REFERENCES	
SYM TAG REFERENCES	
SYM TAG REFERENCES	The state of the s
LOCATION GEN TAG REFFRENCES	
BLCCK NAMES AND LENGTHS LARIABLE REFERENCES	
LOCATION GEN TAG REFERENCES 000034 V00004 I 000007 000021	
372°T LF COLSTANTS CO0626	
START OF TEMPORARIES	
START OF INDIRECTS 600033	•
EXTERNAL REFERENCES SBYT FNC	
COMPILER SPACE UNUSED - 010560 USED - 037300) m.
	1.518
5-159	

						<u> </u>		
0								5-160
0								
	20.57.03		(1)					the control of the co
0	92710720	XSHIET(IG, IP, N.) GR ADVANCE IN TIME R+1	GD 1D 30 IP(1) = 2*IG(1)*IP	FUST CONTAIN A C				The second secon
0	LVER -2-3M1	SUBRCUTINE LOCK TO LEFT IS THE ORDER	IF (16(1).EG.O) GO TO DO 20 I=1,N 16(1) # 16(1) + 1P(1) CCNTINUE CONTINUE	(1) = 16(1+1) LEMENT UF 16	CCNTINUE Return End			
O	a 11 a	* * * * *	20	* *	05			
•	77 T T T T T T T T T T T T T T T T T T		CCC0006 COCC010 CCCC010 CCCC010	22000	000024 000026 000026			

PUNX COMPILER (VER.2.3M) 07/01/76. 20.57.03. XS		
SUBPROGPAM LENGTH		
STATEMENT FUNCTION REFERENCES		Carrier Section
LOCATION GENTAG SYMTAG REFERENCES		
STATEMENT NUMBER REFERENCES LOCATION GEN TAG REFERENCES' 00.0020 100314 30 000006		
BLCCK NAMES AND LENGTHS		THE RESERVE THE THE PERSON NAMED IN
VARIABLE REFERENCES		kan <u>u</u> musanee pres
10CATIUN GEN TAG SYN TAG REFERENCI'S 0C0U35 VOCOO4 I 0C0CO7 0CC015 C0C021		
START CE CONSTANTS COCO30		cherke manace
START CE TEMPORARIES OCUO31		
START CF INDIRECTS 000033		
EXTERNAL REFERENCES END		
COMPILER SPACE UNUSED - 010500 USED - 037200		1.078
	5-161	

果を含めたの場合によっていた。 たたしと アンド・アンドラ とうかい こうかいある からな しゅうかい ならないさい

				1	is	
O					5	-162
6						
C	20.57.03	AT THE END MAKING NN+1	2*()			Section of the sectio
Ċ,	VER.2.3M) C7/01/76 SUBROUTINE PADD(TA.18.1C.NN)	IB WITH ZERO TERM ADDED THE NUMBER OF TERMS IA(1),IB(1),IC(1)	+ 1B(1) - IA(1) * IB(1) *			non-per las policies sprengent per ser
c ,	RUNX COMPILER (VER.2.3M)	# IC = IA (+) IB W # DIMENSION IA(100 CCNTINUE 100 CCNTINUE 1C(NN+1) = G RFTURN END			The second secon
•	AADO XVINA	200000	C0C010 C0C017 C0CC23 C0CC23			

J. Spiriter		2. C. C. C. C. C. C. C. C. C. C. C. C. C.		- All-self-self-self-self-self-self-self-se
	5-163			
i s				
Annual Contraction			037300	COMPILER SPACE UNUSED - 01050G USED - C3
and or a second				EXTERNAL REFERENCES END
				START CF INDIRECTS 000030
				START OF TEMPORARIES
				STAK1 CF CCNSTAMTS
			TAG REFERENCES CCOC17	LCCATION GENTAG SYM CCCC34 VCOCC5 I
				VARIABLE REFERENCES
				RLCCK NAMES AND LENGTHS
			TAG REFERENCES	STATEMENT NUMBER REETRENCES LOCATION GEN TAG SYM
			TAG PEFERENCES	5. 5
				STATEMENT FUNCTION REFERENCE
				PUNK COMPILER (VER.2 3M) SUBPROGRAM LENGTH
1		N. A. C. C. C. C. C. C. C. C. C. C. C. C. C.	1 .	
	C		•	

	Acres de la constante de la constante de la constante de la constante de la constante de la constante de la co	inim menchinas in the	gipatikan song.	*********	l the second property size. I	ም <i>ት</i> ገኛ - 1	pq,				-9 - 1	Se Wi- Selection	miliyahiya ara iyo iyo ara 1888	THE PERSON OF		İs																				
											,						5-165																			
INITIAL																		بالهابات المسابات المسابق والمسابق 76. 20.57.03.	·		CES		ices			CES	26000	220025	CC0026 CC0035							
07/01/			REFEREN		PEFEREN			REFEREN DODDO7	000016	000021	000025																									
		S	SYM TAG		SYM TAG			SYM TAG	II	つ に	I T NN:31					037460		***************************************																		
2.31		REFERENCE	GEN TAG	EERENCES	GEN TAG	LENGTHS		GEN TAG	VCC010	V6C011	V0C012 VC0006		S			useb -	4																			
RUNX COMPILER (VEP.2.3h)	M LENGTH	STATEMENT FUNCTION REFERENCES	LOCATION	STATERENT ALMBER REFERENCES	LGCATIEN	AND	VARIABLE REFERENCES	LOCATION	000053	000057	000055	CORSTANTS	TEMPURARIES	INDIRECTS	REFERENCES END	SPACE 010400																				
FUNX COMPILE	SUBPROGRAM 000056	STATEMENT		STATERENI		BLGCK NAMES	VARIABLE					START GF G00642	START OF	START OF	EXTERNAL	COMPILER UNUSED -																				

A MARTINE TO THE CONTRACT OF T

	mainoir for ones	<u>Spiritos de anistretion de</u>	" the waster state of control	The State and Toler Services	Paragentine, e. 2018	EANTORNIS	Pog sp der de t	- wangloo - Kan				ندع		and the substitute for	d Tjog og der og godelte vijkenspos			i S		
														•				5	-167	
XAMA		<i>;</i> 11.							960000											
76. 20.57.03.		,	SES	V.				. E.S.	000015 000033	67.00.00	000043	76.000		COCC12 606645						
2/10/20			TAG REFERENC	TAG REFERENC				TAG REFERENC		C00C17	040000	NONE OCCOSS	C00023	C00025 C00007						
		REFERENCES	GEN TAG SYM	SEN TAG SYM	100027 30	SHIS		GEN TAG SYM	200	VOCCIO IAI		ACCOOL IR		VOOUI3 K		10			, p	
T THE LVER	GPAM LENGTH	ENT FUNCTION	LUCATION G	**	0000033	NAMES AND LENGTHS	LE REFERENCES	LOCATION		000062		000057 A		000065 V	DF CONSTANTS	CF TEMPORAPIES	CF INDIRECTS	AL REFERENCES End		
• BUNY CC	SUBPRUCPAM COOOZO	STATEFENT		STATEM		ELCCK NAMES	VARIABLE								START	START	START	EXTERNAL		

1 1 4 4 5	- 100			THE PERSON NAMED IN THE PERSON NAMED IN		4 "	• • •	, ,
			,					5-169
	20.57.03.							
	92710720	EE (IP , IP A NA)		I				
C	10 m	SUBECUTINE BINCCEFTE, IPA, NA) DIMENSION IPA(1) TH = IP	DE 16 I=15NA IPA(I) = IH IH = IH/2 CONTINUE	CC 20 =1,0NA IZ = 1PA(I) IH = IZ/2 IFA(I) = IZ - 2*IH CONTINUE	PETURN End			
0	RUNX COMPILER		000007 000010 000012 C0C013	COCO15 OCC016 COCO17 COCO21 COCO24 20	920003			

	The state of the s											•,	:18	
				, pompeter	metar (a-vigamenou)	entrans		A Second		•				5-170
	81MC0EE							200020						
A CONTRACTOR OF THE PROPERTY O	0.57.03							000015 000011 000022						
C C	07.101.76. 20			REFERENCES	REFERENCES		REFERENCES	1						
C			RENCES	TAG SYM TAG	TAG SYR TAG		TAG SYR TAG	105 1 104 1H 106 1Z					.b - 037300	
• 0	RUNX COMPILER (VER 2.3M)	GRAM LENGTH	STATEMENT FUNCTION REFERENCES	LOCATION GEN TAG STATEMENT NUMBER REFERENCES	LOCALION GEN TAG	THE NAMES AND LENGTHS	VARIARIE REFERENCES LOCATION GEN TAG	000035 V00004 000035 V00004 000037 V00006	T DF CONSTANTS	RT CF TEMPOKARIES	NT CF INDIRECTS	PNAL REFERENCES END	ILER SPACE SED - 010500 USED	
•	BUNX C	SUBPRO 000060	STATEM	STATER		BLOCK	VARIAB		START (000030	START	START	EXTERNAL	COMPILER UNUSED -	

:

DENI COR CORPASS - VER 2 CTOILTE 20.57.05 PLEE				Samuel and Car Late Second	market for sulfa	ang de harist kala ta sispekkang agawa-en sunaka		Ås
DENI COR ENTRY COR ENTRY COR ENTRY COR ENTRY COR C(£1) G = INITIAL CONDITIONS POL C(£2) F = ASSCCIATED POLYNGRIAL C(£3) F = ASSCCIATED POLYNGRIAL C(£3) F = ASSCCIATED POLYNGRIAL C(£4) IRHC = NET MINIMUM NUMBER C(£5) LWINDUM = SLIDING WINCOW F X0 = 1	- VER 2. 07/01/76. 20.57.05. PLGE 2	TOMINI	SAGREE			TO X5 TO X4 WINCOW IS DEFINED,	VDOW V FOR LCOP NEI GNES C R LEFT END	DER DF G IS O SHIFT COUNT
CA CC (C (C (C (C (C (C (C (C (C (C (C (C		COR COR E1 INITIAL CONDITIONS	NET PERICE OF C		THEN USED FOR	PUT 1 II PUT 1 II AND IN EETCH 1 FETCH 1	SIPGLE SIPGLE CHANGE S INITIALI FETCH G FETCH F	IE IF LOW OTHER!
		ENT ENT ENT ENT ENT	H		X X X X X X X X X X X X X X X X X X X			

t

C

* *			CONSTANT TERM GUARANTEED IN ASSOCIATED POLYNOMIAL DEMOVER ION OBDES
*			
10 20101 NONE		-	NOS SEIFT
36551	115	X5+XC	
0325000007+	92	X5, LCOPW	IF COUNTER STILL NEGATIVE, LOCP
11 10766	6×7	xe	INITIALIZE MINIFUR ONES COUNT
03E-5GC0C2D+	79	X4.STR	IF THERE IS NO LINCOL. STORE RESULTS
14444	ex 4	7×-	OTHERWISE CHANGE SIGN FOR LOOP COUNT
12 C321C00013+ LCCP	JP PL	XIPPCREI	IF LCW CROEP OF GLEFT IS O SHIFT ONLY
364.00	IX6	X6+X0	UTHERMISE ADD COUNT
13112	8×1	x1-x2	AND DIVIDE
13 20101 NGNE1	LXI LXI	, - 1	THIE SOL
0323000015+	ā	X3.NGNE3	IE LOW GREER OF GRIGHT IS O SHIFT CHLY
37060	1x5	X 6 - X C	CIHERWISE SURTRACT COUNT
14 13332		x3-x2	AND DIVIDE
	NChea LY3	7	NOW SHIEL
37567	IX5	x6-x7	
0325600617+	٦ ٦	XSACONT	SINIBOR CONTINCE
10706	PX7	Хé	
17 36440 CENT		X++XC	INCFEMENT LOOP COUNT
03340CCC12+	9 %	X4,LCOP	IF COUNTER STILL NEGATIVE, LOGP
20 5674C SIR		84	DIH PHISE STOPE RESULTS
+1000000000	63	COR	
21	ENO		
4276C STGFAGE USED	04 STA	FERENTS	9 SYMBOLS
4276C STGRAGE USED	1	STATEMENTS	9 SYMBOLS

5₄173

		Kana Wille Da 'w		and the second s	and the second s		in the second	
u 4								5-174
						.	2,37%	
							1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
7.0								
02701								4 (3), 4
							<i>t</i> , n	
STATE OF								
								-
Vaxos								
		3/26						
				·				
	3/23	1	3/15 3/15 2/30 3/25			,		
		- -						
	3/21	1/09 3/12 2/35 2/35	3/12 3/12 2/27 3/10					
5"		* * * *	***					
	TABLE.	PROGRAM* PROGRAM* PROGRAM* PROGRAM*	PROGRAM* PROGRAM* PROGRAM*					
		1	113 PR					
	REFERENCE 17		2					
3	21			·			- 21	
803	SYMBOL IC	COR LOOP LOOP NONE	NONE 3 NONE 3 OK STR				200	

APPENDIX E.5

TABLE OF PREFERRED PAIRS OF MAXIMAL POLYNOMIALS OF DEGREE 11, 13, 15, 18, 19

a D

1				ASSET CONTRACTOR OF THE PARTY O	With Mallor throated the second	27F 20F 20F 20F 20F 20F 20F 20F 20F 20F 20		all modelles sonn S	24 0 TM	MENN EY OPEN,		: 1	mentos com	NATIONAL PROPERTY OF THE PARTY	2000		RAS MARKET
								The second second second second second second second second second second second second second second second se	1 11 11 11 11 11 11 11 11 11 11 11 11 1	,						:	
										1					:		
0 P												mage a consistence in the case of the case	1				•
··				To the state of th		The statement of the st						n de la company				The second of th	
₹:										***************************************					•		
							; † ;			:					•		
	The state of the s	REFERRED PATRS OF DEGREE 11	4445	6015	5623	6233	7335	5263	6637	5221	5747	7627	6227	7431	5265	2005	
7	·O	PREFEREN PA	4005	4445	4055	6015	7413	4143	4563	4053	5023	5623	4577	6233	6673	7237	
	•					and the deliberation was re-		•	a contract of					•	,		s en skiplinge de u.v. o

		Market and British				;	·		A THE CHARLES THE RESIDENCE TO THE PROPERTY OF		· · · · · · · · · · · · · · · · · · ·		•		* * * * * * * * * * * * * * * * * * * *	12	5-1	177
			examinable desirements of the second of the		The state of the s						· · · · · · · · · · · · · · · · · · ·	, calculation and		· · · · · · · · · · · · · · · · · · ·				
					A COLOR OF THE COL	:			,						:	the many the man man design and the many the many the many the many the many that the		
	DEGREE 11					!			;					,		,		The conditional contents of granten water. The contents was a principle with the contents of t
	PREFERRED PAIRS OF DEGREE		4505 7041	5263 5463	5361 5625	5171 4053	4707	7173 5531	5711 7243	5221 4731	6307 6651	6211 7317	5747 6765	4533 7655	4341 5545			mental and an anti-control of the state of t
O.	PREFE			The state of the s				tradicine is an appropriate to the	to the second organization decision that the		,	in the street of		· Advance of designation of college	The second secon		A Company of the second of the	

		- Adaption of the second	Q Wes t of the Section of the Secti		<u>.</u>	第 14年,大學、法學學學學,	nerellike Factories and section of the	Budos (= mallaneas) de b	the state of the s	ar ilda- al escura		:]						
•							-						•	\$	THE RELEASE OF THE PERSON OF T		5	-181
• •			SA,	on employees to the management of the first term of				and the second s				The state of the s		A LAND TO COMPANY OF THE PARTY	and the second s			
o :											the special section of the section o	to the control of the			To the state of th			
C.	15		the control of the state of the				· · · · · · · · · · · · · · · · · · ·		:									
o c -	PREFERRED PAIRS OF DEGREE	102043	102067	177775	103251	112611	117423	126007	177207	102171	161615	123067	125235	171737	122231			
•	EFERRED PA	100003	102043	110013	102067	104307	100317	103451	110075	10201	114725	103251	163005	112611	120265			
·	PRE					· · · · · · · · · · · · · · · · · · ·			e		The same distribution and supposition of the same of t			a company of the comp			5,	

		Mark of the second
	5-	-182
ORIGINAL PAGE IS OF POOR QUALITY		
		A
RS OF DEGREE 18 1431503 1763717 1763717 1032667 1032667 1703227 1703227 1176621 1176621 1176621 1176621 1176621 1176621 1176621 1176233 1571527 1623325 11623325 11623325		
PREFERED PAIRS OF DEGREE 1000047 1431503 1000077 1763717 1000077 1763717 1000173 1072617 1000201 1325427 1000347 1703227 1000407 1324243 1000517 1571527 10000517 1571527 10000757 10000557 100000557 100000557 100000557 100000557 100000557 100000557 100000557 100000557 100000557 100000557 100000557 100000557 100000557 100000557 100000557 100000057 100000057 100000057 100000057 100000057 1000000057 100000057 100000057 100000057 100000057 100000057 100000057 100000057 100000057 100000057 100000057 100000057 100000057 100000057 10000000000		
PREFER 1000 1000 1000 1000 1000 1000 1000 10		

5-183

t t			estoria ilegistra		en siep k. speech and despellations	查古拉德特象书 取样的	S./ 2+ ^l Ett Sift upplitted	on a second seco	Takkeyin a hine garan in ra		ود او نصور			dragodektokopoco	and and a subsection of the su			**			- - - -
	•					**	;		,								,	1		5-18	5
	0	7.													and the second of the second o			4 % 1, 14, 2 1 =			
					The state of the s																
	8																	•			
	8	2.3					:								1			,			
							1			!		Per despise of same a culture	:			:					
	6	7.7								1							;				,
				,					!				e e e e e e e e e e e e e e e e e e e		ge syndalos dans same				***		1 -
	6			***************************************					1				:		<u> </u>						
		80								-					!						
	8	PREFERRED PAIRS OF CEGREE	1733241	1125611	1743317	1207071	1763515	1156337	1205651	1323607	1613463	1525001	1073733	1011201	1760247	1116115					
**************************************	•	AIRS OF	173	112	116	120	176	115	120	132	161	152	101	102	176	111					- t
		ERRED P	1010211	1010313	1010463	1010613	1010615	1010727	1010741	1011041	1011055	1011245	1011261	1011267	1011333	1011347					
	C	7						-			~			¥7.₹							
	•						4 .		•	-										-	

(0;

PREFERRED PAIRS OF DEGREE 19

5-187

	of any of the second second second second second second second second second second second second second second	্বা ক্লিকেন্ডালনু প্ৰশুক্তিক কৰে হয় ব	्रामुक्तमार्थेकारके रहिमा २ च - नव्ह के व्रस्तवृत्तक्		alektrikaj pauli masta jaj, ajakunta ja masta ja	Same consideration of the same	
		: !		.		54	5-188
O	M						
		1 1 3	1				
			·	· · · · · · · · · · · · · · · · · · ·			
				ORIGINAL	PAGE IS	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
				OF POOR (UALIN		
			,				
The state of the s						5 1 1	
Commonweal and the second				,	:		
C CONSTRUCTION OF THE CONS							
	2			:		1.72	
O GREE 19	r r s	3	S E	ଳ <i>ବ</i> ବି	, , , , , ,		
O C	2032367	2113527 2112543 2172501	2173475	2243311 -2263405 2260165	2241477 2327617 2366261		
PAIR				21	111	34.	
O PREFERRED	2001557 2001637 2001645	2001651	2001733 2001735	2002067	2002117		
PR		\$ T					
						1 / 2 / 2 / 2 / 2 / 2 / 2 / 2 / 2 / 2 /	

		はなるないないないということできるとう	15mm1/40mm1/40mm1/4/16mm1/4/16mm1/5/10mm1/6/16mm1/6	克纳 - 1-25-25-26-1-3 vor. 9, vor. 4, std. 6 ili dath (1884) 4 ili dath	and the second s		
					• !	35	5-189
9							
			:				A many the
•							
8							
DEGREE 19		2					
• • • • • • • • • • • • • • • • • • •		2260507					
O PREFERED P	2002271	2002435					

APPENDIX F. 5

COMPUTER PROGRAM LISTING FOR GENERATION OF PREFERRED PAIRS OF MAXIMAL PN SEQUENCES

C

O

O

0

0

Tarry and the Part sports and and

, 1.

				and the second s	,												And the second s			1		•	:
				a manual care for the case of					:								and or of the contract of the		•				· · · · · · · · · · · · · · · · · · ·
			The second secon	7)				٠	* * * * * * * * * * * * * * * * * * * *		1					14)	0)R)F	IG. P	OO	AI R	, I Qi	PAG
	14.07.16.			IPD(7), IPR(12							; ;					IS DE LENGTH*							
in the second se	12/27/75	(1)		(254), IPC(7),											RINT 150.NR	8	~	(1,	, NR)	3 - 1 - 1			
		JA (INPUT, OUTPU	PROC	IPA (254), IPB	77.	٠		2,7	IOCT . AND. 1	1/2		2.5		SAT AST 15	12) E0.1) P	*BALANCED C	(IPC(I),I=	(IPD(I),I=1,	(IPR(I), I=1,	8011)			****
	ER (VER.2.3M)	PROGRAM IG3	OMPON	DIMENSION	ACCEPT NR	100	01 = 1	11	IPA(II) #	IOCT	_:	1 00	IPB(I	LINUE CEO3	MODO) T V	PRINT 20	2 17	4T 200	FORMAT(1H	LINU	^	END
O	RUNX COMPILI		υ υ υ **	000004	400000	000013	000014	910000	C00017		-		1	→ .	000034	-		000001	000073	2	S	000110	000112

(O O/)

SUBRDUTINE SEGZA7(IPA, IPB, NR, IPC, IDIMENSION IPA(254), IPB(254), IPC(CALL SEGZA7(IPA, IPB, NR, IPC, IDIMENSION IPA(254), IPB(254), IPC(CALL SEGZA7(IPB)) CALL SEGZA7(IPA) CALL SEGZA7(IPB) ICALL EGZA7(IPB) ICAL SEGZA7 ICAL SEGZA	INE SEGZA7(IPA, IPB, NR DN IPA(254) 127 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 27 (IPA) 28 (IPB(I)) ICGUNT 29 (IPB(I)) ICGUN 20 (IPB(I)) ICGUN 21 (IPB(I)) ICGUN 21 (IPB(I)) ICGUN 21 (IPB(I)) ICGUN 21 (IPB(I)) ICGUN 21 (IPB(I)) ICGUN 21 (IPB(I)) ICGUN 21 (IPB(I)) ICGUN 21 (IPD(I)) = 0 21 (IPD(I)) = 0 21 (IPD(I)) = 0 21 (IPD(I)) = 0 21 (IPD(I)) = 0
εz	IPD, IPR) (7), IPD(7), IPR(127) S NOT FOUND*

OR	GINAL	PAGE	18
OF	POOR	QUALI'	ľY

RUNX COMPILER	ILER	(VFP.2.3V)	12/27/75. 14.07.16.	SEC2A7
000105		IPC(1) = 1PA(151431+1)		
000110		IPD(1) = IPB(15TAX1+1)		
000113	410	CONTINUE		
000115		00 420 I=1,0k		
000117		IPP(I) = NUN(1FALISTAFT	IPP(I) = MUD(1PA(151AF1+1) + 1PE(15[AR1+1) . 2)	
000130	420	LUNITHON		
000133		PETUP1:		
600133		C.Z.u.		

CO

Ç

Ç

C

the state of the s

east	RUNX COMPILER (VER.2.3M)	(VER.2.3M) 12/27/75. 14.07.16.	
. codesti		SUBROUTINE SEQ37(IPA)	
desta.	00000	· · · · · · · · · · · · · · · · · · ·	
i de critor	£00000	DD 120 I*8,254	
adias ()	000000	IPA(I) = MOD(IPA(I-3) + IPA(I-7) , 2)	
ore-4	000013 120	CONTINUE	
	000015	RETUPN	
۸,	000016	END	

				+ IPB(I-7) , 2)			
SUBROUTINE SEG1237(IPB)	DIMENSION IPB(254)	DO 120 I=8,254	IP9(I) = MOD(I IPE(I-1) + IPE(I-2) + IPB(I-3) + IPB(I-7) , 2)	120 CONTINUE		9
15	000003	00000	000005 IF	000005	000016 120 CT	020000	000021 EN

APPENDIX G-5

J

CODE LIBRARY FOR FORWARD LINK RANGE CHANNEL MAXIMAL PN CODES OF PERIOD 2¹⁸-1 HAVING SIX OR LESS FEEDBACK TAPS IN THE GENERATING SHIFT REGISTER

SHIFT REGISTERS WITH LESS THAN OR EQUAL NUMBER OF TAPS THAN 6

0 |

;

ı ·

. 6

APPENDIX H-5

ALTERNATE CODE LIBRARY FOR MODE 1 RETURN LINK
MAXIMAL PN CODES OF PERIOD 2¹⁸-1 HAVING SIX OR LESS
FEEDBACK TAPS IN THE GENERATING SHIFT REGISTER

1000115	1004455
1000743	1004545
1000751	1004623
1001013	1004643
1002031	1004645
1002061	1004711
1002075	1005035
1002133	1005213
1002171	1005225
1002211	1005305
1002241	1005341
1002441	1005431
1002623	1005451
1002705	1005521
1002741	1006113
1003011	1006161
1003035	1006605
1003053	1007031
1003215	1010045
1003451	1010051
1003461	1010463
1003521	1010551
1004073	1010613
1004163	1010615
1004205	1010741
1004313	1011041
1004405	1011245
1004447	

) [1